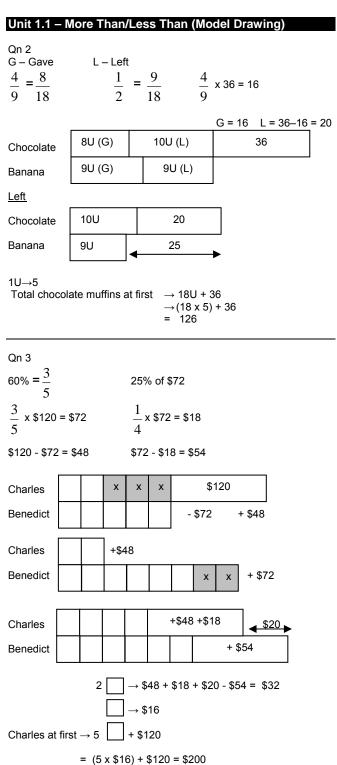
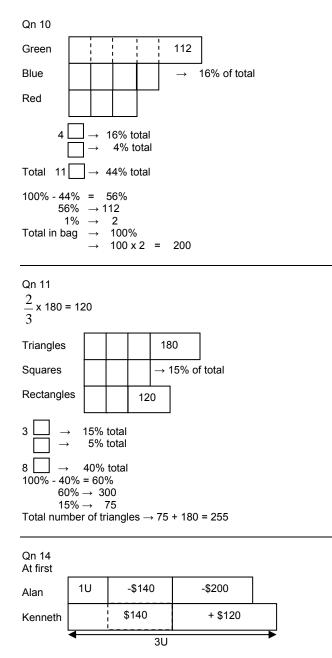
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Note : In all solutions, U represents Units

Chapter 1 More than/Less than





 $\begin{array}{rcl} 2U & \rightarrow & \$140 + \$120 \\ = & \$260 \end{array}$

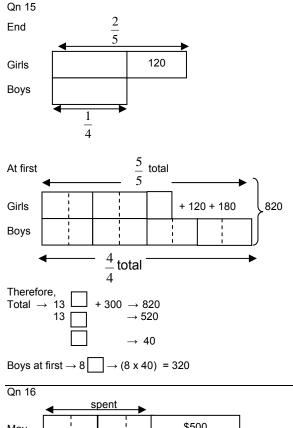
= \$260 1U → \$130

Total at first → 1U + \$340 + 1U + \$140→ 2U + \$480→ $(2 \times $130) + $480 = 740



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Unit 2.1 – Equal Intervals

Qn	4
(a)	

a)					
	Fig.	No. of	No. of	Perimeter	No. of
		squares	triangles		sticks
	1	1	2	6	8
	2	2	4	10	15
	3	3	6	14	22
	4	4	8	18	29
	:	:	:	:	:
	;	:	:	:	:
	8	8	16	6 + (7 x 4)	8 + (7 x 7)
				= 6 + 28	= 8 + 49
				= 34	= 57

- (b) Perimeter for Figure 50 \rightarrow 6 + (49 x 4) = 6 + 196 = 202 units
- (c) No. of sticks for figure 100 \rightarrow 8 + (99 x 7) = 8 + 693 = 701 sticks
- (d) 254 6 = 248 248 ÷ 4 = 62 squares Figure No = 62 + 1 = 63 No. of squares = 63

Qn 8

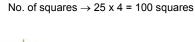
- (a) Total seats \rightarrow (4 x 4) + 2 = 18 seats
- (b) Total seats \rightarrow (20 x 4) + 2 = 82 seats
- (c) Total seats \rightarrow (100 x 4) + 2 = 402 seats
- (d) 370 2 = 368 368 ÷ 4 = 92 Diagram 92 could seat 370 students

Qn 9

(a)

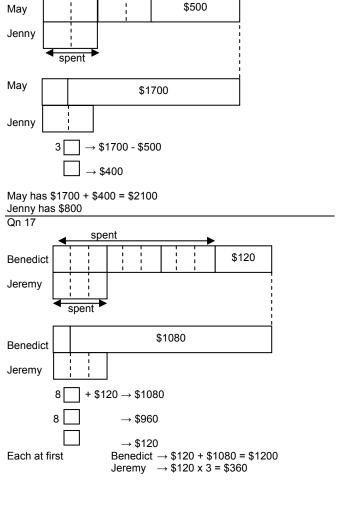
Block.	1-T	2-T	3-T	4-T
Perimeter (cm)	10	14	18	22

- (b) Perimeter of a 20-T block \rightarrow 10 + (19 x 4) = 10 + 76 = 86cm
- (c) Perimeter of a 100-T block → 10 + (99 x 4) = 10 + 396 = 406cm
- (d) 106 10 = 96 $96 \div 4 = 24$ 24 + 1 = 25-T block





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Unit 2.2 – Square Numbers Qn 1 (a) Diagram, n 2 3 4 5 1 V29 No. of shaded 1 1025 V 13 🖪 FA7 +4 squares, S +4 +4 +4 No. of unshaded 0 4 16 36 64 squares Total no. of 9 25 49 81 1 squares, T (b) Total squares in diagram $30 \rightarrow (30 + 29)^2 = 59^2$ = 59 x 59 = 3481 squares (c) Total unshaded squares $\rightarrow (49 \times 2)^2 = 98^2$ = 98 x 98 = 9604 unshaded squares (d) 29 - 1 = 28 28 ÷ 4 = 7 7 + 1 = 8 Diagram 8 has 29 shaded squares Qn 2 (a) No. of squares Total Fig. 1 1 = 11 Fig. 2 1 + 4 = 55 1 + 4 + 9 = 1414 Fig. 3 1 + 4 + 9 + 16 = 30 Fig. 4 30 (b) 1 + 4 + 9 + 16 + 25 + 36 + 49 + 64 + 81 = 285 squares Figure 9 since $9 \times 9 = 81$

Unit 2.4 – Sum of Consecutive Numbers Qn 3 (a) Area = $\frac{20x21}{2}$ x 4cm² = 840cm² 2 Perimeter \rightarrow 20 x 2cm x 4 = 160cm (b) No. of cubes for figure 40 $\rightarrow \frac{40x41}{2}$ = 820 (c) Area $\rightarrow \frac{90x91}{2} \times 4$ cm² = 16380 cm² Perimeter \rightarrow 90 x 2cm x 4 = 720cm

Unit 2.6 – Multiple of Sum of Consecutive

Qn 1 Day $1 \rightarrow 3 \times 1 = 3$ Day $2 \rightarrow 5 \times 3 = 3 + 12 = 15$ Day $3 \rightarrow 7 \times 5 = 3 + 12 + 20 = 35$ Day $4 \rightarrow 9 \times 7 = 3 + 12 + 20 + (9 + 9 + 10) = 63$

(a) No. of cubes added on Day $5 \rightarrow (11 \text{ x } 2) + (7 \text{ x } 2)$ = 22 + 14 = 36 cubes

(b) Total blocks on Day
$$10 \rightarrow (10 \times 2 + 1) \times (10 \times 2 + 1 - 2)$$

= 21 x 19 = 399

(c) Total blocks on Day
$$30 \rightarrow (30 \times 2 + 1) \times (30 \times 2 + 1 - 2)$$

= 61 x 59 = 3599

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```
Qn 2
(a) No. of small triangles \rightarrow 16
                                   \rightarrow 30
     No. of sticks
                                   \rightarrow 3 x 10
(b) Figure 5 \rightarrow 50 \times 50 = 2500 triangles
     Sticks \rightarrow 3 x (1 + 2 + 3 + .... + 50)
                 = 3 \times \frac{50x51}{2} = 3825
                              2
(c) Figure 100 \rightarrow 100 \times 100 = 10000 triangles
     Sticks
                     \rightarrow 3 \times (1 + 2 + 3 + ... + 100)
                      = 3 \times \frac{100 \times 101}{100} = 15150 \text{ sticks}
                                   2
 (d) 84 \div 3 = 28
     28 \times 2 = 56
     Since 7 x 8 = 56
     Figure 7, no. of triangles \rightarrow7 x7 = 49
Qn 5
```

(a) Total no. of dots; No of small right angled triangles T4 \rightarrow 25; 32, T10 → 11x 11 = 121; 10 x 20 = 200

- (b) Total dots for figure $20 \rightarrow 21 \text{ x } 21 = 441$
- (c) Total no. of small right angled triangles in figure 50 \rightarrow 50 x 100
 - = 5000
- (d) No, because 340 ÷ 2 = 170 is not a square number. (Eg. 49 is a square number because 7x7 = 49)

Chapter 3 Circles

Unit 3.2 – Composite Figure (Rugby ball = 2 x (Quadrant – Triangle)) Qn 3 1 shaded part \rightarrow quadrant - triangle 8 $\frac{\pi r^2}{4} - (\frac{1}{2} \times b \times h) \to [\frac{\pi}{4} \times (\frac{7}{2})^2] - [\frac{1}{2} \times (\frac{7}{2})^2]$ ≈ 3.5cm² Shaded part \rightarrow 3.5 x 8 = 28 cm² Qn 4 Area \rightarrow circle – square

→
$$\pi$$
 l^2 - 2($\frac{1}{2}$ x 16 x 8) → π (8)² - (16 x 8) ≈ 73cm²

Area
$$\rightarrow \frac{1}{4}$$
 big circle $\rightarrow \frac{1}{4} \pi r^2 \rightarrow \frac{1}{4} \pi (20)^2 \approx 314$ cm²

1

Perimeter
$$\rightarrow$$
 1 small circle + 1 big quadrant \rightarrow 2 π r + $\frac{2\pi}{4}$

$$\rightarrow 2\pi (7) + \frac{2\pi r(14)}{4} \approx 66 \text{cm}$$
Area \rightarrow quadrant – triangle $\rightarrow \frac{\pi r^2}{4} - (\frac{1}{2} \text{ x b x h})$

$$\rightarrow [\frac{\pi (14)^2}{4} - [\frac{1}{2} \text{ x (14)}^2]$$

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Unit 3.3 – Similar Figures

Qn 3 Diameter (M) : Diameter (B) Diameter (S) : 4 8 12 \rightarrow = 1 2 3 Area (M) Area (B) Area (S) = 1 4 9 Shaded part \rightarrow 9U – 4U – 1U= 4U Area of small semi-circle \rightarrow 1U = π (2)² ≈ 6.3 Area of shaded \rightarrow 4U \rightarrow 4 x 6.3 \approx 25cm² Perimeter of shaded part ightarrow 1 big circle ightarrow 2 π r $\rightarrow 2\pi$ (6) ≈ 38cm Qn 6

Diameter (S) \rightarrow 72 ÷ 4 = 18 cm Radius \rightarrow 9 cm Area of small circle \rightarrow 1 U $\rightarrow \pi$ (9)² = 81 π cm² Area of shaded part \rightarrow 81 π x 8= 648 π cm²

Qn 8

Perimeter \rightarrow 1 quadrant + 1 semi + 16 \rightarrow 1 semi-circle(big) + 16 $\rightarrow \pi r$ + 16 = π (16) + 16 \approx 66cm Area of (quadrant) $\rightarrow \frac{\pi (16)^2}{4} \approx 201.1 \text{ cm}^2$ Area of (semi) \approx 100.6cm² Shaded $\rightarrow 201.1 - 100.6$ $\approx 101 \text{ cm}^2$

Unit 3.4 – Cut and Paste

Qn 5 Area of shaded part \rightarrow area of sector $\rightarrow \frac{120}{360} \times \pi (10)^2$ $\approx 105 \text{cm}^2$ Qn 7 Area of shaded part \rightarrow area of triangle $\rightarrow \frac{1}{2} \times 16 \times 8 = 64 \text{ cm}^2$

Qn 10

Square – quadrant
$$\rightarrow$$
 (12)² – $\frac{\pi (12)^2}{4} \approx 30.9 \text{ cm}^2$
Area of region Z \rightarrow 30.9 ÷ 2 \approx 15.5 cm²
Shaded area \rightarrow semi-circle – region Z
 $\rightarrow \frac{\pi (12)^2}{2}$ - 15.5 \approx 211 cm²

Qn13

Area of shaded \rightarrow big semi – triangle + rectangle(after cut N paste)

$$\rightarrow \frac{\pi (14)^2}{2} - \frac{1}{2} (28)(10) + (14x7) ≈ 266 cm^2$$

Unit 3.5 Overlapping Method

Qn 4 Triangle $\rightarrow 48 \text{cm}^2$ $\frac{1}{3}$ triangle $\rightarrow 16 \text{cm}^2$ Area of 1 circle $\rightarrow \pi \times 6 \times 6 \approx 113.1 \text{ cm}^2$ $113.1 - 48 = 65.1 \text{ cm}^2$ $65.1 \div 3 = 21.7 \text{ cm}^2$ Area of 1 shaded $\rightarrow 21.7 \text{ cm}^2 - 16 \text{ cm}^2 = 5.7 \text{ cm}^2$ Area of shaded parts $\rightarrow 5.7 \text{ cm}^2 \times 3 = 17.1 \text{ cm}^2$

Qn 5

Area of Region A
$$\rightarrow$$
 rectangle – quadrant

$$= (8 \times 4) - \frac{\pi(4)^2}{4} \approx 19.4 \text{ cm}^2$$

Shaded region \rightarrow Big semi-circle - (2 x region A) = $\frac{\pi(8)^2}{2}$ - (2 x 19.4) \approx 62cm²

Qn 7

Areas X + A \rightarrow quadrant – small semi-circle

$$\rightarrow \frac{\pi(14)^2}{4} - \frac{\pi(7)^2}{2} \approx 77.0 \text{cm}^2$$
Areas Y + A \rightarrow square - quadrant $\rightarrow (14 \text{ x}14) - \frac{\pi(14)^2}{4}$

$$\approx 42.1 \text{cm}^2$$
Difference between X and Y $\rightarrow 77 - 42.1 \approx 35 \text{cm}^2$

Chapter 4 Speed

Unit 4.1 - Journey by Parts

To find the average speed for the whole journey, we must first find the total distance from Town A to B.

Distance $(1^{st} 2h) \rightarrow 24$ km/h x 2h = 48km

 $\frac{4}{2}$ Distance \rightarrow 48km

5

Qn6

 $\frac{1}{5}$ Distance \rightarrow 12km

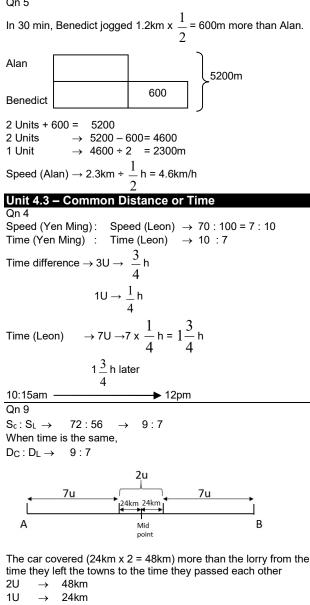
Whole distance \rightarrow 12km x 5 = 60km

Average speed for whole journey $\rightarrow \frac{60km}{3h}$ = 20km/h

Unit 4.2 – Journey in Opposite Direction					
Qn 4					
Distance (Janet) \rightarrow	80km/h x 2h =	160km			
Distance (Tommy) \rightarrow	310km – 160km =	150km			
Speed (Tommy) \rightarrow	150km ÷ 2 =	75km/h			



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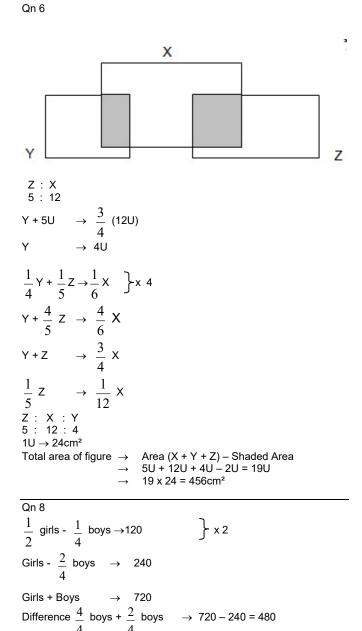
Distance from A to B \rightarrow 16U \rightarrow 16 x 24 = 384km

Chapter 5 Simultaneous

Unit 5.1 – Simultaneous (Fraction of different quantities)

Qn 4 circle + $\frac{1}{3}$ rectangle $\rightarrow \frac{2}{5}$ square $\left\{ \begin{array}{c} x & 3 \end{array} \right\}$ $\frac{1}{4}$ $\frac{3}{4}$ circle + rectangle $\rightarrow \frac{6}{5}$ square Circle + rectangle $\rightarrow \frac{7}{r}$ square $\frac{1}{4}$ circle $\rightarrow \frac{1}{5}$ square Circle : Square 4 5 4U + rectangle $\rightarrow \frac{7}{5} \times 5 = 7U$ \rightarrow 3U Rectangle Circle : Square : Rectangle 4 : 5 : 3

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 $\frac{6}{4} \text{ boys} \to 480$ $\frac{3}{2} \text{ boys} \to 480$

 $boys \rightarrow 160$

Boys \rightarrow 160 x 2 = 320

1

2

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Chapter 6 Percentage

Qn 3	– Percentage
(a) Adult Child	$s \rightarrow 80\%$ ren $\rightarrow 20\%$
Female	\rightarrow 30% of 80% $\rightarrow \frac{3}{10} \times 80\% = 24\%$
	→ 80% - 24% = 56%
	\rightarrow 60% of 20% $\rightarrow \frac{6}{10}$ x 20% = 12%
Boys Boys - Gi	
Total 100	% of audience \rightarrow 1000 people.
Children If 80% of 1% o 20% Woman a	umber of children and men remained the same, + male \rightarrow 76% = 760 remaining people \rightarrow 760 f remaining people \rightarrow 9.5 of remaining people \rightarrow 9.5 x 20 = 190 women t first \rightarrow 240 tho left \rightarrow 240 - 190 = 50
0n 5	
Qn 5 Fixed Unfixed	$\begin{array}{ccc} \rightarrow & 40\% \ (2U) \\ \rightarrow & 100\% \ (5U) \end{array} \begin{array}{c} \rightarrow x \ 5 & \rightarrow 10U \\ \rightarrow x \ 5 & \rightarrow 25U \end{array}$
Fixed Unfixed	$ \begin{array}{ccc} \rightarrow & 80\% \ (4U) \\ \rightarrow & 20\% \ (1U) \end{array} \right\} \begin{array}{c} x \ 7 & \rightarrow 28U \\ x \ 7 & \rightarrow \ 7U \end{array} $
Transfer	
Total	$\begin{array}{rrrr} 1U & \rightarrow & 10 \text{ pieces} \\ \rightarrow & 35U & \rightarrow & 35 \text{ x } 10 \text{ = } 350 \text{ pieces} \end{array}$
Qn 8	00%/ D
50% A	
$\frac{1}{2}$ A	$\rightarrow \frac{10}{10}$ B
$\frac{3}{6}$ A	$\rightarrow \frac{3}{10} B$
A : B	\rightarrow 6 : 10
C is 50%	of A + B
$C \rightarrow$	$\frac{1}{2}$ X 16U \rightarrow 8U
Removed	$\frac{1}{4} \times 8U = 2U$ (in C)
6 : 10 :	
4U 1U No. of ora	$ \begin{array}{ccc} \rightarrow & 12 \\ \rightarrow & 3 \\ \text{inges in A} & \rightarrow & 6U & \rightarrow & 6 \times 3 = 12 \end{array} $
Qn 10	
oney 7	5% + \$30 (book) 60% + \$20 (CD) 5% - \$30
r	emainder40% - \$20 (left)
10% rom	\$64

Qn 10 (cont) 20% remainder \$42 \rightarrow \$42 x 5 = \$210 Remainder \rightarrow 75% total - \$30 \rightarrow \$210 75% total \rightarrow \$240 25% total \rightarrow \$80 Total \rightarrow \$80 x 4 = \$320 Qn 12 $\rightarrow 80\%$ Jenny Daryl \rightarrow 100% Jenny left \rightarrow 80% of 80% \rightarrow 64% Daryl (end) \rightarrow 64% x 2 = 128% Increase (Daryl) 28% of cards \rightarrow 56 \rightarrow 1% of cards \rightarrow 2 Jenny at first \rightarrow 80% \rightarrow 80 x 2 = 160 pieces Qn 13 Red \rightarrow 120% (6U) } _{x 3} \rightarrow 18U 100% (5U) Blue ightarrow 15U \rightarrow \rightarrow 18U → 90% (9U) Red ∫x 2 100% (10U) Green \rightarrow $\rightarrow 20U$ Total No. x Value Red 18U x $2 \rightarrow$ 36U Green $20U \ x \quad 5 \rightarrow$ 100U Blue 15U x $3 \rightarrow$ 45U = 724 Total 181U 1U $\rightarrow 4$ Red balls \rightarrow 18U \rightarrow 18 x 4 = 72 <u>Qn 14</u> : <u>Susan</u> Jason 75% <u>3U</u> x 5 +48 }_100% ∫<u>x 6</u> At first : 4U <u>x 5</u> Change +4 End (120%) 5 x 6p : 5p x 6 (100%) Jason 15U 240 Susan 24U 24 $9U \rightarrow$ 240 - 24 = 216 $1U \rightarrow$ 24 Jason at first \rightarrow 3U \rightarrow 3 x 24 = 72 Unit 8.1 – Algebra Qn 7 (a) = $\frac{x}{4}$ cm Total perimeter \rightarrow 12U \rightarrow X cm $1U \rightarrow \frac{x}{12}$ cm Shortest length $\rightarrow 3U \rightarrow 3x(\frac{x}{12}) = \frac{x}{4}$ cm (b) Since X = 24cm; Shortest = 6cm \rightarrow 4U \rightarrow 4 x ($\frac{24}{12}$) \rightarrow 8cm 2nd shortest Area of triangle $\rightarrow \frac{1}{2} \times 6 \times 8 = 24 \text{cm}^2$



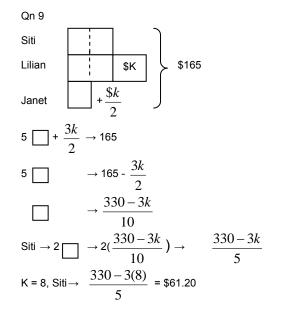
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40% remainder \rightarrow \$20 + \$64 = \$84

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Unit 9.1 – Revision of Key Constructs Qn 12

Case 1 : + 10 red beads Ratio Red : Blue 2 : 3 Case 2 : +10 red beads + 30 blue beads 1 : 3 (x2) 2 : 6

Blue changed by 3 units \rightarrow 3u \rightarrow 30 beads 1u \rightarrow 10 beads

Red beads \rightarrow 2units \rightarrow 2 x 10 beads = 20 beads Number of beads \rightarrow 20 – 10 = 10 beads

Qn 13

=	90% female $\frac{9}{10}$ female
=	$\frac{72}{80}$ female
	90U + 80U = 170U 170 members 1 member
	=

Total this year \rightarrow 144U \rightarrow 144 members

Qn 16

\$834 - \$66 = \$768 $\$768 \div 2 = \384 Pants $\rightarrow \$384 + \$66 = \$450$ Shirts $\rightarrow \$384$ 3U of pants cost \$450 4U of shirts cost \$450 4U of shirts cost \$384 1U of pants cost \$150 1U of shirts cost \$96 Difference in 1U \rightarrow \$54 No. of items in 1U \rightarrow \$54 \div 9 = 6 Total shirt + pants bought \rightarrow 7U x 6 = 42

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Ωn	1	7
u i		1

Item	No. of Boxes	х	Item	Total
Blue	Red + 12	х	120	120Red + 1440
Red	Red	х	150	150Red

Comparing the total of items (plates vs cups) Cups \rightarrow Plates + 120 150 Red \rightarrow 120 Red + 1440 + 120 30 Red \rightarrow 1560 Number of Red boxes \rightarrow 1560 ÷ 30 = 52 Number of Blue boxes \rightarrow 52 + 12 = 64 Total Plates \rightarrow 64 x 120 = 7680

Qn 18

$\frac{1}{3}$ Lim =	$\frac{3}{4}$ Zhang]		
lim	$\frac{\frac{3}{4}}{4}$ Zhan 1 : Zha : 4U + 50 : 5p _	na		
Lim 45U				
Zhang	24U	300	750	
$(45-24)U \longrightarrow 21U \longrightarrow 1050$				

 $\begin{array}{ccc} 1U & \rightarrow 50 \\ \text{Total ducks} & \rightarrow 13U \rightarrow 13 \text{ x } 50 \text{ = } 650 \end{array}$

Qn 19

Total shaded area = $\frac{1}{2}$ x 20 x 17 x 4 = 680cm² Since AB = BE but AB = BC Therefore EB = BC = CF = 60 ÷ 3 = 20cm

Qn 24

 (a) No. of shaded tiles = 20 No. of plain tiles = 16
 (b) Shaded 8 + 8 (4) = 40

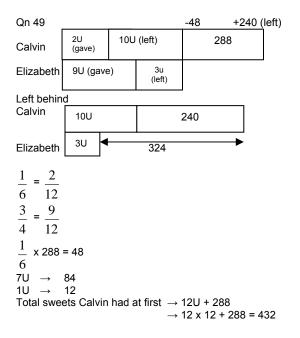
, ,	Plain	9 x 9 ິ	= 81
	Total	\rightarrow 40 + 81	= 121

Qn 25

Assume all delivered successfully, Total earned \rightarrow \$25 x 500 = \$12500 Amount refunded \rightarrow \$12500 - \$9500 = \$3000 No. of parcels damaged \rightarrow \$3000 \div (\$25 +\$15) = 75 No. of parcels delivered successfully \rightarrow 500 - 75 = 425 parcels



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Sample Examination Paper 2 – Booklet B

12. $\begin{array}{cccc} S_1\ :\ S_2 & T_1\ :\ T_2 \\ 10\ :\ 12 & 6 & :\ 5 \\ 5\ :\ 6 \\ 11U \rightarrow & 55min \\ 1U \rightarrow & 5\ min \\ T_1\ (home\ to\ nearby\ park) \rightarrow 6U \rightarrow \ 6\ x\ 5=\ 30min \end{array}$

16.

$ \begin{array}{c} $		_ : <u>Roy</u> : 10U (100%)} <u>+25</u>	
Elias	15U	250	
Roy	40U	100	

 $\begin{array}{l} 25U{\rightarrow}\ 150\\ 1U\ {\rightarrow}\ 150\ \div\ 25\ =\ 6\\ Elias\ at\ first \ {\rightarrow}\ 3U{\rightarrow}\ 3\ x\ 6\ =\ 18 \end{array}$