

5

Primary

Based on Latest
MOE Syllabus



+hinkingMath@
onSponge

CONQUER PROBLEM SUMS

- Proven strategies used by top performing schools to conquer problem sums
- Structured and guided approach to support learning in school
- Challenging questions to excel in P5 Mathematics

Ammiel Wan
M.Ed, B(Biz), PGDE

www.onsponge.com



Answers for P5 Conquer Problem Sums

For full solutions, please visit www.onsponge.com to download.

Chapter 1 Whole Numbers

Unit 1.1 – More Than/Less Than

Qn 1	210 shells	Qn 2	102 sweets
Qn 3	105 muffins	Qn 4	\$140
Qn 5	32 stickers	Qn 6	53 boys

Unit 1.2 – More Than/Less Than (External Unchanged)

Qn 1	114 adults	Qn 2	80 chocolates
Qn 3	165	Qn 4	\$280
Qn 5	32 pupils	Qn 6	96 muffins

Unit 1.3 – Equal Stage (Beginning/End)

Qn 1	14 boys	Qn 2	51 cards
Qn 3	55 oranges	Qn 4	66 stickers
Qn 5	84 magnets	Qn 6	55 pears

Unit 1.4 – Constant Difference Between Individuals

Qn 1	4 years ago	Qn 2	4 years ago
Qn 3	180 children	Qn 4	41 adults
Qn 5	72 sweets	Qn 6	\$76

Unit 1.5 – Number of Units x Value of Units

Qn 1	60 cars		
Qn 2	72 chickens		
Qn 3	(a) 30 plates	(b)	\$290
Qn 4	25		
Qn 5	120 adults		
Qn 6	(a) 12	(b)	\$500

Unit 1.6 – Key Construct: Simultaneous Concept

Qn 1	4 small cubes	Qn 2	350g
Qn 3	\$1.20	Qn 4	\$6.50
Qn 5	800g	Qn 6	\$80
Qn 7	17 pieces		

Unit 1.7 – Key Construct: Excess and Shortage

Qn 1	\$51.20		
Qn 2	\$1058		
Qn 3	(a) 0.35ℓ	(b)	9.95ℓ
Qn 4	235 beads		
Qn 5	178 adults		
Qn 6	(a) 96g	(b)	62 pies
Qn 7	\$15.80		

Unit 1.8 – Key Construct: Gap and Differences

Qn 1	84		
Qn 2	168		
Qn 3	312		
Qn 4	(a) 120 pens	(b)	$\frac{2}{5}$
Qn 5	(a) 105 cups	(b)	\$1400

Chapter 2 Fraction

Unit 2.1 – Part-whole Relationship (Type 1)

Qn 1	(a) $\frac{9}{20}$	(b)	\$60
Qn 2	(a) $\frac{2}{15}$	(b)	\$180
Qn 3	(a) $\frac{3}{14}$	(b)	\$224
Qn 4	25 muffins	Qn 5	\$3000
Qn 6	1050 students		

Unit 2.2 – Part-whole Relationship (Type 2)

Qn 1	\$3700	Qn 2	\$108
Qn 3	\$4050	Qn 4	\$189
Qn 5	40 students		
Qn 6	240 participants		

Unit 2.3 – Part-whole Relationship (Type 3)

Qn 1	\$65	Qn 2	\$320
Qn 3	48 students	Qn 4	\$78
Qn 5	\$400	Qn 6	\$3000

Unit 2.4 – Equal Fractions

Qn 1	\$456	Qn 2	\$840
Qn 3	1560 students	Qn 4	\$120
Qn 5	120 chocolate cookies	Qn 6	\$120

Unit 2.5 – Repeated Identity

Qn 1	12 banana muffins	Qn 2	171 sweets
Qn 3	301 students	Qn 4	400 people
Qn 5	$\frac{18}{19}$	Qn 6	36 cm ²

Unit 2.6 – External Unchanged

Qn 1	600 mℓ	Qn 2	750 children
Qn 3	64 students	Qn 4	48 fruits
Qn 5	84 members	Qn 6	800 mℓ

Unit 2.7 – Unchanged Total

Qn 1	84 students	Qn 2	25 stickers
Qn 3	200 pieces	Qn 4	60 questions
Qn 5	\$112	Qn 6	\$240

Unit 2.8 – Constant Difference

Qn 1	21 children	Qn 2	4 years old
Qn 3	10 years' time	Qn 4	12 cards
Qn 5	56 kg	Qn 6	184 cm ²

Unit 2.9 – Number of Units x Value of Units

Qn 1	85 girls	Qn 2	75 green marbles
Qn 3	72 people	Qn 4	1000 students
Qn 5	42 coins	Qn 6	100 adults

Unit 2.10 – Key Construct: Fraction As An Object

Qn 1	$\frac{11}{12} \ell$	Qn 2	$1\frac{2}{3} \ell$
Qn 3	$\frac{13}{18} \text{ kg}$	Qn 4	$1\frac{7}{8} \text{ m}$
Qn 5	$2\frac{1}{5} \text{ kg}$	Qn 6	$\frac{1}{5} \text{ m}$
Qn 7	(a) 16 cups	(b) $\frac{1}{10} \ell$	

Chapter 3 Rate**Unit 3.1 – Rate Involving One Object**

Qn 1	270 plates	Qn 2	12 houses
Qn 3	\$12.60	Qn 4	162 km
Qn 5	\$400	Qn 6	$4\frac{4}{9}$ days

Unit 3.2 – Rate Involving Two Different Objects

Qn 1	\$16.30		
Qn 2	(a) \$21	(b) \$6	
Qn 3	\$164	Qn 4	\$12
Qn 5	\$532		
Qn 6	(a) \$5.70	(b) 13 min	

Unit 3.3 – Key Construct: Rate involving 2 Different Objects

Qn 1	10 stickers	Qn 2	6 days
Qn 3	$2\frac{2}{3}$ days		
Qn 4	(a) Machine A	(b) 49 min	
Qn 5	11.45 a.m.		
Qn 6	(a) 80 toys		
	(b) Please refer to Full Solutions for the answer		
	(c) 4.30 p.m.		

Chapter 4 Angles I**Unit 4.1 – Angles on a Straight Line**

Qn 1	48°	Qn 2	40°
------	-----	------	-----

Qn 3	$\angle x = 45^\circ; \angle y = 75^\circ$
Qn 4	$\angle x = 45^\circ; \angle y = 90^\circ; \angle z = 45^\circ$
Qn 5	$\angle x = 54^\circ; \angle y = 56^\circ$

Unit 4.2 – Vertically Opposite Angles

Qn 1	$\angle x = 50^\circ; \angle y = 25^\circ$
Qn 2	80°
Qn 3	$\angle x = 80^\circ; \angle y = 40^\circ$
Qn 4	$\angle x = 40^\circ; \angle y = 20^\circ$
Qn 5	$\angle x = 32^\circ; \angle y = 74^\circ$
Qn 6	$\angle x = 42^\circ; \angle y = 55^\circ$
Qn 7	$\angle x = 72^\circ; \angle y = 24^\circ; \angle z = 72^\circ$

Unit 4.3 – Alternate, Corresponding & Interior Angles

Qn 1	$\angle x = 37^\circ; \angle y = 50^\circ$
Qn 2	$\angle a = 31^\circ; \angle b = 80^\circ$
Qn 3	$\angle x = 28^\circ; \angle y = 30^\circ; \angle z = 90^\circ$
Qn 4	$\angle a = 45^\circ; \angle b = 135^\circ$
Qn 5	171°
Qn 6	$\angle a = 119^\circ; \angle b = 30^\circ$
Qn 7	$\angle p = 25^\circ; \angle q = 80^\circ$
Qn 8	$\angle x = 30^\circ; \angle y = 95^\circ; \angle z = 150^\circ$

Unit 4.4 – Isosceles Triangle

Qn 1	105°
Qn 2	25°
Qn 3	(a) $\angle PRS = 110^\circ$ (b) $\angle RST = 40^\circ$
Qn 4	20°
Qn 5	$\angle x = 25^\circ; \angle y = 60^\circ$
Qn 6	$\angle x = 68^\circ; \angle y = 44^\circ; \angle z = 38^\circ$
Qn 7	$\angle x = 25^\circ; \angle y = 240^\circ$
Qn 8	123°
Qn 9	(a) $\angle PRS = 110^\circ$ (b) $\angle RST = 40^\circ$

Chapter 5 Angles II (Closed Figures)**Unit 5.1 – Interior and Exterior Angles Within a Triangle**

Qn 1	55°	Qn 2	77°
Qn 3	$\angle y = 20^\circ; \angle z = 76^\circ$		
Qn 4	$\angle x = 76^\circ; \angle y = 96^\circ$		
Qn 5	320°	Qn 6	10°
Qn 7	160°	Qn 8	360°
Qn 9	$\angle x = 92^\circ; \angle y = 122^\circ$		

Unit 5.2 – Angle Properties Within a Rhombus

Qn 1	60°		
Qn 2	(a) $\angle QPR = 33^\circ$ (b) $\angle QCB = 96^\circ$		
	(c) $\angle RSC = 63^\circ$		
Qn 3	25°	Qn 4	15°
Qn 5	(a) 55°	(b) 10°	

- Qn 6 $\angle x = 72^\circ$; $\angle y = 43^\circ$
 Qn 7 (a) $\angle x = 32.5^\circ$ (b) $\angle y = 45^\circ$
 Qn 8 $\angle x = 55^\circ$; $\angle y = 95^\circ$
 Qn 9 $\angle x = 17.5^\circ$; $\angle y = 35^\circ$
 Qn 10 $\angle x = 105^\circ$; $\angle y = 15^\circ$

Unit 5.3 – Angle Properties Within a Parallelogram

- Qn 1 $\angle x = 15^\circ$; $\angle y = 60^\circ$; $\angle z = 75^\circ$
 Qn 2 $\angle x = 25^\circ$; $\angle y = 67^\circ$; $\angle z = 33^\circ$
 Qn 3 (a) $\angle SRU = 44^\circ$ (b) $\angle PSR = 124^\circ$
 Qn 4 (a) $\angle ADC = 20^\circ$ (b) $\angle CAD = 130^\circ$
 (c) $\angle ACB = 130^\circ$

Unit 5.4 – Angle Properties Within a Trapezium

- Qn 1 (a) 48° (b) 32°
 Qn 2 $\angle x = 34^\circ$; $\angle y = 34^\circ$
 Qn 3 $\angle x = 94^\circ$; $\angle y = 49^\circ$
 Qn 4 42°
 Qn 5 (a) $\angle t = 69^\circ$ (b) $\angle y = 15^\circ$
 (c) $\angle x = 72^\circ$ (d) $\angle u = 57^\circ$

Unit 5.5 – Angle Properties Within a Trapezium

- Qn 1 69° Qn 2 11°
 Qn 3 $\angle BGC = 14^\circ$; $\angle CDG = 110^\circ$
 Qn 4 67.5°
 Qn 5 38°
 Qn 6 (a) $\angle ZNM = 58^\circ$ (b) $\angle XMZ = 64^\circ$
 Qn 7 (a) $\angle EDB = 113^\circ$ (b) $\angle AEB = 128^\circ$

Chapter 6 Area of Triangle

Unit 6.1 – Area of Triangle

- Qn 1 Height = AB Height = AF
 Height = DC Height = AB
 Qn 2 Base = 12 cm; Height = 16 cm
 Qn 3 Base = 4 cm; Height = 7 cm
 Qn 4 Base = 5 cm; Height = 20 cm
 Qn 5 Base = 14 cm; Height = 7 cm
 Qn 6 Base = 12 cm; Height = 3 cm
 Qn 7 12 cm Qn 8 12 cm
 Qn 9 10 cm Qn 10 42 cm

Unit 6.2 – Finding the Area of a Triangle in Unit Squares

- Qn 1 (a) 14 cm^2 (b) 12 cm^2
 Qn 2 (a) 11 cm^2 (b) 15 cm^2
 Qn 3 (a) 23.5 cm^2 (b) 13 cm^2
 Qn 4 (a) 16.5 cm^2 (b) 20 cm^2

Unit 6.3 – Triangle with Common Base or Height

- Qn 1 32 cm^2 Qn 2 100 cm^2

- Qn 3 150 cm^2 Qn 4 200 cm^2
 Qn 5 100 cm^2 Qn 6 18 cm^2
 Qn 7 17.5 cm^2

Unit 6.4 – Triangles with Common Bases

- Qn 1 60 cm^2 Qn 2 120 cm^2
 Qn 3 16 cm Qn 4 62 cm
 Qn 5 48 cm^2 Qn 6 230 cm^2
 Qn 7 150 cm^2 Qn 8 150 cm^2

Unit 6.5 – Composite Figures Involving Triangles

- Qn 1 240 cm^2 Qn 2 480 cm^2
 Qn 3 240 cm^2 Qn 4 49 cm^2
 Qn 5 44 cm; 42 cm

Chapter 7 Percentage

Unit 7.1 – Percentage Increase

- Qn 1 425 pebbles Qn 2 270 workers
 Qn 3 360 pupils Qn 4 \$300
 Qn 5 \$4000 Qn 6 240 boys

Unit 7.2 – Multiplication in Percentage

- Qn 1 \$400 Qn 2 \$4000
 Qn 3 \$1000 Qn 4 200 litres
 Qn 5 200 blue marbles Qn 6 \$2160
 Qn 7 10% Qn 8 5%
 Qn 9 130 cm Qn 10 56.25%
 Qn 11 \$3200 Qn 12 \$3600

Unit 7.3 – Overlapping Percentage

- Qn 1 300 students Qn 2 30 children
 Qn 3 200 students Qn 4 104 students

Unit 7.4 – GST and Annual Interest

- Qn 1 \$480 Qn 2 \$1850
 Qn 3 \$817.50 Qn 4 \$118.30
 Qn 5 \$2092.80 Qn 6 \$1962

Unit 7.5 – Simple Interest

- Qn 1 \$32 137.50 Qn 2 \$15 000
 Qn 3 \$34 200 Qn 4 \$336 000
 Qn 5 \$3888 Qn 6 \$12 500

Unit 7.6 – Discount and Percentage Discount

- Qn 1 \$10 Qn 2 15%
 Qn 3 \$280 Qn 4 \$128.25
 Qn 5 \$2.50 Qn 6 \$250

Unit 7.7 – Equal Fractions

- Qn 1 112 stickers Qn 2 \$300
 Qn 3 136 students Qn 4 \$170
 Qn 5 200 chocolate muffins Qn 6 330 students

Unit 7.8 – External Unchanged

Qn 1	30 students	Qn 2	12 children
Qn 3	30 lemons	Qn 4	36 boys

Unit 7.9 – Repeated Identity

Qn 1	150 cards	Qn 2	200 cookies
Qn 3	100 marks	Qn 4	154 people
Qn 5	188 marbles	Qn 6	55 more log cake
Qn 7	60 books		

Unit 7.10 – Unchanged Total

Qn 1	80 adults	Qn 2	200 pieces
Qn 3	180 pieces	Qn 4	150 pages
Qn 5	70 pages	Qn 6	\$156
Qn 7	100 cookies		

Unit 7.11 – Constant Difference

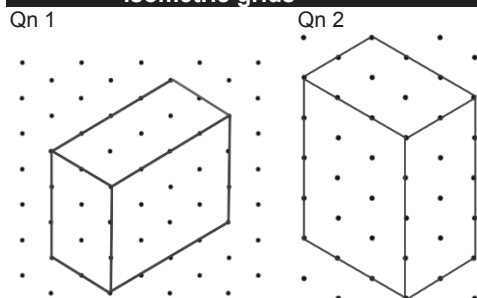
Qn 1	48 students	Qn 2	\$450
Qn 3	504 students	Qn 4	825 shirts
Qn 5	80 cm ²	Qn 6	6 years old

Unit 7.12 – External Changed

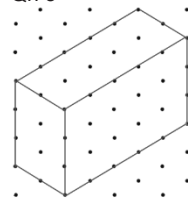
Qn 1	\$31.20	Qn 2	36 stickers
Qn 3	X = 1620 students; Y = 1800 students		
Qn 4	\$30	Qn 5	128 ducks
Qn 6	\$720		

Chapter 8 Volume**Unit 8.1 – Finding Volume of a Cuboid with Given Dimension**

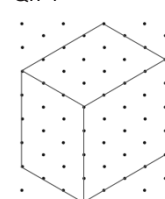
Qn 1	270 cm ³	Qn 2	240 cm ³
Qn 3	7200 cm ³	Qn 4	10 000 cm ³
Qn 5	10 000 cm ³	Qn 6	1728 cm ³
Qn 7	5184 cm ³	Qn 8	5400 cm ³
Qn 9	2000 cm ³	Qn 10	1000 cm ³
Qn 11	250 litres	Qn 12	432 cm ³

Unit 8.2 – Drawing cubes and cuboids on isometric grids

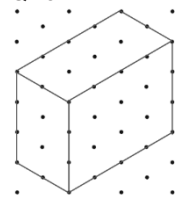
Qn 3



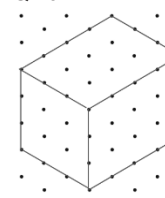
Qn 4



Qn 5



Qn 6

**Unit 8.3 – Finding Dimension with Given Volume**

Qn 1	600 cm ²		
Qn 2	(a) 4.5 cm	(b) 4 cm	
Qn 3	11 cm	Qn 4	20 cm
Qn 5	144 cm ²		

Unit 8.4 – Length, Area and Volume of Cubes

Qn 1	1664 cm ³	Qn 2	2 cm
Qn 3	25 cm ²	Qn 4	729 cm ³
Qn 5	3 cm	Qn 6	216 cm ³
Qn 7	3 cm ³	Qn 8	54 cm ³

Unit 8.5 – Volume and Area of Unit Cubes

Qn 1	12 cm ³	Qn 2	6 cm ³
Qn 3	8 cm ³	Qn 4	7 cm ³
Qn 5	14 cm ³	Qn 6	44 cm ²
Qn 7	54 cm ²	Qn 8	26 cm ²

Unit 8.6 – Volume = Base Area x Height

Qn 1	3 cm	Qn 2	60 cm
Qn 3	30 min	Qn 4	100 cm
Qn 5	60 min	Qn 6	8 cm
Qn 7	(a) 24 litres	(b) 16 cm	
Qn 8	2304 cm ³		

Solutions

Note: In all solutions, U represents Units

Chapter 1 Whole Numbers

Unit 1.1 – More than/Less Than

Qn 1

Box A		12
Box B		

	3 units		
Box A	96	+ 12	+ 96
Box B	- 96		

$$\begin{aligned} 2 \text{ units} &= 96 + 12 + 96 = 204 \\ 1 \text{ unit} &= 204 \div 2 \\ &= 102 \end{aligned}$$

Number of shells in Box A at first = $102 + 96 + 12 = 210$

Qn 2

X		24
Y		

	4 units		
X	42	+ 24	+ 42
Y	1u	- 42	

$$\begin{aligned} 3 \text{ units} &= 42 + 24 + 42 = 108 \\ 1 \text{ unit} &= 108 \div 3 \\ &= 36 \end{aligned}$$

Number of sweets in Container X at first
 $= 36 + 42 + 24$
 $= 102$

Qn 3

	2 units		
Tan	1 unit	15	30
Krishnan	1 unit	15	

$$\begin{aligned} 1 \text{ unit} &= 15 + 30 + 15 \\ &= 60 \end{aligned}$$

Number of muffins Mrs Tan had at first = $1 \text{ unit} + 45$
 $= 60 + 45$
 $= 105$

Qn 4

	1 unit		1 unit	
Jerry		20	40	
Tommy		20	+ 40	+ 20

$$\begin{aligned} 1 \text{ unit} &= \$20 + \$40 + \$20 \\ &= \$80 \\ \text{Jerry at first} &= 1 \text{ unit} + \$60 \\ &= \$80 + \$60 \\ &= \$140 \end{aligned}$$

Qn 5

Elise		24
Fiona		

Elise	1u	- 36	- 24
Fiona		36	60

$$\begin{aligned} 2 \text{ units} &= 36 + 60 = 96 \\ 1 \text{ unit} &= 96 \div 3 \\ &= 32 \end{aligned}$$

Qn 6

A		16
B		

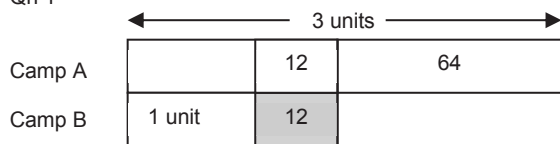
A	1u	- 22	- 16
B		22	38

$$\begin{aligned} 4 \text{ units} &= 22 + 38 = 60 \\ 1 \text{ unit} &= 60 \div 4 = 15 \end{aligned}$$

Number of boys in group A at first = $15 + 38 = 53$

Unit 1.2 – More Than/Less Than (External Unchanged)

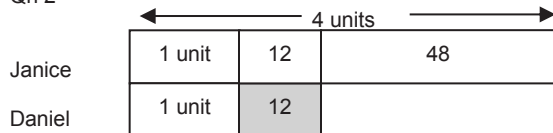
Qn 1



$$\begin{aligned} 2 \text{ units} &= 12 + 64 \\ &= 76 \\ 1 \text{ unit} &= 76 \div 2 \\ &= 38 \end{aligned}$$

$$\begin{aligned} \text{Total number of adults in Campsite A at first} &= 3 \text{ units} \\ &= 3 \times 38 \\ &= 114 \end{aligned}$$

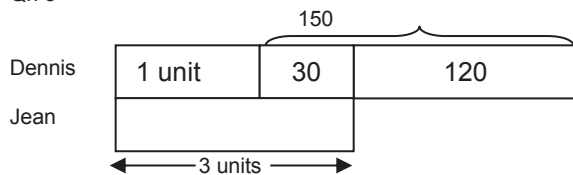
Qn 2



$$\begin{aligned} 3 \text{ units} &= 12 + 48 \\ &= 60 \\ 1 \text{ unit} &= 60 \div 3 \\ &= 20 \end{aligned}$$

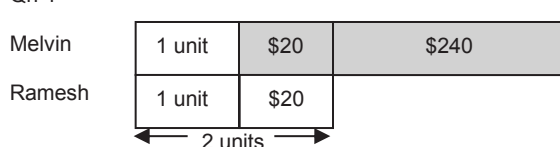
$$\begin{aligned} \text{Number of chocolate Janice had at first} &= 4 \text{ units} \\ &= 4 \times 20 \\ &= 80 \end{aligned}$$

Qn 3



$$\begin{aligned} 2 \text{ units} &= 30 \\ 1 \text{ unit} &= 15 \\ \text{Dennis at first} &= 1 \text{ unit} + 150 \\ &= 15 + 150 \\ &= 165 \end{aligned}$$

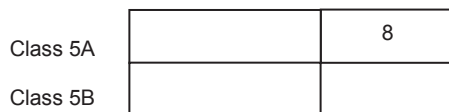
Qn 4



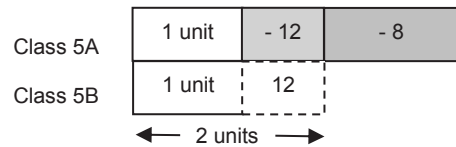
$$1 \text{ unit} = \$20$$

$$\begin{aligned} \text{Amount of money Melvin had at first} &= 1 \text{ unit} + \$260 \\ &= \$20 + \$260 \\ &= \$280 \end{aligned}$$

Qn 5

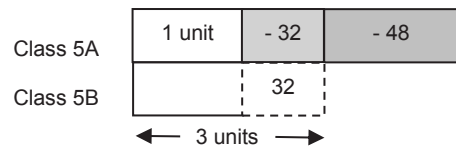
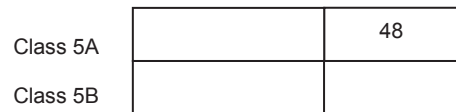


Qn 5 (Cont.)



$$\begin{aligned} \text{Number of pupils in Class 5 A at first} &= 12 + 12 + 8 \\ &= 32 \end{aligned}$$

Qn 6

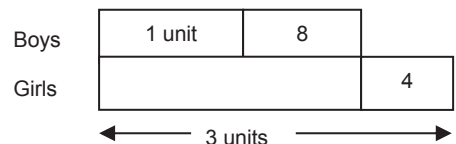


$$\begin{aligned} 2 \text{ units} &= 32 \\ 1 \text{ unit} &= 32 \div 2 \\ &= 16 \end{aligned}$$

$$\begin{aligned} \text{Number of muffins Melissa baked at first} &= 16 + 32 + 48 \\ &= 96 \end{aligned}$$

Unit 1.3 – Equal Stage (Beginning/End)

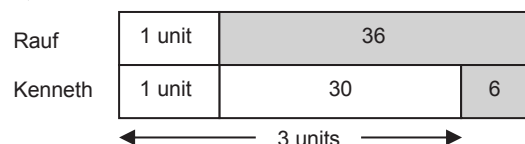
Qn 1



$$\begin{aligned} 2 \text{ units} &= 8 + 4 \\ &= 12 \\ 1 \text{ unit} &= 12 \div 2 \\ &= 6 \end{aligned}$$

$$\begin{aligned} \text{Number of boys at first} &= 1 \text{ unit} + 8 \\ &= 6 + 8 \\ &= 14 \end{aligned}$$

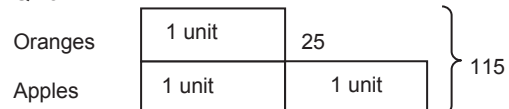
Qn 2



$$\begin{aligned} 2 \text{ units} &= 36 - 6 \\ &= 30 \\ 1 \text{ unit} &= 30 \div 2 \\ &= 15 \end{aligned}$$

$$\begin{aligned} \text{Number of cards each had at first} &= 15 + 36 \\ &= 51 \end{aligned}$$

Qn 3



Qn 3 (Cont.)

$$\begin{aligned} 3 \text{ units} + 25 &= 115 \\ 3 \text{ units} &= 115 - 25 \\ &= 90 \\ 1 \text{ unit} &= 90 \div 3 \\ &= 30 \end{aligned}$$

$$\begin{aligned} \text{Number of oranges at first} &= 1 \text{ unit} + 25 \\ &= 30 + 25 \\ &= 55 \end{aligned}$$

Qn 4

End

Rakesh	1 unit	24	} 216
Xijie	1 unit	24	
		+60	

$$\begin{aligned} 2 \text{ units} + 84 &= 216 \\ 2 \text{ units} &= 132 \\ 1 \text{ unit} &= 132 \div 2 \\ &= 66 \\ \text{Rakesh at first} &= 66 \end{aligned}$$

Qn 5

Raymond	
Kiera	
Raymond	1 unit 18 + 22
Kiera	1 unit - 18

$$\begin{aligned} \text{Total at first} &= 2 \text{ units} + 18 \\ &= 128 \end{aligned}$$

$$\begin{aligned} 2 \text{ units} &= 128 - 40 = 88 \\ 1 \text{ unit} &= 88 \div 2 = 44 \end{aligned}$$

$$\begin{aligned} \text{Number of magnets Raymond had at first} &= 44 + 18 + 22 \\ &= 84 \end{aligned}$$

Qn 6

Apples	
Pears	
Mangoes	

Apples	2 unit	
Pears	1u	
Mangoes	2 unit + 15	- 22

$$\begin{aligned} \text{Total left} &= 5 \text{ units} + 15 = 105 \\ 1 \text{ unit} &= (105 - 15) \div 5 = 18 \end{aligned}$$

$$\begin{aligned} \text{Mangoes at first} &= 18 \times 2 + 15 + 22 = 73 \\ \text{Number of pears sold} &= 73 - 18 = 55 \end{aligned}$$

Unit 1.4 – Constant Difference Between Individuals

Qn 1

Difference in age = 30 years

Mr Tan						
Son		← 30 years →				

$$\begin{aligned} 5 \text{ units} &= 30 \\ 1 \text{ unit} &= 30 \div 5 \\ &= 6 \end{aligned}$$

$$\begin{aligned} \text{Mr Tan's age when son was 6} &= 6 \text{ units} \\ &= 6 \times 6 \\ &= 36 \\ \text{Number of years ago} &= 40 - 36 \\ &= 4 \end{aligned}$$

Qn 2

Now

Ismael			
Son	1 unit	← 24 years →	

$$\begin{aligned} 2 \text{ units} &= 24 \\ 1 \text{ unit} &= 24 \div 2 \\ &= 12 \end{aligned}$$

Some time ago

Ismael				
Son		← 24 yrs →		

$$\begin{aligned} 3 \text{ units} &= 24 \\ 1 \text{ unit} &= 24 \div 3 \\ &= 8 \\ \text{Number of years ago} &= 12 - 8 \\ &= 4 \end{aligned}$$

Qn 3

$$\begin{aligned} \text{Difference at first} &= 180 - 120 \\ &= 60 \end{aligned}$$

End

Girls			
Boys		← 60 →	

$$2 \square = 60 \quad \square = 30$$

$$\begin{aligned} \text{No. of pupils who left midway} &= (120 - 30) \times 2 \\ &= 90 \times 2 \\ &= 180 \end{aligned}$$

Qn 4

Difference between the number of adults and children = 123

End

Adults		← 123 →		
Children				

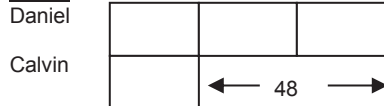
Qn 4 (Cont.)

$$\begin{aligned}\text{Difference } 3 \text{ units} &= 123 \\ 1 \text{ unit} &= 123 \div 3 \\ &= 41 \\ \text{Adults in the end} &= 1 \text{ unit} \\ &= \mathbf{41}\end{aligned}$$

Qn 5
End

$$\begin{aligned}\text{Calvin} &= 48 \\ \text{Daniel} &= 2 \times 48 \\ &= 96 \\ \text{Difference} &= 48\end{aligned}$$

At first



$$2 \text{ } \boxed{} = 48$$

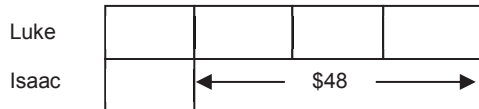
$$\boxed{} = 24$$

$$\begin{aligned}\text{Daniel at first} &= 3 \text{ } \boxed{} \\ &= 3 \times 24 \\ &= \mathbf{72}\end{aligned}$$

Qn 6

$$\begin{aligned}\text{Difference at first} &= \$140 - \$92 \\ &= \$48\end{aligned}$$

In the end



$$\begin{aligned}3 \text{ units} &= \$48 \\ 1 \text{ unit} &= \$48 \div 3 \\ &= \$16\end{aligned}$$

$$\begin{aligned}\text{Amount each of them spent} &= \$92 - \$16 \\ &= \mathbf{\$76}\end{aligned}$$

Unit 1.5 – Number of Units x Value of Units

Qn 1

	Number of vehicles (units)	x	Number of wheels	=	Total value (wheels)
Motorbikes	4	x	2	=	8u
Cars	1	x	4	=	4u
				=	12u

$$\begin{aligned}12 \text{ units} &= 720 \\ 1 \text{ unit} &= 720 \div 12 \\ &= 60\end{aligned}$$

$$\begin{aligned}\text{Total number of cars} &= 1 \text{ unit} \\ &= 1 \times 60 \\ &= \mathbf{60}\end{aligned}$$

Qn 2

	Number of Animals (units)	x	Number of legs	=	Total unit (legs)
Chicken	2	x	2	=	4u
Horses	1	x	4	=	4u
				=	8u

Qn 2 (Cont.)

$$\begin{aligned}8 \text{ units} &= 288 \\ 1 \text{ unit} &= 288 \div 8 \\ &= 36\end{aligned}$$

$$\begin{aligned}\text{Total number of chickens} &= 2 \text{ units} \\ &= 2 \times 36 \\ &= \mathbf{72}\end{aligned}$$

Qn 3

	Number of Items (units)	x	Cost of 1 item (\$)	=	Total unit (\$)
Plates	3	x	12	=	36u
Bowls	1	x	7	=	7u
				=	43u

$$\begin{aligned}43 \text{ units} &= 430 \\ 1 \text{ unit} &= 430 \div 43 \\ &= 10\end{aligned}$$

$$\begin{aligned}\text{(a) Total number of plates bought} &= 3 \text{ units} \\ &= 3 \times 10 \\ &= \mathbf{30 \text{ plates}}\end{aligned}$$

$$\begin{aligned}\text{(b) Difference in the amount of money spent} &= \$29 \text{ units} \\ &= \$29 \times 10 \\ &= \mathbf{\$290}\end{aligned}$$

Qn 4

	No. of students	x	No. of packet drinks/person	=	Total packet
Girls	3 units	x	3	=	9 units
Boys	1 unit	x	5	=	5 unit

$$\begin{aligned}\text{Total amount} &= 5 \text{ units} + 9 \text{ units} \\ &= 14 \text{ units} \\ 14 \text{ units} &= 350 \\ 1 \text{ unit} &= 350 \div 14 \\ &= \mathbf{25}\end{aligned}$$

Qn 5

	Units	x	Value (\$)	=	Total unit (\$)
Adults	4	x	7	=	28u
Children	1	x	4	=	4u
				=	32u

$$\begin{aligned}32 \text{ units} &= 960 \\ 1 \text{ unit} &= 960 \div 32 \\ &= 30\end{aligned}$$

$$\begin{aligned}\text{Number of adults} &= 4 \text{ units} \\ &= 4 \times 30 \\ &= \mathbf{120}\end{aligned}$$

Qn 6

	No.	x	Value	=	Total value
Bolster	1 units	x	\$25	=	25 units
Pillow	3 units	x	\$50	=	150 units
			175 units	=	700
			1 unit	=	4

$$\begin{aligned}\text{(a) No. of pillows} &= 3 \text{ units} \\ &= 3 \times 4 \\ &= \mathbf{12}\end{aligned}$$

$$\begin{aligned}\text{(b) Difference in amount spent} &= 125 \text{ units} \\ &= 125 \times 4 \\ &= \mathbf{\$500}\end{aligned}$$

Unit 1.6 Key Construct: Simultaneous Concept

Qn 1

12 big cubes = 30 small cubes (÷ by 3 throughout)
4 big cubes = 10 small cubes
8 big cubes = 20 small cubes
8 big cubes + 6 small cubes = 20 small cubes + 6 small cubes
= 26 small cubes

Number of extra small cubes container can hold
= 30 small cubes – 26 small cubes
= **4 small cubes**

Qn 2

Container + 15 balls = 1100g
Container + 20 balls = 1350g
Difference = 5 balls = 1350g – 1100g = 250g

1 ball = 250g ÷ 5 = 50g
15 balls = 50g x 15 = 750g

Container = 1100g – 750g = **350g**

Qn 3

3 highlighters + 7 pens = \$13.50

Let cost of 1 pen = 1 unit
1 highlighter = 1 unit + \$0.50
3 highlighters = 3 units + \$1.50

7 pens = 7 units
Total cost = 10 units + \$1.50 = \$13.50
10 units = \$12
1 unit = \$12 ÷ 10
= **\$1.20**

Qn 4

3 files + 2 markers = \$22.50
2 files + 3 markers = \$17.50
(make the markers the same)

Since LCM of 2 and 3 is 6,
9 files + 6 markers = \$22.50 x 3 = \$67.50
4 files + 6 markers = \$17.50 x 2 = \$35

5 files = \$67.50 – \$32(\$35)
= \$32.50

1 file = \$32.50 ÷ 5
= **\$6.50**

Qn 5

Box + 30 balls = 1100g
Box + 25 batteries = 1550g

Let the mass of 1 ball = 1u
Mass of 1 battery = 3u
Mass of 30 balls = 30u
Mass of 25 batteries = 25 x 3u = 75u

Difference = 75u – 30u = 45u
45u = 1550g – 1100g = 450g
1u = 450g ÷ 45 = 10g

Qn 5 (Cont.)

30 balls = 10g x 30 = 300g
Box = 1100g – 300g
= **800g**

Qn 6

4 volleyballs = 3 basketballs
5 volleyballs + 2 basketballs = \$460
(make the number of volleyballs the same)

Since LCM of 4 and 5 is 20,
20 volleyballs = 15 basketballs
20 volleyballs + 8 basketballs = \$460 x 4 = \$1840
15 basketballs + 8 basketballs = \$1840

23 basketballs = \$1840
1 basketball = \$1840 ÷ 23
= **\$80**

Qn 7

1 rectangular piece of cardboard cut into 4 squares, increase
= 3 pieces

Big increase = 101 – 50 = 51
Small increase = 3

No. of rectangular pieces she bought
= 51 ÷ 3
= **17 pieces**

Unit 1.7 Key Construct: Excess and Shortage

Qn 1

Difference between a highlighter and a pen
= \$0.40 + \$0.20
= \$0.60

Let the cost of 1 pen = \$1 unit

Cost of 1 highlighter = \$1 unit + \$0.60
15 highlighters + 12 pens = 12 units + 15 units + \$0.60 x 15
= 27 units + \$9

27 units + \$9 = \$49.50
27 units = \$49.50 – \$9 = \$40.50
1 unit = \$40.50 ÷ 27 = \$1.50

Amount of money he had at first
= \$49.50 + \$1.50 + \$0.20
= **\$51.20**

Qn 2

Difference between a big pot and a small pot = \$32 + \$16 = \$48

Let the cost of 1 small pot = \$1 unit

Cost of 1 big pot = \$1 unit + \$48

3 big pots + 5 small pots = 3 units + \$48 x 3 + 5 units = 8 units + \$144

8 units + \$144 = \$928
8 units = \$928 – \$144 = \$784
1 unit = \$784 ÷ 8 = \$98

Qn 2 (Cont.)

- (a) Each small pot cost **\$98**
(b) Amount of money Mrs Imran had at first
= \$928 + \$98 + \$32
= **\$1058**

Qn 3

Difference between a big bottle and small bottle =
 $0.2\ell + 0.15\ell = 0.35\ell$

Let the volume of 1 small bottle = 1 unit

Cost of 1 big pot = 1 unit + 0.35ℓ
4 big bottles + 7 small bottles
= 4 units + $4 \times 0.35\ell$ + 7 units = 11 units + 1.4ℓ

11 units + $1.4\ell = 9.1\ell$
11 units = $9.1\ell - 1.4\ell = 7.7\ell$
1 unit = $7.7\ell \div 11 = 0.7\ell$

- (a) **0.35ℓ**
(b) Amount of apple juice at first
= $9.1\ell + 0.7\ell + 0.15\ell = 9.95\ell$

Qn 4

7 necklaces, short of 114 beads
4 necklaces, 36 beads left

3 necklace = 114 beads + 36 beads = 150 beads
1 necklace = 150 beads \div 3 = 50 beads

Total beads Celine had
= $50 \times 4 + 36$
= **236 beads.**

Qn 5

Each child 5 sweets, left 53 sweets
Each child 7 sweets, left 3 sweets.

Each child extra 2 sweets, Jason need $53 - 3 = 50$ sweets

- (a) Number of children = $50 \div 2 = 25$
(b) Number of sweets Jason had
= $25 \times 5 + 53$
= **178 sweets**

Qn 6

Made 48 pies, left 1800g of flour,
Made 23 pies, left 4200g of flour.

25 pies will need $4200\text{g} - 1800\text{g} = 2400\text{g}$

- (a) 1 pie = $2400\text{g} \div 25 = 96\text{g}$
Each pie weighed **96g**
(b) $4200\text{g} + 1800\text{g} = 6000\text{g}$

Number of additional pies
= $6000\text{g} \div 96\text{g}$
= 62.5 pies \approx 62 pies.

Qn 7

Difference between a pen and a pencil = $\$1.40 - \$0.80 = \$0.60$

Let the cost of a pencil be \$1 unit

Cost of 1 pen = $\$1\text{u} + \0.60

Since 3 pens = 4 pencils
 $\$3\text{u} + \$0.60 \times 3 = 4$ units
1 unit = \$1.80
3 pens + 4 pencils = 7 units + \$1.80
= $7 \times \$1.80 + \$1.80 = \$14.40$

Amount of money Daniel had = $\$14.40 + \1.40
= **\$15.80**

Unit 1.8 Key Construct: Gap and Differences

Qn 1

3 small key chains for \$7
2 large key chains for \$11.

Since James made an equal number of small and large key chains,
LCM of 2 and 3 is 6.

6 small key chains = $\$7 \times 2 = \14
6 large key chains = $\$11 \times 3 = \33

Difference between 6 small and 6 large key chains
= $\$33 - \14
= \$19

Number of sets = $\$133 \div \$19 = 7$ sets
Number of key chains he made
= $7 \times (6 + 6)$
= **84**

Qn 2

3 cakes cost \$4
4 muffins cost \$7

Since Auntie Pek bought an equal number of cakes and muffins,
LCM of 3 and 4 is 12.

12 cakes cost $\$4 \times 4 = \16
12 muffins cost $\$7 \times 3 = \21

Difference between 12 cakes and 12 muffins = $\$21 - \$16 = \$5$

Number of sets
= $\$70 \div \5
= 14 sets

Number of cakes she bought
= 12×14
= **168 cakes**

Qn 3

3 key chains cost \$7
4 magnets cost \$11

Qn 3 (Cont.)

Since Jimmy bought an equal number of key chains and magnets,

LCM of 3 and 4 is 12.

12 key chains cost $\$7 \times 4 = \28
 12 magnets cost $\$11 \times 3 = \33

Difference between 12 key chains and 12 magnets
 = $\$33 - \28
 = $\$5$

Number of sets
 = $\$65 \div \5
 = 13 sets

Number of magnets and key chains he bought
 = $13 \times (12 + 12)$
 = **312**

Qn 4

(a) 5 pens cost \$6
 3 pencils cost \$2.40
 Since Celest bought an equal number of pens and pencils,
 LCM of 3 and 5 is 15.

15 pens cost $\$6 \times 3 = \18
 15 pencils cost $\$2.40 \times 5 = \12
 Total cost of 15 pens and 15 pencils
 = $\$18 + \12
 = $\$30$

Number of sets = $\$240 \div \$30 = 8$ sets
 Number of pens she bought
 = 8×15
 = **120**

(b) 5 pens cost \$6
 3 pencils cost \$2.40

Since Brian spent equal amount on the pens and pencils,
 LCM of 2.4 and 6 is 12

$\$12 \div \$6 = 2$ sets
 $\$12$ can buy 2×5 pens = 10 pens

$\$12 \div \$2.40 = 5$ sets
 $\$12$ can also buy $3 \times 5 = 15$ pencils
 Fraction of total items that were pens = $\frac{10}{25} = \frac{2}{5}$

Qn 5

(a) 7 cups cost \$20
 3 plates cost \$14
 Since Mrs Imran bought an equal number of plates and cups,
 LCM of 3 and 7 is 21.

21 cups cost $\$20 \times 3 = \60
 21 plates cost $\$14 \times 7 = \98

Difference between 21 plates and 21 cups
 = $\$98 - \60
 = $\$38$

Number of sets = $\$190 \div \$38 = 5$
 Number of cups she bought = $21 \times 5 = \mathbf{105}$

Qn 5 (Cont.)

(b) 7 cups cost \$20
 3 plates cost \$14

Since Mrs Gomez spent an equal amount on the plates and cups,
 LCM of 14 and 20 is 140.

$\$140 \div \$20 = 7$ sets
 $\$140$ can buy $7 \times 7 = 49$ cups

$\$140 \div \$14 = 10$ sets
 $\$140$ can buy $3 \times 10 = 30$ plates

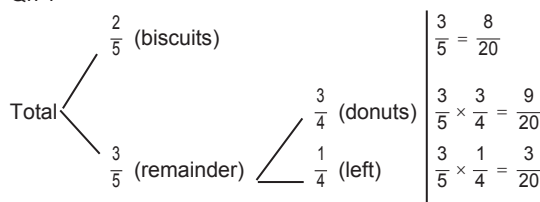
Difference = $49 - 30 = 19$ items
 Number of sets = $190 \div 19 = 10$

Amount of money she spent on the cups
 = $10 \times \$140$
 = **\$1400**

Chapter 2 Fractions

Unit 2.1 – Part-whole Relationship (Type 1)

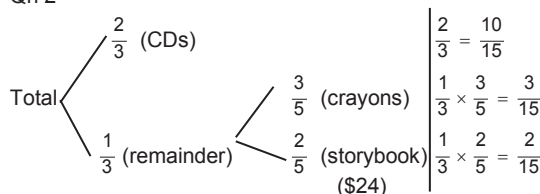
Qn 1



(a) Fraction of money spent on donuts = $\frac{9}{20}$

(b) $\frac{3}{20}$ of total = \$9
 $\frac{1}{20}$ of total = $\$9 \div 3$
 = \$3
 Total = 20×3
 = **\$60**

Qn 2

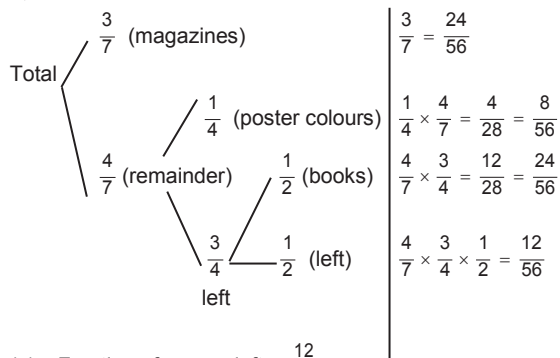


(a) $\frac{2}{15}$ of her money was spent on the storybook

(b) $\frac{2}{15}$ of total = \$24
 $\frac{1}{15}$ of total = $\$24 \div 2$
 = \$12

Total = $15 \times \$12$
 = **\$180**

Qn 3



(a) Fraction of money left = $\frac{12}{56}$
 $= \frac{3}{14}$

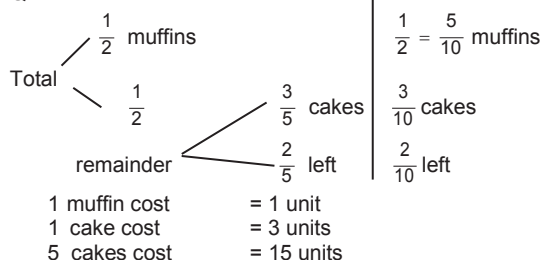
(b) Difference = $\frac{12}{56}$ of total - $\frac{8}{56}$ of total
 $= \frac{4}{56}$ of total

$\frac{4}{56}$ of total = \$16

$\frac{1}{56}$ of total = $\$16 \div 4$
 $= \$4$

Total = $56 \times \$4$
 $= \$224$

Qn 4

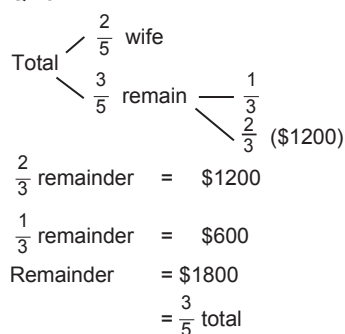


$\frac{3}{10}$ total = 15 units

$\frac{1}{10}$ total = 5 units

$\frac{5}{10}$ total = 25 units
 $= 25$

Qn 5

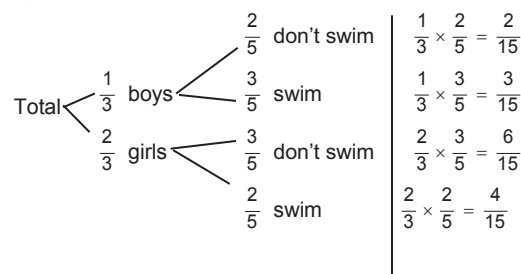


Qn 5 (Cont.)

$\frac{1}{5}$ total = $\$1800 \div 3$
 $= \$600$

Total = $\$600 \times 5$
 $= \$3000$

Qn 6



Total swimmers, $\frac{3}{15} + \frac{4}{15} \rightarrow 490$

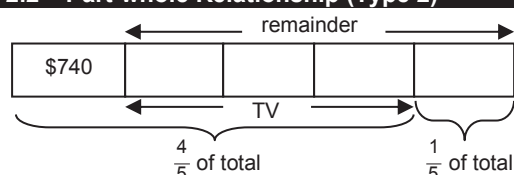
$\frac{7}{15}$ total = 490

$\frac{1}{15}$ total = 70

Total = 70×15
 $= 1050$

Unit 2.2 – Part-whole Relationship (Type 2)

Qn 1

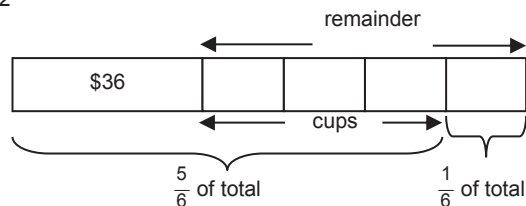


Since $\frac{1}{5}$ of total = 1 unit, $\frac{4}{5}$ of total = 4 units

$\$740 = 1 \text{ unit} \rightarrow \frac{1}{5}$ of total

Salary = $\$740 \times 5$
 $= \$3700$

Qn 2



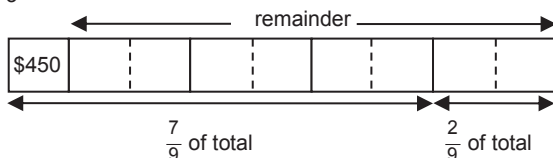
Since $\frac{1}{6}$ of total = 1 unit, $\frac{5}{6}$ of total = 5 units

$\frac{2}{6}$ of total = \$36

$\frac{1}{6}$ of total = $\$36 \div 2$
 $= \$18$

Total = $\$18 \times 6$
 $= \$108$

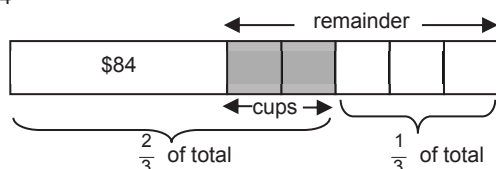
Qn 3



$$\frac{1}{9} \text{ of total} = \$450$$

$$\begin{aligned} \text{Total} &= \$450 \times 9 \\ &= \mathbf{\$4050} \end{aligned}$$

Qn 4



$$\frac{1}{3} \text{ of total} = 3 \text{ units}$$

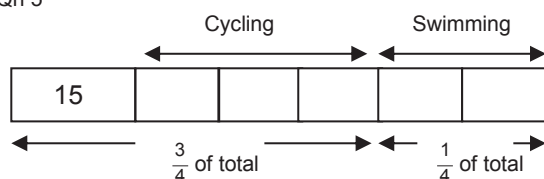
$$\frac{2}{3} \text{ of total} = 6 \text{ units}$$

$$4 \text{ units} = \$84$$

$$\begin{aligned} 1 \text{ unit} &= \$84 \div 4 \\ &= \$21 \end{aligned}$$

$$\begin{aligned} \text{At first} &= 9 \text{ units} \\ &= 9 \times \$21 \\ &= \mathbf{\$189} \end{aligned}$$

Qn 5



$$\text{Since } \frac{1}{4} \text{ total} = 2 \text{ } \boxed{}$$

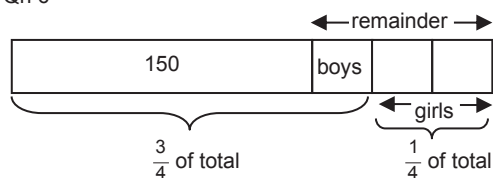
$$\frac{3}{4} \text{ total} = 6 \text{ } \boxed{}$$

$$3 \text{ } \boxed{} = 15$$

$$\boxed{} = 5$$

$$\begin{aligned} \text{Total } 8 \text{ } \boxed{} &= 8 \times 5 \\ &= \mathbf{40} \end{aligned}$$

Qn 6



Qn 6 (Cont.)

$$\text{Since } \frac{1}{4} \text{ of total} = 2 \text{ units, } \frac{3}{4} \text{ of total} = 6 \text{ units}$$

$$5 \text{ units} = 150$$

$$1 \text{ unit} = 150 \div 5 = 30$$

$$\begin{aligned} \text{Total} &= 8 \text{ units} \\ &= 8 \times 30 \\ &= \mathbf{240} \end{aligned}$$

There were **240** participants.

Unit 2.3 – Part-whole Relationship (Type 3)

Qn 1

$$\begin{aligned} \text{Total} &= \frac{1}{5} \text{ of total} + \$4 \text{ (game cartridge)} \\ &= \frac{4}{5} \text{ of total} - \$4 \text{ (remainder)} \\ &= \frac{1}{3} \text{ remainder} + \$8 \text{ (comics)} \\ &= \frac{2}{3} \text{ remainder} - \$8 = \$24 \end{aligned}$$

$$\begin{aligned} \frac{2}{3} \text{ of remainder} &= \$8 + \$24 \\ &= \$32 \end{aligned}$$

$$\frac{1}{3} \text{ of remainder} = \$16$$

$$\begin{aligned} \text{Remainder} &= \$16 \times 3 \\ &= \$48 \end{aligned}$$

$$\frac{4}{5} \text{ of total} - \$4 = \$48$$

$$\frac{4}{5} \text{ of total} = \$52$$

$$\begin{aligned} \frac{1}{5} \text{ of total} &= \$52 \div 4 \\ &= \$13 \end{aligned}$$

$$\begin{aligned} \text{Total} &= \$13 \times 5 \\ &= \mathbf{\$65} \end{aligned}$$

Qn 2

$$\begin{aligned} \text{Total} &= \frac{1}{4} \text{ of total} + \$40 \text{ (present)} \\ &= \frac{3}{4} \text{ of total} - \$40 \text{ (remainder)} \\ &= \frac{2}{5} \text{ of remainder} + \$45 \text{ (resource books)} \\ &= \frac{3}{5} \text{ of remainder} - \$45 \rightarrow \$75 \end{aligned}$$

$$\frac{3}{5} \text{ of remainder} = \$75 + \$45 \rightarrow \$120$$

$$\frac{1}{5} \text{ of remainder} = \$120 \div 3 \rightarrow \$40$$

$$\text{Remainder} = 5 \text{ units} \rightarrow 5 \times \$40 \rightarrow \$200$$

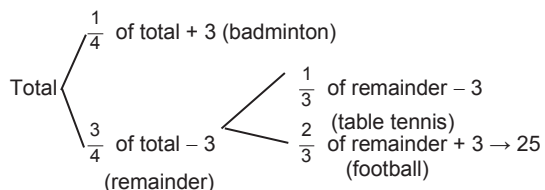
$$\frac{3}{4} \text{ of total} - \$40 = \$200$$

$$\frac{3}{4} \text{ of total} = \$240$$

$$\begin{aligned} \frac{1}{4} \text{ of total} &= \$240 \div 3 \\ &= \$80 \end{aligned}$$

$$\begin{aligned} \text{Total} &= \$80 \times 4 \\ &= \mathbf{\$320} \end{aligned}$$

Qn 3



$$\frac{2}{3} \text{ of remainder} = 25 - 3$$

$$= 22$$

$$\frac{1}{3} \text{ of remainder} = 22 \div 2$$

$$= 11$$

$$\text{Remainder} = 3 \text{ units}$$

$$= 3 \times 11$$

$$= 33$$

$$\frac{3}{4} \text{ of total} - 3 = 33$$

$$\frac{3}{4} \text{ of total} = 36$$

$$\frac{1}{4} \text{ of total} = 36 \div 3$$

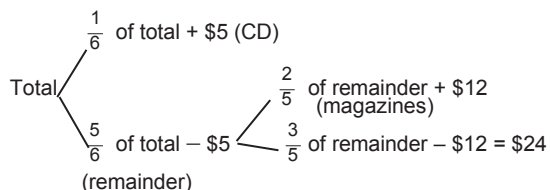
$$= 12$$

$$\text{Total} = 4 \text{ units}$$

$$= 4 \times 12$$

$$= 48$$

Qn 4



$$\frac{3}{5} \text{ of remainder} = \$24 + \$12$$

$$= \$36$$

$$\frac{1}{5} \text{ of remainder} = \$36 \div 3$$

$$= \$12$$

$$\text{Remainder} = 5 \text{ units}$$

$$= 5 \times \$12$$

$$= \$60$$

$$\frac{5}{6} \text{ of total} - \$5 = \$60$$

$$\frac{5}{6} \text{ of total} = \$65$$

$$\frac{1}{6} \text{ of total} = \$65 \div 5$$

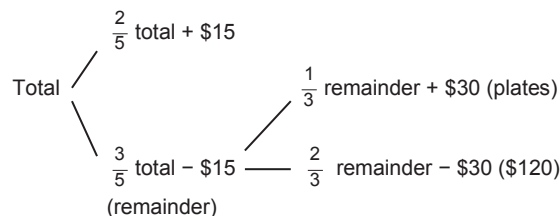
$$= \$13$$

$$\text{Total} = 6 \text{ units}$$

$$= 6 \times \$13$$

$$= \$78$$

Qn 5



$$\frac{2}{3} \text{ remainder} = \$120 + \$30$$

$$= \$150$$

$$\frac{1}{3} \text{ remainder} = \$75$$

$$\text{Remainder} = 75 \times 3$$

$$= \$225$$

$$\frac{3}{5} \text{ total} - \$15 = \$225$$

$$\frac{3}{5} \text{ total} = \$225 + 15$$

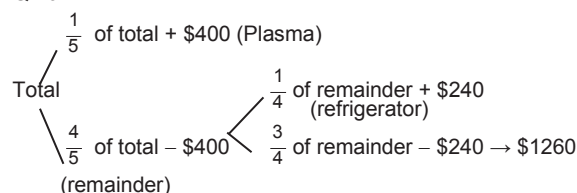
$$= \$240$$

$$\frac{1}{5} \text{ total} = \$80$$

$$\text{Total} = \$80 \times 5$$

$$= \$400$$

Qn 6



$$\frac{3}{4} \text{ remainder} = \$1260 + \$240$$

$$= \$1500$$

$$\frac{1}{4} \text{ remainder} = \$1500 \div 3$$

$$= \$500$$

$$\text{Remainder} = 4 \text{ units}$$

$$= 4 \times \$500$$

$$= \$2000$$

$$\frac{4}{5} \text{ total} - \$400 = \$2000$$

$$\frac{4}{5} \text{ total} = \$2400$$

$$\frac{1}{5} \text{ total} = \$2400 \div 4$$

$$= \$600$$

$$\text{Total} = 5 \times \$600$$

$$= \$3000$$

Unit 2.4 – Equal Fractions

Qn 1

$$\frac{3}{4} \text{ of Chelsia's money} = \frac{5}{6} \text{ of Brian's money}$$

$$\frac{15}{20} \text{ of Chelsia's money} = \frac{15}{18} \text{ of Brian's money}$$

$$\text{Chelsia's money} = 20 \text{ units}$$

$$\text{Brian's money} = 18 \text{ units}$$

Qn 1 (Cont.)

$$\begin{aligned}\text{Difference} &= 20 \text{ units} - 18 \text{ units} \\ &= 2 \text{ units}\end{aligned}$$

$$\begin{aligned}2 \text{ units} &= \$24 \\ 1 \text{ unit} &= \$24 \div 2 \\ &= \$12\end{aligned}$$

$$\begin{aligned}\text{Total of Chelsia's and Brian's money} &= 38 \text{ units} \\ &= 38 \times \$12 \\ &= \mathbf{\$456}\end{aligned}$$

Qn 2

Amount Left

$$\frac{3}{4} \text{ of Ema's money} = \frac{3}{7} \text{ of Keng Wee's money}$$

$$\begin{aligned}\text{Ema's money} &= 4 \text{ units} \\ \text{Keng Wee's money} &= 7 \text{ units}\end{aligned}$$

$$\begin{aligned}\text{Difference} &= 7 \text{ units} - 4 \text{ units} \\ &= 3 \text{ units} \\ 3 \text{ units} &= \$360 \\ 1 \text{ unit} &= \$360 \div 3 \\ &= \$120\end{aligned}$$

$$\begin{aligned}\text{Keng Wee's money} &= 7 \text{ units} \\ &= 7 \times \$120 \\ &= \mathbf{\$840}\end{aligned}$$

Qn 3

$$\frac{3}{5} \text{ Boys} = \frac{4}{7} \text{ Girls}$$

$$\frac{12}{20} \text{ Boys} = \frac{12}{21} \text{ Girls}$$

$$\begin{aligned}\text{Boys} &= 20 \text{ units} \\ \text{Girls} &= 21 \text{ units} \\ \text{Difference} &= 1 \text{ unit} \\ &= 65\end{aligned}$$

$$\begin{aligned}\text{Total no. of students in the end} &= 24 \times 65 \\ &= \mathbf{1560}\end{aligned}$$

Qn 4

Left amount

$$\text{Rasidah} = \frac{2}{5} \quad \text{Chai Seng} = \frac{1}{7}$$

$$\frac{1}{7} \text{ Chai Seng} = \frac{1}{2} \text{ of what Rasidah left}$$

$$\frac{1}{7} \text{ Chai Seng} = \frac{1}{2} \times \frac{2}{5} \text{ Rasidah}$$

$$\frac{1}{7} \text{ Chai Seng} = \frac{1}{5} \text{ Rasidah}$$

$$\begin{aligned}\text{Chai Seng} &= 7 \text{ units} \\ \text{Rasidah} &= 5 \text{ units} \\ \text{Difference} &= 2 \text{ units}\end{aligned}$$

$$\begin{aligned}2 \text{ units} &= \$48 \\ 1 \text{ unit} &= \$24\end{aligned}$$

$$\begin{aligned}\text{Total (Raidah) at first} &= 5 \text{ units} \\ &= 5 \times \$24 \\ &= \mathbf{\$120}\end{aligned}$$

Qn 5

Number of cookies Left

$$\text{Chocolate} = \frac{1}{4} \quad \text{Vanilla} = \frac{1}{6}$$

$$\frac{1}{4} \text{ of Chocolate} = \text{Twice of the vanilla cookies left}$$

$$\frac{1}{4} \text{ of Chocolate} = 2 \times \frac{1}{6} \text{ of Vanilla}$$

$$\frac{1}{4} \text{ of Chocolate} = \frac{1}{3} \text{ of Vanilla}$$

$$\begin{aligned}\text{Chocolate} &= 4 \text{ units} \\ \text{Vanilla} &= 3 \text{ units} \\ \text{Total} &= 4 \text{ units} + 3 \text{ units} \\ &= 7 \text{ units}\end{aligned}$$

$$\begin{aligned}7 \text{ units} &= 280 \\ 1 \text{ unit} &= 280 \div 7 \\ &= 40\end{aligned}$$

$$\begin{aligned}\text{Number of chocolate cookies given away} &= 3 \text{ units} \\ &= 3 \times 40 \\ &= \mathbf{120}\end{aligned}$$

Qn 6

Left

$$\text{Roy} = \frac{1}{3} \quad \text{Dennis} = \frac{3}{4}$$

$$\frac{3}{4} \text{ Dennis} = \text{Twice} \times \frac{1}{3} \text{ Roy}$$

$$\frac{3}{4} \text{ Dennis} = \frac{2}{3} \text{ Roy}$$

$$\frac{6}{8} \text{ Dennis} = \frac{6}{9} \text{ Roy}$$

$$\begin{aligned}\text{Dennis} &= 8 \text{ units} \\ \text{Roy} &= 9 \text{ units}\end{aligned}$$

$$\begin{aligned}\text{Total, 17 units} &= \$340 \\ 1 \text{ unit} &= \$20\end{aligned}$$

$$\begin{aligned}\text{Dennis in the end} &= 6 \text{ units} \\ &= 6 \times \$20 \\ &= \mathbf{\$120}\end{aligned}$$

Unit 2.5 – Repeated Identity

Qn 1

Banana	1 unit	$\times 3 = 3 \text{ units}$	}	Banana	= 3 units
Chocolates	5 units	$\times 3 = 15 \text{ units}$		Chocolates	= 15 units
Banana	3 units			Blueberry	= 1 unit
Blueberry	1 unit				
Total	= 3 units + 15 units + 1 unit				
	= 19 units				

$$\begin{aligned}19 \text{ units} &= 76 \\ 1 \text{ unit} &= 76 \div 19 \\ &= 4\end{aligned}$$

$$\begin{aligned}\text{Number of banana muffins} &= 3 \text{ units} \\ &= 3 \times 4 \\ &= \mathbf{12}\end{aligned}$$

Qn 2

Siti	2 unit	$\times 4 = 8$ units	}	Siti = 8 units Joel = 28 units Melvin = 21 units
Joel	7 units	$\times 4 = 28$ units		
Melvin	3 units	$\times 7 = 21$ units		
Joel	4 unit	$\times 7 = 28$ units		

Difference between Melvin and Siti = 21 units – 8 units
= 13 units

13 units = 39
1 unit = 3

Total number of sweets shared at first = 57 units
= 57×3
= **171**

Qn 3

Group A	3 unit	$\times 5 = 15$ units	}	Group A = 15 units Group B = 20 units Group C = 8 units
Group B	4 units	$\times 5 = 20$ units		
Group C	2 units	$\times 4 = 8$ units		
Group B	5 unit	$\times 4 = 20$ units		

Difference between Group A and Group C
= 15 units – 8 units
= 7 units

7 units = 49
1 unit = $49 \div 7$
= 7

Total number of students in the three groups
= 15 units + 20 units + 8 units
= 43 units
= 43×7
= **301**

Qn 4

Boys = 1 unit
Girls = 5 units
Children = 6 units

Adults = $\frac{2}{3} \times 6$ units = 4 units

Difference between adults and boys
= 4 units – 1 unit
= 3 units

3 units = 120
1 unit = $120 \div 3 = 40$

Total = $40 \times 10 = \mathbf{400}$

Qn 5

Total Square = 5 units			
Unshaded square	4 units	}	Unshaded Square = 4 units Shaded Area = 1 unit Unshaded Rectangle = 14 units
Shaded square	1 unit		
Square	1 units $\times 5 = 5$ units		
Rectangle	3 unit $\times 5 = 15$ units		

Fraction unshaded $\rightarrow \frac{14 \text{ units} + 4 \text{ units}}{14 \text{ units} + 4 \text{ units} + 1 \text{ unit}} = \frac{18}{19}$

Qn 6

Square = 2 units
Rectangle = 5 units

Shaded area = $\frac{3}{4} \times 2$ units = 1.5 units

Unshaded part of square = 2 units – 1.5 units = 0.5 units

Unshaded part of rectangle = 5 units – 1.5 units = 3.5 units

Total unshaded parts = 4 units = 72cm^2

1 unit = $72\text{cm}^2 \div 4 = 18\text{cm}^2$

Area of square = $2 \times 18\text{cm}^2$
= **36cm^2**

Unit 2.6 – External Unchanged

Qn 1

Orange 1 unit $\times 2 = 2$ units
Water 3 units $\times 2 = 6$ units

Orange 2 units
Water 7 units

Increase in water = 1 unit
= 300 mℓ

Amount of syrup used = 2 units
= 2×300 mℓ
= **600 mℓ**

Qn 2

Before

Children : 3 units $\times 2 = 6$ units
Adults : 5 units $\times 2 = 10$ units

After

Children : 2 units $\times 3 = 6$ units
Adults : 3 units $\times 3 = 9$ units

Decrease in adults = 1 unit
= 125

Number of children = 6 units
= 6×125
= **750**

Qn 3

Boys : 2 units $\times 3 = 6$ units
Girls : 3 units $\times 3 = 9$ units

Boys : 3 units $\times 2 = 6$ units
Girls : 5 units $\times 2 = 10$ units

Increase in girls
= 4

No. of students in the end
= 16×4
= **64**

Qn 4

Before

Pear : 1 unit $\times 4 = 4$ units
Kiwi : 2 units $\times 4 = 8$ units

If given away

Pear : 4 units
Kiwi : 5 units

Qn 4 (Cont.)

Decrease in number of Kiwi fruit = 8 units – 5 units
= 3 units

3 units = 12

1 unit = $12 \div 3$
= 4

Total number of fruits = 12 units
= 12×4
= **48**

Qn 5

At first

Team A 6 units $\times 7 = 42$ units

Team B 7 units $\times 7 = 49$ units

End

Team A 7 units $\times 6 = 42$ units

Team B 8 units $\times 6 = 48$ units



Difference in members in Team B = 2 (1 unit)

Number of members in Team A = 42 units
= 42×2
= **84**

Qn 6

At first

Syrup = 1 unit $\times 2 = 2$ units

Water = 2 units $\times 2 = 4$ units

End

Syrup = 2 units

Water = 5 units

Since the amount of syrup is the same, make the units that represent the syrup the same.

Increase in water = 5 units – 4 units = 1 unit

1 unit = 200 ml

Water at first = 200 ml $\times 4 =$ **800 ml**

Unit 2.7 – Unchanged Total

Qn 1

At first

Boys 2 units $\times 4 = 8$ units

Girls 5 units $\times 4 =$ 20 units
28 units

End

Boys 1 unit $\times 7 = 7$ units

Girls 3 units $\times 7 =$ 21 units
28 units

Number of students transferred = 3

Total number of students at first = 28×3
= **84**

Qn 2

At first

Teck Seng 3 units $\times 4 = 12$ units

Wilson 4 units $\times 4 =$ 16 units
28 units

End

Teck Seng 1 unit $\times 7 = 7$ units

Wilson 3 units $\times 7 =$ 21 units
28 units

Total number of stickers = 28 units

28 units = 140

1 unit = $140 \div 28$
= 5

Qn 2 (Cont.)

Number of stickers transferred = 12 units – 7 units
= 5 units
= 5×5
= **25**

Qn 3

After 3 days

Fixed 1 unit $\times 5 = 5$ units

Unfixed 3 units $\times 5 = 15$ units

After 1 week

Fixed 2 units $\times 4 = 8$ units

Unfixed 3 units $\times 4 = 12$ units

Transfer 3 units = 30

1 unit = $30 \div 3$
= 10

Total pieces of puzzle = 20 units

= 20×10
= **200**

Qn 4

After 1 hour

Answered 1 unit $\times 5 = 5$ units

Unanswered 1 unit $\times 5 = 5$ units

After 20 minutes

Answered 4 units $\times 2 = 8$ units

Unanswered 1 unit $\times 2 = 2$ units

Transfer 3 units = 18

1 unit = 6

Total questions in quiz = 10 units

= 10×6
= **60**

Qn 5

Terry = 1 unit $\times 7 = 7$ units

Chelsea + Dave = 3 units $\times 7 = 21$ units

Total = 4 units $\times 7 = 28$ units

Chelsea = 2 units $\times 4 = 8$ units

Terry + Dave = 5 units $\times 4 = 20$ units

Total = 7 units $\times 4 = 28$ units

Since the cost of the present remains the same, we find the LCM of 4 and 7, which is 28.

Terry = 7 units

Dave = 20 units – 7 units = 13 units

Difference between Terry and Dave = 13 units – 7 units = 6 units

6 units = \$24

1 unit = $\$24 \div 6 = \4

Cost of present = $28 \times \$4 =$ **\$112**

Qn 6

Benson + Daryl = 3 units $\times 5 = 15$ units

Jean = 1 units $\times 5 = 5$ units

Qn 6 (Cont.)

$$\text{Total} = 4 \text{ units} \times 5 = 20 \text{ units}$$

$$\begin{aligned} \text{Daryl + Jean} &= 3 \text{ units} \times 4 = 12 \text{ units} \\ \text{Benson} &= 2 \text{ units} \times 4 = 8 \text{ units} \end{aligned}$$

$$\text{Total} = 5 \text{ units} \times 4 = 20 \text{ units}$$

Since the sum of money remains the same, we find the LCM of 4 and 5, which is 20.

$$\begin{aligned} \text{Jean} &= 5 \text{ units} \\ \text{Benson} &= 8 \text{ units} \end{aligned}$$

$$\begin{aligned} \text{Difference between Benson and Jean} &= 8 \text{ units} - 5 \text{ units} = 3 \text{ units} \\ 3 \text{ units} &= \$36 \end{aligned}$$

$$\begin{aligned} 1 \text{ unit} &= \$36 \div 3 = \$12 \\ \text{Sum of money} &= 20 \times \$12 = \mathbf{\$360} \end{aligned}$$

Unit 2.8 – Constant Difference

Qn 1

At first

$$\begin{aligned} \text{Boys} & 1 \text{ unit} \times 3 = 3 \text{ units} \\ \text{Girls} & \underline{2 \text{ units}} \times 3 = \underline{6 \text{ units}} \\ \text{Difference} & 1 \text{ unit} \times 3 = 3 \text{ units} \end{aligned}$$

End

$$\begin{aligned} \text{Boys} & 2 \text{ units} \\ \text{Girls} & \underline{5 \text{ units}} \\ \text{Difference} & 3 \text{ units} \end{aligned}$$

$$\begin{aligned} \text{Decrease} & 1 \text{ unit} = 3 \\ \text{Total number of children in the end} & = 7 \text{ units} \\ & = 7 \times 3 \\ & = \mathbf{21} \end{aligned}$$

Qn 2

Present

$$\begin{aligned} \text{John} & 1 \text{ unit} \times 2 = 2 \text{ units} \\ \text{Sister} & \underline{4 \text{ units}} \times 2 = \underline{8 \text{ units}} \\ \text{Difference} & 3 \text{ units} \times 2 = 6 \text{ units} \end{aligned}$$

$$\begin{aligned} \text{John} & 3 \text{ units} \times 3 = 9 \text{ units} \\ \text{Sister} & \underline{5 \text{ units}} \times 3 = \underline{15 \text{ units}} \\ \text{Difference} & 2 \text{ units} \times 3 = 6 \text{ units} \end{aligned}$$

$$\begin{aligned} \text{Increase each} & 7 \text{ units} = 14 \\ & 1 \text{ unit} = 14 \div 7 \\ & = 2 \end{aligned}$$

$$\begin{aligned} \text{John's age now} & = 2 \text{ units} \\ & = 2 \times 2 \\ & = \mathbf{4} \end{aligned}$$

Qn 3

Present

$$\begin{aligned} \text{Mira} & = 8 \text{ years old} \\ \text{Father} & = \underline{44 \text{ years old}} \\ \text{Difference} & = 36 \text{ years old} \end{aligned}$$

Future

$$\begin{aligned} \text{Mira} & = 1 \text{ unit} \\ \text{Father} & = \underline{3 \text{ units}} \\ \text{Difference} & = 2 \text{ units} \end{aligned}$$

$$2 \text{ units} = 36$$

Qn 3 (Cont.)

$$\begin{aligned} 1 \text{ unit} & = 36 \div 2 \\ & = 18 \text{ (Mira's age in the future)} \\ \text{Number of years} & = 18 - 8 \\ & = 10 \end{aligned}$$

$$\text{Mira will be } \frac{1}{3} \text{ as old as her father in } \mathbf{10 \text{ years' time.}}$$

Qn 4

At first

$$\begin{aligned} \text{Jenny} & 1 \text{ unit} \times 2 = 2 \text{ units} \\ \text{Daryl} & 2 \text{ units} \times 2 = 4 \text{ units} \\ \text{Difference} & 1 \text{ unit} \times 2 \end{aligned}$$

End

$$\begin{aligned} \text{Jenny} & = 1 \text{ unit} \\ \text{Daryl} & = 3 \text{ units} \\ \text{Difference} & = 2 \text{ units} \end{aligned}$$

$$\begin{aligned} \text{Decrease each} & 1 \text{ unit} = 12 \\ \text{Jenny in the end} & 1 \text{ unit} = \mathbf{12} \end{aligned}$$

Qn 5

At first

$$\begin{aligned} \text{Shop A} & = 68 \text{ kg} \\ \text{Shop B} & = 128 \text{ kg} \\ \text{Difference} & = 60 \text{ kg} \end{aligned}$$

End

$$\begin{aligned} \text{Shop A} & = 2 \text{ units} \\ \text{Shop B} & = 5 \text{ units} \\ \text{Difference} & = 3 \text{ units} \end{aligned}$$

$$\begin{aligned} 3 \text{ units} & = 60 \text{ kg} \\ 1 \text{ unit} & = 20 \text{ kg} \end{aligned}$$

$$\begin{aligned} \text{Shop A (end)} & = 2 \text{ units} \\ & = 40 \text{ kg} \\ \text{Shop A (sold)} & = 68 \text{ kg} - 40 \text{ kg} \\ & = 28 \text{ kg} \\ \text{Total sold} & = 28 \text{ kg} \times 2 \\ & = \mathbf{56 \text{ kg}} \end{aligned}$$

Qn 6

$$\begin{aligned} \text{Square} & 2 \text{ unit} \times 4 = 8 \text{ units} \\ \text{Rectangle} & 5 \text{ units} \times 4 = 20 \text{ units} \\ \text{Difference} & 3 \text{ units} \times 4 \end{aligned}$$

$$\begin{aligned} \text{Unshaded square} & 1 \text{ unit} \times 3 = 3 \text{ units} \\ \text{Unshaded rect} & 5 \text{ units} \times 3 = 15 \text{ units} \\ \text{Difference} & 4 \text{ units} \times 3 \end{aligned}$$

$$\begin{aligned} \text{Decrease each} & 5 \text{ units} = 40 \text{ cm}^2 \\ & 1 \text{ unit} = 8 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Total area of figure} & = 3 \text{ units} + 15 \text{ units} + 5 \text{ units} \\ & = 23 \text{ units} \\ & = 23 \times 8 \text{ cm}^2 \\ & = \mathbf{184 \text{ cm}^2} \end{aligned}$$

Unit 2.9 – Number of Units x Value of Units

Qn 1	Number of units	x	Value	=	Total unit (stickers)
Boys	2	x	4	=	8
Girls	1	x	5	=	<u>5</u>
					13 units

$$13 \text{ units} = 1105$$

Qn 1 (Cont.)

$$1 \text{ unit} = 1105 \div 13$$

$$= 85$$

$$\text{Total number of girls} \quad 1 \text{ unit} = 1 \times 85$$

$$= 85$$

Qn 2

Red = 1 unit $\times 2 = 2$ units (since red is repeated)

Yellow = 3 units $\times 2 = 6$ units

Red = 2 units

Green = 5 units

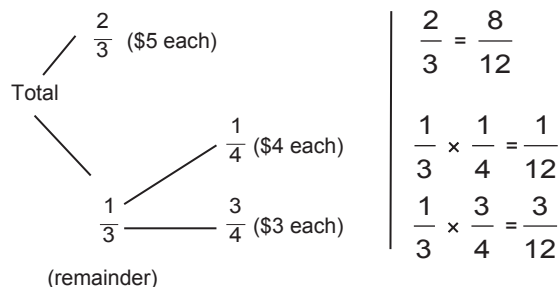
	Number	x	Value	= Total weight
Red	2 units	x	10g	= 20 units grams
Yellow	6 units	x	15g	= 90 units grams
Green	5 units	x	20g	= 100 units grams

$$\text{Total} = 210 \text{ units} = 3150$$

$$1 \text{ unit} = 3150 \div 210 = 15$$

$$\text{Green marbles} = 5 \times 15 = 75$$

Qn 3



No. (units)	x	Value (\$)	=	Total unit (\$)
8 units	x	5	=	40 units
1 units	x	4	=	4 units
3 units	x	3	=	9 units
				<u>53 units</u>

$$53 \text{ units} = 318$$

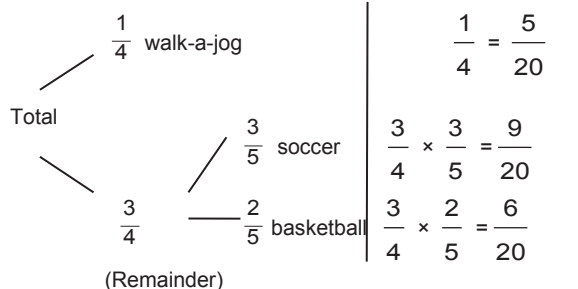
$$1 \text{ unit} = 318 \div 53$$

$$= 6$$

$$\text{Total number of people} = 12 \times 6$$

$$= 72$$

Qn 4



No. units	x	value(points)	=	Total (unit points)
Walk-a-jog	5 units	x 6	=	30 units
Soccer	9 units	x 5	=	45 units
Basketball	6 units	x 4	=	24 units
				<u>99 units</u>

$$99 \text{ units} = 4950$$

$$1 \text{ unit} = 50$$

Qn 4 (Cont.)

$$\text{Total students} = 20 \text{ units}$$

$$= 20 \times 50$$

$$= 1000$$

Qn 5

$$\frac{1}{3} 20 \text{ ct} = \frac{2}{3} 50 \text{ ct}$$

$$\frac{2}{6} 20 \text{ ct} = \frac{2}{3} 50 \text{ ct}$$

20 ct : 6 units

50 ct: 3 units

\$1: 3 units

No. units	x	value (¢)	=	Total amount (unit ¢)
6 units	x	20	=	120 units
3 units	x	50	=	150 units
5	x	100	=	<u>500 units</u>
				770 units

$$770 \text{ units} = 2310$$

$$1 \text{ unit} = 3$$

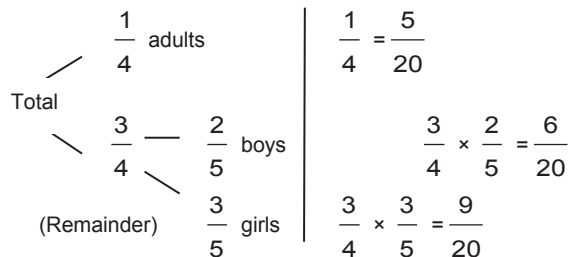
$$\text{Total coins} = 6 \text{ units} + 3 \text{ units} + 5 \text{ units}$$

$$= 14 \text{ units}$$

$$= 14 \times 3$$

$$= 42$$

Qn 6



No.	x	value	=	Total coupons
Adults	5 units	x 5 coupons	=	25 units
Boys	6 units	x 4 coupons	=	24 units
Girls	9 units	x 3 coupons	=	<u>27 units</u>
Total				76 units

$$76 \text{ units} = 1520$$

$$1 \text{ unit} = 20$$

$$\text{Total adults} = 5 \text{ units} = 5 \times 20$$

$$= 100$$

Unit 2.10 – Key Construct: Fraction As An Object

Qn 1

$$\text{Remaining orange juice} = 3\frac{1}{3} \ell - 1\frac{1}{2} \ell$$

$$= \frac{10}{3} \ell - \frac{3}{2} \ell$$

$$= \frac{20}{6} \ell - \frac{9}{6} \ell$$

$$= \frac{11}{6} \ell$$

$$\text{Amount of orange juice in 1 cup} = \frac{1}{2} \times \frac{11}{6} \ell = \frac{11}{12} \ell$$

Qn 2

$$\begin{aligned}\text{Milk for smoothie} &= \frac{1}{3} \times 4 \frac{1}{2} \ell = \frac{1}{3} \times \frac{9}{2} \ell \\ &= \frac{3}{2} \ell\end{aligned}$$

$$\begin{aligned}\text{Amount of milk left} &= 4 \frac{1}{2} \ell - 1 \frac{1}{3} \ell - \frac{3}{2} \ell = \frac{9}{2} \ell - \frac{4}{3} \ell - \frac{3}{2} \ell \\ &= \frac{27}{6} \ell - \frac{8}{6} \ell - \frac{9}{6} \ell \\ &= \frac{10}{6} \ell = 1 \frac{4}{6} \ell \\ &= 1 \frac{2}{3} \ell\end{aligned}$$

Qn 3

$$\begin{aligned}\text{Remaining flour} &= \frac{2}{3} \times 2 \frac{1}{6} \text{ kg} = \frac{2}{3} \times \frac{13}{6} \\ &= \frac{13}{9} \text{ kg}\end{aligned}$$

$$\text{Amount of flour left} = \frac{1}{2} \times \frac{13}{9} \text{ kg} = \frac{13}{18} \text{ kg}$$

Qn 4

$$\begin{aligned}\text{Remaining ribbon} &= \frac{3}{4} \times 7 \frac{1}{2} \text{ m} = \frac{3}{4} \times \frac{15}{2} \text{ m} \\ &= \frac{45}{8} \text{ m}\end{aligned}$$

$$\begin{aligned}\text{Amount of ribbon left} &= \frac{1}{3} \times \frac{45}{8} \text{ m} \\ &= \frac{15}{8} \text{ m} = 1 \frac{7}{8} \text{ m}\end{aligned}$$

Qn 5

$$\begin{aligned}\text{Remaining sugar} &= 3 \frac{1}{3} \text{ kg} - \frac{2}{5} \text{ kg} = \frac{10}{3} \text{ kg} - \frac{2}{5} \text{ kg} \\ &= \frac{50}{15} \text{ kg} - \frac{6}{15} \text{ kg} = \frac{44}{15} \text{ kg}\end{aligned}$$

$$\begin{aligned}\text{Final amount of sugar left} &= \frac{3}{4} \times \frac{44}{15} \text{ kg} = \frac{33}{15} \text{ kg} \\ &= 2 \frac{3}{15} \text{ kg} = 2 \frac{1}{5} \text{ kg}\end{aligned}$$

Qn 6

$$\begin{aligned}\text{No. of pieces} &= 7 \frac{2}{5} \text{ m} \div \frac{4}{5} \text{ m} \\ &= \frac{37}{5} \div \frac{4}{5} = \frac{37}{5} \times \frac{5}{4} \\ &= \frac{37}{4} = 9 \frac{1}{4}\end{aligned}$$

(a) She can cut **9** shorter pieces

(b) Length of remaining ribbon = $\frac{1}{4} \times \frac{4}{5} \text{ m} = \frac{1}{5} \text{ m}$

Qn 7

$$\begin{aligned}\text{No. of cups} &= 6 \frac{1}{2} \ell \div \frac{2}{5} \ell \\ &= \frac{13}{2} \div \frac{2}{5} = \frac{13}{2} \times \frac{5}{2} \\ &= \frac{65}{4} = 16 \frac{1}{4} \text{ cups}\end{aligned}$$

(a) She can pour **16** cups

(b) Amount of remaining orange juice = $\frac{1}{4} \times \frac{2}{5} \ell = \frac{1}{10} \ell$

Chapter 3 Rate

Unit 3.1 Rate Involving One Object

Qn1

$$\begin{aligned}1 \text{ minute} &\rightarrow 6 \text{ plates} \\ 45 \text{ minutes} &\rightarrow 45 \times 6 = \mathbf{270 \text{ plates}}\end{aligned}$$

Qn 2

$$3 \text{ days} \rightarrow 1 \text{ house}$$

$$1 \text{ day} \rightarrow \frac{1}{3} \text{ house}$$

$$36 \text{ days} \rightarrow \frac{1}{3} \times 36 = \mathbf{12 \text{ houses}}$$

Qn 3

$$\begin{aligned}8 \text{ notebooks} &\rightarrow \$7.20 \\ 1 \text{ notebook} &\rightarrow \$7.20 \div 8 = \$0.90 \\ 14 \text{ notebooks} &\rightarrow 14 \times \$0.90 = \mathbf{\$12.60}\end{aligned}$$

Qn 4

$$\begin{aligned}6 \text{ litres} &\rightarrow 54 \text{ km} \\ 1 \text{ litre} &\rightarrow 54 \text{ km} \div 6 = 9 \text{ km} \\ 18 \text{ litres} &\rightarrow 18 \times 9 \\ &= \mathbf{162 \text{ km}}\end{aligned}$$

Qn 5

$$\begin{aligned}5 \text{ lessons} &\rightarrow \$125 \\ 1 \text{ lesson} &\rightarrow \$125 \div 5 = \$25 \\ 16 \text{ lessons} &\rightarrow 16 \times \$25 = \mathbf{\$400}\end{aligned}$$

Qn 6

In a day, Johnny paint $\frac{1}{8}$ house, Alan paint $\frac{1}{10}$ house

$$\text{Together, they paint } \frac{1}{8} + \frac{1}{10} = \frac{5}{40} + \frac{4}{40} = \frac{9}{40}$$

$\frac{9}{40}$ house take both 1 day, $\frac{1}{40}$ house take both $\frac{1}{9}$ day

The whole house will take both $\frac{40}{9}$ days = $4 \frac{4}{9}$ days.

Unit 3.2 – Rate Involving Two Different Objects

Qn 1

$$\begin{aligned}11.4 \text{ km} - 2 \text{ km} &= 9.4 \text{ km} \\ 9.4 \text{ km} &= 9.4 \times 1000 = 9400 \text{ m} \\ 9400 \text{ m} \div 500 \text{ m} &= 18, \text{ Remainder } 400 \text{ m}\end{aligned}$$

$$\begin{aligned}\text{Taxi fare} &= \$4.50 + 19 \times \$0.40 + \$4.20 \\ &= \mathbf{\$16.30}\end{aligned}$$

Qn 2

(a) 4 p.m. to 5 p.m., he will pay \$5
5 p.m. to 7 p.m., he will pay $\$8 \times 2 = \16

Total Jason had to pay = $\$5 + \$16 = \mathbf{\$21}$

Qn 2 (Cont.)

(b) 4 p.m. to 7 p.m., she will pay $\$9 \times 3 = \27

Difference she had to pay = $\$27 - \21
= **\$6**

Qn 3

$$115\text{m}^3 = 50\text{m}^3 + 50\text{m}^3 + 15\text{m}^3$$

$$\text{Cost} = \$1.35 \times 50 + \$1.45 \times 50 + \$1.60 \times 15$$
$$= \mathbf{\$164}$$

Qn 4

3.30 p.m. to 6 p.m., duration = 2h 30min = 1h + 1h 30min
Parking charges = $\$2.50 + \$1.50 \times 3 + \$5 = \mathbf{\$12}$

Qn 5

$$\text{Weekday} = \$7 \times 8 + 2 \times \$10 = \$76$$

$$\text{Weekend} = \$76 \times 1.5 = \$114$$

$$\text{Wages} = \$76 \times 4 + \$114 \times 2$$
$$= \mathbf{\$532}$$

Qn 6

(a) 10 min = 5 min + 5 min

$$\text{Total cost} = \$3.20 + \$0.50 \times 5 = \mathbf{\$5.70}$$

(b) Difference in first 5 min = $\$4 - \$3.20 = \$0.80$

$$\text{Difference in every additional min}$$
$$= \$0.50 - \$0.40$$
$$= \$0.10$$

$$\text{Number of additional min needed to close the gap of } \$0.80$$
$$= \$0.80 \div \$0.10$$
$$= 8 \text{ minutes}$$

$$\text{Total duration of talk time} = 8 \text{ min} + 5 \text{ min} = \mathbf{13 \text{ min}}$$

Unit 3.3 – Key Construct: Rate involving 2 Different Objects

Qn 1

In 1 min, machine X print $\frac{1}{40}$ of the stickers.

In 1 min, machine Y print $\frac{1}{50}$ of the stickers.

$$\text{In 1 min, difference} = \frac{1}{40} - \frac{1}{50} \text{ of the stickers.}$$
$$= \frac{5}{200} - \frac{4}{200} \text{ of the stickers}$$
$$= \frac{1}{200} \text{ stickers}$$

$$\frac{1}{200} \text{ stickers} = \mathbf{10 \text{ stickers}}$$

Qn 2

In 1 day, Johnny can paint $\frac{1}{6}$ house

Together, Johnny and Ramesh can paint $\frac{1}{3}$ house

Ramesh alone can paint $\frac{1}{3} - \frac{1}{6} = \frac{1}{6}$ house

$\frac{1}{6}$ house take Ramesh 1 day

Whole house will take Ramesh **6 days**.

Qn 3

In 1 day, John and Rauf build $\frac{1}{4}$ of the model train, Rauf

and Sean build $\frac{1}{6}$ of the model train and John and Sean

build $\frac{1}{3}$ of the model train.

Together (John, Rauf and Sean) build

$$\rightarrow \frac{1}{4} + \frac{1}{6} + \frac{1}{3} \rightarrow \frac{9}{12} = \frac{3}{4} \text{ of the model train}$$

John, Rauf and Sean build

$\frac{3}{8}$ of the model train in 1 day

$\frac{1}{8}$ of the model train in $\frac{1}{3}$ day

$\frac{8}{8}$ of the model train in $\frac{8}{3}$ days = **$2\frac{2}{3}$ days**.

Qn 4

In 2 min, machine A assembles 12 toys

In 3min, machine B assembles 15 toys

In 1 minute, machine A assembles 6 toys

In 1 minute, machine B assembles 5 toys

(a) **Machine A** is faster

(b) In 5 min, machine B assembles $5 \times 5 = 25$ toys

$$\text{Big difference needed} = 25 + 24 = 49 \text{ toys}$$

$$\text{Small difference} = 6 - 5 = 1 \text{ toy}$$

$$\text{No. of mins needed} = 49 \div 1 = \mathbf{49 \text{ min}}$$

Qn 5

In 1min, machine A folds 5 boxes

In 3min, machine A folds 15 boxes.

In 3min, machine B folds 10 boxes.

In 3min, machine A folds 5 more boxes than machine B.

From 0900 to 0930, machine B folds $10 \times 10 = 100$ boxes.

No. of sets of 3min needed for machine A to fold 125 more boxes than machine B

$$= (100 + 125) \div (15 - 10) = 45 \text{ blocks of 3min}$$

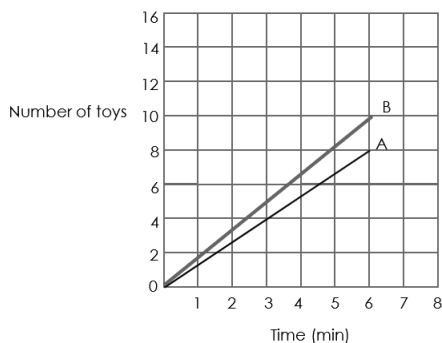
$$\text{Actual time needed} = 45 \times 3\text{min} = 135\text{min} = 2\text{h } 15\text{min}$$

At **11.45 a.m.**, machine A will fold 125 more boxes than machine B.

Qn 6

- (a) Machine A in 6min can assemble 8 toys
Machine A in 1 hour can assemble $8 \times 10 = 80$ toys

(b)



- (c) Machine A in 90min can assemble $8 \times 15 = 120$ toys
In 1 hour, machine B assembles 20 more toys than machine A.

Time needed for machine B = $120 \div 20 = 6$ hours.

At 4.30 p.m., both machines will assemble the same number of toys.

Chapter 4 Angles I

Unit 4.1 – Angles on a Straight Line

Qn 1

$$\angle x = 180^\circ - 54^\circ - 78^\circ = 48^\circ$$

Qn 2

$$\angle x = 180^\circ - 98^\circ - 42^\circ = 40^\circ$$

Qn 3

$$\begin{aligned} 80^\circ - 60^\circ &= 120^\circ \\ 8 \text{ units} &= 120^\circ \\ 1 \text{ unit} &= 15^\circ \\ \angle y &= 5 \text{ units} \\ &= 5 \times 15^\circ \\ &= 75^\circ \end{aligned}$$

$$\begin{aligned} \angle x &= 3 \text{ units} \\ &= 3 \times 15^\circ \\ &= 45^\circ \end{aligned}$$

Qn 4

$$\angle y = 2 \text{ units}, \angle x = 1 \text{ unit}, \angle z = 1 \text{ unit}$$

$$\begin{aligned} \text{Total} &= 4 \text{ units} = 180^\circ \\ 1 \text{ unit} &= 45^\circ \\ \angle x &= 1 \text{ unit} = 45^\circ \end{aligned}$$

$$\begin{aligned} \angle y &= 2 \text{ units} = 2 \times 45^\circ = 90^\circ \\ \angle z &= 1 \text{ unit} = 45^\circ \end{aligned}$$

Qn 5

$$\begin{aligned} \angle x &= 180^\circ - 90^\circ - 36^\circ = 54^\circ \\ \angle y &= 90^\circ - 34^\circ = 56^\circ \end{aligned}$$

Unit 4.2 – Vertically Opposite Angles

Qn 1

$$\begin{aligned} \angle y &= 25^\circ \text{ (vertically opposite } \angle) \\ \angle x &= 50^\circ \text{ (vertically opposite } \angle) \end{aligned}$$

Qn 2

$$\begin{aligned} \angle y + 45^\circ &= 125^\circ \text{ (vertically opposite } \angle) \\ \angle y &= 125^\circ - 45^\circ \text{ (vertically opposite } \angle) \\ &= 80^\circ \end{aligned}$$

Qn 3

$$\begin{aligned} \angle x + \angle y &= 120^\circ \text{ (vertically opposite } \angle) \\ 3 \text{ units} &= 120^\circ \\ 1 \text{ unit} &= 40^\circ \\ \angle x &= 2 \text{ units} \\ &= 2 \times 40^\circ \\ &= 80^\circ \\ \angle y &= 1 \text{ unit} \\ &= 40^\circ \end{aligned}$$

Qn 4

$$\begin{aligned} \angle x + \angle y + 120^\circ &= 180^\circ \text{ (}\angle \text{ on straight line)} \\ \angle x + \angle y &= 60^\circ \\ 3 \text{ units} &= 60^\circ \\ 1 \text{ unit} &= 20^\circ \\ \angle x &= 2 \text{ units} \\ &= 2 \times 20^\circ \\ &= 40^\circ \\ \angle y &= 20^\circ \end{aligned}$$

Qn 5

$$\begin{aligned} \angle x &= 32^\circ \\ \angle y &= 180^\circ - \angle x - 74^\circ \\ &= 180^\circ - 32^\circ - 74^\circ \\ &= 74^\circ \text{ (}\angle \text{ on a straight line)} \end{aligned}$$

Qn 6

$$\begin{aligned} \angle x &= 42^\circ \text{ (vertically opposite } \angle) \\ \angle y &= 180^\circ - 83^\circ - 42^\circ \\ &= 55^\circ \text{ (}\angle \text{ on a straight line)} \end{aligned}$$

Qn 7

$$\begin{aligned} \angle x + \angle y + 84^\circ &= 180^\circ \text{ (}\angle \text{ on a straight line)} \\ \angle x + \angle y &= 180^\circ - 84^\circ \\ &= 96^\circ \\ 4 \text{ units} &= 96^\circ \\ 1 \text{ unit} &= 24^\circ \\ \angle x &= 3 \text{ units} = 3 \times 24^\circ = 72^\circ \\ \angle y &= 1 \text{ unit} = 24^\circ \\ \angle z &= \angle x \\ &= 72^\circ \text{ (vertically opposite } \angle) \end{aligned}$$

Unit 4.3 – Alternate, Corresponding & Interior Angles

Qn 1

$$\begin{aligned} \angle BFC &= 130^\circ \text{ (corresponding } \angle) \\ \angle y &= 180^\circ - 130^\circ \\ &= 50^\circ \text{ (}\angle \text{ on a straight line)} \\ \angle EFC &= 130^\circ - 75^\circ \\ &= 55^\circ \\ \angle ECF &= 180^\circ - 55^\circ - 112^\circ \\ &= 13^\circ \\ \angle x &= 180^\circ - 13^\circ - 130^\circ \\ &= 37^\circ \text{ (sum of } \angle \text{ s in a } \triangle) \end{aligned}$$

Qn 2

$$\angle a = 180^\circ - 69^\circ - 80^\circ \\ = 31^\circ$$

$$\angle b = 180^\circ - 100^\circ \\ = 80^\circ$$

Qn 3

$$\angle z = 180^\circ - 56^\circ - 34^\circ \\ = 90^\circ \text{ (}\angle\text{s on a straight line)} \\ 2x = 180^\circ - 34^\circ - 90^\circ \text{ (alternate } \angle\text{)} \\ = 56^\circ \\ x = 28^\circ$$

$$3y = 180^\circ - 90^\circ \text{ (alternate } \angle\text{)} \\ = 90^\circ \\ y = 30^\circ$$

Qn 4

$$\angle x = 180^\circ - 135^\circ \\ = 45^\circ$$

$$\angle y = 135^\circ$$

Qn 5

$$180^\circ - 93^\circ = 87^\circ \\ 180^\circ - 78^\circ = 102^\circ$$

$$\angle x + \angle y = 360^\circ - 102^\circ - 87^\circ \\ = 171^\circ$$

Qn 6

$$\angle a = 180^\circ - 61^\circ = 119^\circ \\ 180^\circ - 31^\circ - 61^\circ = 88^\circ$$

$$\angle b = 180^\circ - 88^\circ - 62^\circ \\ = 30^\circ$$

Qn 7

$$\angle BDE = 50^\circ \text{ (alternate } \angle\text{)} \\ \angle p = 50^\circ \div 2 \\ = 25^\circ \text{ (}\angle\text{ bisector)}$$

$$\angle BGD = 180^\circ - 105^\circ \\ = 75^\circ$$

$$\angle q = 180^\circ - 75^\circ - 25^\circ \\ = 80^\circ \text{ (sum of } \angle\text{s in a } \Delta\text{)}$$

Qn 8

$$\angle BEG = 60^\circ \text{ (alternate } \angle\text{)} \\ \angle x = 60^\circ \div 2 \\ = 30^\circ \\ \angle BDE = 180^\circ - 125^\circ \\ = 55^\circ \text{ (}\angle\text{ on a straight line)} \\ \angle y = 180^\circ - 55^\circ - 30^\circ \\ = 95^\circ \text{ (sum of } \angle\text{s in a } \Delta\text{)} \\ \angle z = 180^\circ - 30^\circ \\ = 150^\circ \text{ (sum of interior } \angle\text{s)}$$

Unit 4.4 – Isosceles Triangle

Qn 1

$$\angle CBE = 85^\circ \text{ (isosceles } \Delta\text{)} \\ \angle CAD = 180^\circ - 85^\circ - 85^\circ \\ = 10^\circ \text{ (sum of } \angle\text{s in a } \Delta\text{)} \\ \angle FBA = 180^\circ - 85^\circ \\ = 95^\circ \text{ (}\angle\text{ on a straight line)}$$

Qn 1 (Cont.)

$$\angle BFA = 180^\circ - 95^\circ - 10^\circ \\ = 75^\circ \text{ (sum of } \angle\text{s in a } \Delta\text{)} \\ \angle m = 180^\circ - 75^\circ \\ = 105^\circ \text{ (}\angle\text{ on a straight line)}$$

Qn 2

$$\angle ABC = \angle ACB \\ = 180^\circ - 110^\circ \\ = 70^\circ \text{ (}\angle\text{ on a straight line)} \\ \angle XBA = 180^\circ - 70^\circ \\ = 110^\circ \text{ (}\angle\text{ on a straight line)} \\ \angle a = 180^\circ - 45^\circ - 110^\circ \\ = 25^\circ \text{ (sum of } \angle\text{s in a } \Delta\text{)}$$

Qn 3

$$\angle PQR = 55^\circ \text{ (isosceles } \Delta\text{)} \\ \angle PRQ = 180^\circ - 55^\circ - 55^\circ \text{ (sum of } \Delta\text{)} \\ = 70^\circ \\ \angle PRS = 180^\circ - 70^\circ \text{ (}\angle\text{s on a straight line)} \\ = 110^\circ \\ \angle SRT = 180^\circ - 110^\circ \\ = 70^\circ \text{ (}\angle\text{s on straight line)} \\ \angle RST = 180^\circ - 70^\circ - 70^\circ \\ = 40^\circ$$

Qn 4

$$\angle PQT = 70^\circ \text{ (isosceles } \Delta\text{)} \\ \angle QTU = 70^\circ \text{ (alternate } \angle\text{)} \\ \angle QTR = 70^\circ - 50^\circ \\ = 20^\circ$$

Qn 5

$$\angle x = \frac{180^\circ - 130^\circ}{2} \\ = 25^\circ \text{ (isosceles } \Delta\text{)} \\ \angle ACF = 180^\circ - \angle x \\ = 180^\circ - 25^\circ \\ = 155^\circ \text{ (sum of interior } \angle\text{s)} \\ \angle DCF = 180^\circ - 110^\circ \\ = 70^\circ \text{ (sum of interior } \angle\text{s)} \\ \angle y = 155^\circ - 70^\circ - 25^\circ \\ = 60^\circ$$

Qn 6

$$\angle z = 38^\circ \text{ (alternate } \angle\text{s)} \\ 180^\circ - 30^\circ - 38^\circ = 112^\circ \text{ (sum of } \angle\text{s in a } \Delta\text{)} \\ \angle x = 180^\circ - 112^\circ \\ = 68^\circ \text{ (}\angle\text{ on a straight line)} \\ \angle y = 180^\circ - \angle x - \angle x \\ \text{(vertically opp. } \angle\text{s, sum of } \angle\text{ in a } \Delta\text{)} \\ = 180^\circ - 68^\circ - 68^\circ \\ = 44^\circ$$

Qn 7

$$\frac{180^\circ - 75^\circ}{2} = 55^\circ \\ 180^\circ - 30^\circ - 30^\circ = 120^\circ \\ \angle y = 360^\circ - 120^\circ \\ = 240^\circ \\ \angle x = 55^\circ - 30^\circ \\ = 25^\circ$$

Qn 8

$$\begin{aligned}\angle KEF &= 60^\circ - 38^\circ \\ &= 22^\circ \\ \angle KFE &= 60^\circ - 25^\circ \\ &= 35^\circ \\ \angle EKF &= 180^\circ - 22^\circ - 35^\circ \\ &= 123^\circ \text{ (vertically opp. } \angle\text{s, sum of } \angle\text{s in a } \Delta\text{)} \\ \angle HKG &= 123^\circ \text{ (vertically opp. } \angle\text{s)}\end{aligned}$$

Qn 9

$$\begin{aligned}\angle PQR &= 55^\circ \text{ (isosceles } \Delta\text{)} \\ \angle PRQ &= 180^\circ - 55^\circ - 55^\circ \text{ (sum of triangle)} \\ &= 70^\circ\end{aligned}$$

$$\begin{aligned}\text{(a) } \angle PRS &= 180^\circ - 70^\circ \text{ (angle on straight line)} \\ &= 110^\circ\end{aligned}$$

$$\begin{aligned}\angle SRT &= 180^\circ - 110^\circ \\ &= 70^\circ \text{ (angle on straight line)}\end{aligned}$$

$$\begin{aligned}\text{(b) } \angle RST &= 180^\circ - 70^\circ - 70^\circ \\ &= 40^\circ \text{ (isosceles } \Delta\text{)}\end{aligned}$$

Chapter 5 Angles II (Closed Figures)

Unit 5.1 – Interior and Exterior Angles Within A Triangle

Qn 1

$$\begin{aligned}\angle x &= 125^\circ - 70^\circ \\ &= 55^\circ \text{ (2 interior } \angle = 1 \text{ exterior } \angle)\end{aligned}$$

Qn 2

$$\begin{aligned}\angle y &= 142^\circ - 65^\circ \\ &= 77^\circ \text{ (2 interior } \angle = 1 \text{ exterior } \angle)\end{aligned}$$

Qn 3

$$\begin{aligned}\angle z &= 34^\circ + 42^\circ \\ &= 76^\circ \text{ (2 interior } \angle\text{s} = 1 \text{ exterior } \angle) \\ \angle y + 56^\circ &= 76^\circ \text{ (2 interior } \angle\text{s} = 1 \text{ exterior } \angle) \\ \angle y &= 20^\circ\end{aligned}$$

Qn 4

$$\begin{aligned}\angle y &= 42^\circ + 54^\circ \\ &= 96^\circ \text{ (2 internal } \angle = 1 \text{ external } \angle) \\ 180^\circ - 96^\circ &= 84^\circ \\ \angle x &= 180^\circ - 84^\circ - 20^\circ \\ &= 76^\circ\end{aligned}$$

Qn 5

$$\begin{aligned}\angle a + \angle b + 20^\circ &= \angle c + \angle d + 20^\circ = 180^\circ \text{ (sum of } \angle\text{s in } \Delta) \\ \angle a + \angle b + \angle c + \angle d &= (180^\circ \times 2) - 20^\circ - 20^\circ \\ &= 360^\circ - 40^\circ \\ &= 320^\circ\end{aligned}$$

Qn 6

$$\begin{aligned}60^\circ + 60^\circ &= 120^\circ \\ 180^\circ - 110^\circ - 20^\circ &= 50^\circ \\ \angle x &= 180^\circ - 100^\circ - 70^\circ \\ &= 10^\circ \text{ (sum of } \angle\text{s in a } \Delta)\end{aligned}$$

Qn 7

$$\begin{aligned}\angle WUV &= \angle b + \angle d \text{ (2 internal } \angle = 1 \text{ external } \angle) \\ \angle UWV &= \angle a + \angle c \text{ (2 internal } \angle = \text{external } \angle) \\ \angle a + \angle b + \angle c + \angle d + 20^\circ &= 180^\circ \text{ (sum of } \Delta) \\ \angle a + \angle b + \angle c + \angle d &= 160^\circ\end{aligned}$$

Qn 8

$$\begin{aligned}\angle a + \angle b + \angle c + \angle d + \angle e + \angle f \\ &= (180^\circ \times 3) - 180^\circ \\ &= 360^\circ \text{ since the sum of } \angle \text{ of } \Delta RSV = 180^\circ\end{aligned}$$

Qn 9

$$\begin{aligned}\angle PQS &= \frac{80^\circ - 34^\circ}{2} \\ &= 73^\circ \text{ (isosceles } \Delta)\end{aligned}$$

$$\begin{aligned}\angle x &= 180^\circ - 73^\circ - 15^\circ \\ &= 92^\circ \text{ (sum of } \angle\text{s in } \Delta)\end{aligned}$$

$$\begin{aligned}\angle PTR &= 180^\circ - 92^\circ \\ &= 88^\circ\end{aligned}$$

$$\begin{aligned}\angle y &= 34^\circ + 88^\circ \\ &= 122^\circ \text{ (2 interior } \angle\text{s} = 1 \text{ exterior } \angle)\end{aligned}$$

Unit 5.2 – Angle Properties Within A Rhombus

Qn 1

$$\begin{aligned}\angle DAB &= 180^\circ - 30^\circ - 30^\circ \\ &= 120^\circ \text{ (sum of } \angle\text{s in a } \Delta)\end{aligned}$$

$$\begin{aligned}\angle x &= \frac{120^\circ}{2} \\ &= 60^\circ\end{aligned}$$

Qn 2

$$\begin{aligned}\angle QPB &= 180^\circ - 114^\circ \\ &= 66^\circ\end{aligned}$$

$$\begin{aligned}\text{(a) } \angle QPR &= \frac{66^\circ}{2} \\ &= 33^\circ\end{aligned}$$

$$\text{(b) } \angle QCB = 96^\circ$$

$$\begin{aligned}\text{(c) } \angle RSC &= 180^\circ - 84^\circ - 33^\circ \\ &= 63^\circ\end{aligned}$$

Qn 3

$$\begin{aligned}\angle ADC &= 180^\circ - 130^\circ \\ &= 50^\circ \\ \angle x &= \frac{50^\circ}{2} \\ &= 25^\circ\end{aligned}$$

Qn 4

$$\begin{aligned}180^\circ - 45^\circ - 90^\circ - 30^\circ &= 15^\circ \\ \angle x &= 15^\circ\end{aligned}$$

Qn 5

$$\begin{aligned}\angle FBE &= 90^\circ \\ \text{(a) } \angle BFE &= \angle DFC \\ &= 180^\circ - 90^\circ - 35^\circ \\ &= 55^\circ \\ \angle DBF &= 45^\circ \text{ (diagonal of square)} \\ \angle BDF + 45^\circ &= \angle DFC\end{aligned}$$

$$\begin{aligned}\text{(b) } \angle BDF &= 55^\circ - 45^\circ \\ &= 10^\circ\end{aligned}$$

Qn 6

$$\begin{aligned}\angle x &= 180^\circ - 108^\circ \\ &= 72^\circ \text{ (interior } \angle\text{s)} \\ 180^\circ - 90^\circ - 47^\circ &= 43^\circ \\ \angle y &= 43^\circ \text{ (alternate } \angle\text{s)}\end{aligned}$$

Qn 7

$$\begin{aligned}\angle FBD &= 180^\circ - 70^\circ - 45^\circ \\ &= 65^\circ \\ \angle x &= 65^\circ \div 2 \\ &= 32.5^\circ \\ \angle BDE &= 180^\circ - 65^\circ \\ &= 115^\circ \\ 70^\circ + \angle y &= 115^\circ \text{ (2 internal } \angle = 1 \text{ external } \angle) \\ \angle y &= 115^\circ - 70^\circ \\ &= 45^\circ\end{aligned}$$

Qn 8

$$\begin{aligned}\angle x &= 180^\circ - 105^\circ + 20^\circ \\ &= 55^\circ \\ \angle y &= 55^\circ + 20^\circ + 20^\circ \\ &= 95^\circ \text{ (2 interior } \angle\text{s} = 1 \text{ exterior } \angle)\end{aligned}$$

Qn 9

$$\begin{aligned}\text{BD diagonal, bisector} &\rightarrow \angle y = \angle 2x \\ \angle ADC &= 180^\circ - 110^\circ \\ &= 70^\circ \text{ (interior } \angle) \\ \angle y &= \angle 2x \\ &= 180^\circ - 110^\circ \\ &= \frac{70^\circ}{2} \text{ (sum of } \angle\text{s in a } \triangle) \\ \angle x &= 17.5^\circ \\ \angle y &= 35^\circ\end{aligned}$$

Qn 10

$$\begin{aligned}\angle DAO &= 45^\circ \text{ (diagonal of square)} \\ \angle DAE &= 180^\circ - 90^\circ - 60^\circ \\ &= 30^\circ \text{ (sum of } \triangle) \\ \angle y &= 45^\circ - 30^\circ \\ &= 15^\circ \\ \angle x &= 15^\circ + 90^\circ \\ &= 105^\circ \text{ (2 internal } \angle = 1 \text{ external } \angle)\end{aligned}$$

Unit 5.3 – Angles Properties Within a Parallelogram

Qn 1

$$\begin{aligned}\angle y &= 60^\circ \text{ (alternate } \angle) \\ \angle x &= 180^\circ - 35^\circ - 70^\circ - 60^\circ \\ &= 15^\circ \text{ (sum of } \angle\text{s in a } \triangle) \\ \angle z &= \angle x + \angle y \\ &= 60^\circ + 15^\circ \\ &= 75^\circ \text{ (2 interior } \angle\text{s} = 1 \text{ exterior } \angle)\end{aligned}$$

Qn 2

$$\begin{aligned}\angle x &= 25^\circ \text{ (alternate } \angle) \\ \angle y &= 42^\circ + 25^\circ \\ &= 67^\circ \text{ (2 internal } \angle = 1 \text{ external } \angle) \\ \angle z &= 180^\circ - 80^\circ - 42^\circ - 25^\circ \\ &= 33^\circ \text{ (sum of } \triangle)\end{aligned}$$

Qn 3

$$\begin{aligned}\angle RSU &= 180^\circ - 88^\circ = 92^\circ \text{ (corresponding } \angle) \\ \text{(a) } \angle SRU &= \frac{180^\circ - 92^\circ}{2} \\ &= 44^\circ \text{ (isosceles } \triangle) \\ \text{(b) } \angle PSR &= 360^\circ - 144^\circ - 92^\circ \\ &= 124^\circ\end{aligned}$$

Qn 4

$$\begin{aligned}\angle BAC &= 30^\circ \text{ (alternate } \angle) \\ \angle CAD &= 180^\circ - 30^\circ - 20^\circ = 130^\circ \\ \text{(a) } \angle ADC &= 180^\circ - 130^\circ - 30^\circ \\ &= 20^\circ \text{ (sum of } \triangle) \\ \text{(b) } \angle CAD &= 130^\circ \\ \text{(c) } \angle ACB &= 180^\circ - 20^\circ - 30^\circ \\ &= 130^\circ\end{aligned}$$

Unit 5.4 – Angle Properties Within A Trapezium

Qn 1

$$\begin{aligned}\angle CDB &= \frac{180^\circ - 120^\circ}{2} \\ &= 30^\circ \text{ (isosceles } \triangle) \\ \text{(a) } \angle BDE &= 78^\circ - 30^\circ \\ &= 48^\circ \\ \text{(b) } \angle BEA &= 78^\circ \text{ (corresponding } \angle) \\ \angle EBC &= 180^\circ - 120^\circ \\ &= 60^\circ \text{ (interior } \angle) \\ \angle EBA &= 130^\circ - 60^\circ \\ &= 70^\circ \\ \angle BAE &= 180^\circ - 78^\circ - 70^\circ \\ &= 32^\circ \text{ (sum of } \angle\text{s in a } \triangle)\end{aligned}$$

Qn 2

$$\begin{aligned}180^\circ - 118^\circ &= 62^\circ \text{ (} \angle \text{ on straight line)} \\ \angle y &= 180^\circ - 84^\circ - 62^\circ \\ &= 34^\circ \text{ (sum of } \triangle) \\ \angle x &= \angle y \\ &= 34^\circ \text{ (alt. } \angle)\end{aligned}$$

Qn 3

$$\begin{aligned}\angle DAB &= 180^\circ - 86^\circ \\ &= 94^\circ \\ \angle ABD &= \frac{180^\circ - 94^\circ}{2} \\ &= 43^\circ \\ \angle y &= 180^\circ - 88^\circ - 43^\circ \\ &= 49^\circ \text{ (interior } \angle\text{s)} \\ \angle x &= 180^\circ - 86^\circ \\ &= 94^\circ \text{ (interior } \angle\text{s)}\end{aligned}$$

Qn 4

$$\begin{aligned}\angle y &= 90^\circ - 48^\circ \\ &= 42^\circ \text{ (2 interior } \angle\text{s} = 1 \text{ exterior } \angle)\end{aligned}$$

Qn 5

$$\begin{aligned}\angle BFC &= 54^\circ \text{ (alternate } \angle) \\ \text{(a) } \angle t &= 180^\circ - 57^\circ - 54^\circ \\ &= 69^\circ \\ \text{(b) } \angle y &= 69^\circ - 54^\circ \\ &= 15^\circ\end{aligned}$$

Qn 5 (Cont.)

$$\begin{aligned} \text{(c)} \quad \angle BAF &= 54^\circ \text{ (isosceles } \Delta) \\ \angle x &= 180^\circ - 54^\circ - 54^\circ \\ &= 72^\circ \text{ (sum of isosceles } \Delta) \end{aligned}$$

$$\begin{aligned} \text{(d)} \quad \angle u &= \angle CBE \\ &= 57^\circ \text{ (alternate } \angle) \end{aligned}$$

Unit 5.5 – Key Construct: Similar Angles in Folded Shapes

Qn 1

$$\begin{aligned} \angle DCA &= (90^\circ - 48^\circ) \div 2 \\ &= 21^\circ \\ \angle DAC &= 180^\circ - 90^\circ - 21^\circ \\ &= 69^\circ \end{aligned}$$

Qn 2

$$\begin{aligned} \angle ACD &= 45^\circ \\ \angle CAD &= 180^\circ - 118^\circ - 45^\circ \\ &= 17^\circ \\ \angle BAE &= 45^\circ - 17^\circ - 17^\circ \\ &= 11^\circ \end{aligned}$$

Qn 3

$$\begin{aligned} \angle BGC &= 180^\circ - 61^\circ - 61^\circ - 22^\circ - 22^\circ \\ &= 14^\circ \\ \angle CDG &= 180^\circ - 22^\circ - 48^\circ \\ &= 110^\circ \end{aligned}$$

Qn 4

$$\begin{aligned} \angle PQR &= 45^\circ \\ \angle SQO &= (90^\circ - 45^\circ) \div 2 \\ &= 22.5^\circ \\ \angle SOQ &= 180^\circ - 90^\circ - 22.5^\circ \\ &= 67.5^\circ \end{aligned}$$

Qn 5

$$\begin{aligned} \angle BAC &= 180^\circ - 35^\circ - 35^\circ \\ &= 110^\circ \\ \angle DAB &= \angle CAE \\ &= 180^\circ - 129^\circ - 33^\circ \\ &= 18^\circ \\ \angle BAC &= 110^\circ - 18^\circ \times 4 \\ &= 38^\circ \end{aligned}$$

Qn 6

$$\begin{aligned} \angle XZY &= (180^\circ - 52^\circ) \div 2 \\ &= 64^\circ \\ \angle MNZ &= \angle NMZ \\ &= (180^\circ - 64^\circ) \div 2 \\ &= 58^\circ \\ \angle ZNM &= 58^\circ \\ \angle XMZ &= 180^\circ - 58^\circ - 58^\circ \\ &= 64^\circ \end{aligned}$$

Qn 7

$$\begin{aligned} \angle EDB &= 180^\circ - 67^\circ \\ &= 113^\circ \end{aligned}$$

Qn 7 (Cont.)

$$\begin{aligned} \angle ABC &= (180^\circ - 98^\circ) \div 2 \\ &= 41^\circ \\ \angle DEB &= 180^\circ - 41^\circ - 113^\circ \\ &= 26^\circ \\ \angle AEB &= 180^\circ - 26^\circ \times 2 \\ &= 128^\circ \end{aligned}$$

Chapter 6 Area of Triangle

Unit 6.1 – Area of Triangle

Qn 1

$$\begin{array}{ll} \text{Height} = \mathbf{AB} & \text{Height} = \mathbf{AF} \\ \text{Height} = \mathbf{DC} & \text{Height} = \mathbf{AB} \end{array}$$

Qn 2

$$\begin{array}{ll} \text{Base} = \mathbf{12 \text{ cm}} & \text{Height} = \mathbf{16 \text{ cm}} \end{array}$$

Qn 3

$$\begin{array}{ll} \text{Base} = \mathbf{4 \text{ cm}} & \text{Height} = \mathbf{7 \text{ cm}} \end{array}$$

Qn 4

$$\begin{array}{ll} \text{Base} = \mathbf{5 \text{ cm}} & \text{Height} = \mathbf{20 \text{ cm}} \end{array}$$

Qn 5

$$\begin{array}{ll} \text{Base} = \mathbf{14 \text{ cm}} & \text{Height} = \mathbf{7 \text{ cm}} \end{array}$$

Qn 6

$$\begin{array}{ll} \text{Base} = 4 \text{ cm} + 8 \text{ cm} & \text{Height} = 8 \text{ cm} - 5 \text{ cm} \\ = \mathbf{12 \text{ cm}} & = \mathbf{3 \text{ cm}} \end{array}$$

Qn 7

$$\begin{aligned} \text{Area of } \triangle BCD &= \left(\frac{1}{2} \times 18 \times 8 \right) \\ &= \left(\frac{1}{2} \times 8 \times DF \right) \\ DF &= \frac{18 \times 8}{12} \\ &= \mathbf{12 \text{ cm}} \end{aligned}$$

Qn 8

$$\begin{aligned} \text{Area of shaded } \triangle BCD &= \left(\frac{1}{2} \times 20 \times CE \right) \\ &= \left(\frac{1}{2} \times 16 \times 15 \right) \\ CE &= \frac{16 \times 15}{20} \\ &= \mathbf{12 \text{ cm}} \end{aligned}$$

Qn 9

$$\begin{aligned} \text{Area of } \triangle ABC &= \left(\frac{1}{2} \times 15 \times 20 \right) \\ &= \left(\frac{1}{2} \times 30 \times BD \right) \\ BD &= \frac{15 \times 20}{30} \\ &= \mathbf{10 \text{ cm}} \end{aligned}$$

Qn 10

Area of shaded $\triangle ABC$

$$= \left(\frac{1}{2} \times 12 \times AB\right)$$

$$= \left(\frac{1}{2} \times 28 \times 18\right)$$

$$AB = \frac{28 \times 18}{12}$$

$$= 42 \text{ cm}$$

Unit 6.2 – Finding the Area of a Triangle in Unit Squares

Qn 1

(a) Triangle

$$\begin{aligned} &= (6 \times 6) - \left(\frac{1}{2} \times 4 \times 2\right) - \left(\frac{1}{2} \times 6 \times 2\right) - \left(\frac{1}{2} \times 4 \times 6\right) \\ &= 36 \text{ cm}^2 - 4 \text{ cm}^2 - 6 \text{ cm}^2 - 12 \text{ cm}^2 \\ &= 14 \text{ cm}^2 \end{aligned}$$

(b) Triangle

$$\begin{aligned} &= (6 \times 6) - \left(\frac{1}{2} \times 4 \times 6\right) - \left(\frac{1}{2} \times 2 \times 3\right) - \left(\frac{1}{2} \times 3 \times 6\right) \\ &= 36 \text{ cm}^2 - 12 \text{ cm}^2 - 3 \text{ cm}^2 - 9 \text{ cm}^2 \\ &= 12 \text{ cm}^2 \end{aligned}$$

Qn 2

(a) Triangle

$$\begin{aligned} &= (4 \times 6) - \left(\frac{1}{2} \times 6 \times 1\right) - \left(\frac{1}{2} \times 3 \times 4\right) - \left(\frac{1}{2} \times 4 \times 2\right) \\ &= 24 \text{ cm}^2 - 3 \text{ cm}^2 - 6 \text{ cm}^2 - 4 \text{ cm}^2 \\ &= 11 \text{ cm}^2 \end{aligned}$$

(b) Triangle

$$\begin{aligned} &= (6 \times 5) - \left(\frac{1}{2} \times 6 \times 2\right) - \left(\frac{1}{2} \times 6 \times 3\right) \\ &= 30 \text{ cm}^2 - 6 \text{ cm}^2 - 9 \text{ cm}^2 \\ &= 15 \text{ cm}^2 \end{aligned}$$

Qn 3

(a) Shaded

$$\begin{aligned} &= (6 \times 6) - \left(\frac{1}{2} \times 4 \times 2\right) - \left(\frac{1}{2} \times 3 \times 2\right) - \left(\frac{1}{2} \times 3 \times 1\right) - \\ &\quad \left(\frac{1}{2} \times 4 \times 2\right) \\ &= 36 \text{ cm}^2 - 4 \text{ cm}^2 - 3 \text{ cm}^2 - 1.5 \text{ cm}^2 - 4 \text{ cm}^2 \\ &= 23.5 \text{ cm}^2 \end{aligned}$$

(b) Shaded

$$\begin{aligned} &= (6 \times 6) - \left(\frac{1}{2} \times 5 \times 4\right) - (4 \times 2) - \left(\frac{1}{2} \times 2 \times 2\right) - \left(\frac{1}{2} \times \right. \\ &\quad \left. 6 \times 1\right) \\ &= 36 \text{ cm}^2 - 10 \text{ cm}^2 - 8 \text{ cm}^2 - 2 \text{ cm}^2 - 3 \text{ cm}^2 \\ &= 13 \text{ cm}^2 \end{aligned}$$

Qn 4

(a) Area of rectangle = $6 \text{ cm} \times 5 \text{ cm}$
= 30 cm^2

Area of Region A = $\frac{1}{2} \times 6 \text{ cm} \times 1 \text{ cm}$
= 3 cm^2

Area of Region B = $\frac{1}{2} \times 5 \text{ cm} \times 3 \text{ cm}$
= 7.5 cm^2

Qn 4 (Cont.)

Area of region C = $\frac{1}{2} \times 2 \text{ cm} \times 3 \text{ cm}$
= 3 cm^2

Shaded area = $30 \text{ cm}^2 - 3 \text{ cm}^2 - 7.5 \text{ cm}^2 - 3 \text{ cm}^2$
= 16.5 cm^2

(b) Area of rectangle = $6 \text{ cm} \times 6 \text{ cm}$
= 36 cm^2

Area of Region A = $\frac{1}{2} \times 4 \text{ cm} \times 2 \text{ cm}$
= 4 cm^2

Area of Region B = $\frac{1}{2} \times 2 \text{ cm} \times 3 \text{ cm}$
= 3 cm^2

Area of region C = $\frac{1}{2} \times 6 \text{ cm} \times 3 \text{ cm}$
= 9 cm^2

Shaded area
= $36 \text{ cm}^2 - 9 \text{ cm}^2 - 4 \text{ cm}^2 - 3 \text{ cm}^2$
= 20 cm^2

Unit 6.3 – Triangle with Common Base or Height

Qn 1

Area of rectangle = (11×8)
= 88 cm^2

Area of 3 \triangle s

$$\begin{aligned} &= \left(\frac{1}{2} \times 11 \times 3\right) + \left(\frac{1}{2} \times 8 \times 8\right) + \left(\frac{1}{2} \times 5 \times 3\right) \\ &= 16.5 \text{ cm}^2 + 32 \text{ cm}^2 + 7.5 \text{ cm}^2 \\ &= 56 \text{ cm}^2 \end{aligned}$$

Area of shaded triangle = $88 \text{ cm}^2 - 56 \text{ cm}^2$
= 32 cm^2

Qn 2

Area of 1 triangle = $\frac{1}{2} \times b \times h$

= $\frac{1}{2} \times 10 \text{ cm} \times 10 \text{ cm}$
= 50 cm^2

Area of shaded parts = 2 triangles
= $2 \times 50 \text{ cm}^2$
= 100 cm^2

Qn 3

Area of big triangle = $\frac{1}{2} \times 20 \text{ cm} \times 10 \text{ cm}$
= 100 cm^2

Area of small triangle = $\frac{1}{2} \times 10 \text{ cm} \times 10 \text{ cm}$
= 50 cm^2

Area of shaded parts = $100 \text{ cm}^2 + 50 \text{ cm}^2$
= 150 cm^2

Qn 4

Area of 1 triangle = $\frac{1}{2} \times b \times h$

= $\frac{1}{2} \times 20 \text{ cm} \times 10 \text{ cm}$
= 100 cm^2

Area of shaded parts = 2 triangles
= $2 \times 100 \text{ cm}^2$
= 200 cm^2

Qn 5

$$\begin{aligned}\text{Area of 1 triangle} &= \frac{1}{2} \times b \times h \\ &= \frac{1}{2} \times 10 \text{ cm} \times 10 \text{ cm} \\ &= 50 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Area of shaded parts} &= 2 \text{ triangles} \\ &= 2 \times 50 \text{ cm}^2 \\ &= \mathbf{100 \text{ cm}^2}\end{aligned}$$

Qn 6

$$\triangle DEC \text{ is } \frac{1}{4} \text{ of square ABCD.}$$

$$\triangle CBF \text{ is } \frac{1}{4} \text{ of square ABCD.}$$

$$\triangle AEF \text{ is } \frac{1}{8} \text{ of square ABCD.}$$

$$\begin{aligned}\text{Shaded triangle} &= 1 - \frac{1}{4} - \frac{1}{4} - \frac{1}{8} \\ &= 1 - \frac{2}{8} - \frac{2}{8} - \frac{1}{8} \\ &= \frac{3}{8} \text{ square ABCD} \\ &= \frac{3}{8} \times 48 \text{ cm}^2 \\ &= \mathbf{18 \text{ cm}^2}\end{aligned}$$

Qn 7

$$\begin{aligned}\text{Area of shaded triangle} &= \frac{1}{2} \times 7 \times 5 \\ &= \mathbf{17.5 \text{ cm}^2}\end{aligned}$$

Unit 6.4 – Triangles with Common Bases

Qn 1

$$\begin{aligned}\text{Area of shaded parts} &= \frac{1}{2} \times 20 \text{ cm} \times 6 \text{ cm} \\ &= \mathbf{60 \text{ cm}^2}\end{aligned}$$

Qn 2

$$\begin{aligned}\text{Area of shaded parts} &= \frac{1}{2} \times 20 \text{ cm} \times 12 \text{ cm} \\ &= \mathbf{120 \text{ cm}^2}\end{aligned}$$

Qn 3

Since $\triangle ABC$ and $\triangle ADC$ share the same base AC, the area of $\triangle ABC$ is $\frac{1}{3}$ of $\triangle ADC$.

$$\begin{aligned}\text{Difference} &= 2 \text{ units} = 64 \text{ cm}^2 \\ 1 \text{ unit} &= 64 \text{ cm}^2 \div 2 \\ &= 32 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Area of } \triangle ADC &= \frac{1}{2} \times AC \times 12 \text{ cm} \\ &= 3 \times 32 \text{ cm}^2\end{aligned}$$

$$AC = 96 \text{ cm}^2 \div 6 \text{ cm} = \mathbf{16 \text{ cm}}$$

Qn 4

Since $\triangle ADE$ and $\triangle BCE$ share the same base,

$$\triangle ADE + \triangle BCE = \frac{1}{2} \text{ rectangle ABCD}$$

$$\begin{aligned}\text{Area of rectangle ABCD} &= 84 \text{ cm}^2 \times 2 \\ &= 168 \text{ cm}^2\end{aligned}$$

$$\text{Breath AD} = 168 \text{ cm}^2 \div 24 \text{ cm} = 7 \text{ cm}$$

$$\begin{aligned}\text{Perimeter of ABCD} &= (24 \text{ cm} + 7 \text{ cm}) \times 2 \\ &= \mathbf{62 \text{ cm}}\end{aligned}$$

Qn 5

Since $\triangle ABD$ and $\triangle BCD$ share the same base BD, the area of $\triangle BCD$ is $\frac{3}{5}$ of $\triangle ABD$

$$\begin{aligned}\text{Area of } \triangle ABD &= 5 \text{ units} = 30 \text{ cm}^2 \\ 1 \text{ unit} &= 30 \text{ cm}^2 \div 5 = 6 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Area of quadrilateral} &= 8 \text{ units} \\ &= 8 \times 6 \text{ cm}^2 \\ &= \mathbf{48 \text{ cm}^2}\end{aligned}$$

Qn 6

$$\begin{aligned}\text{Area of shaded region} &= \left(\frac{1}{2} \times 8 \times 20 \right) + \left(\frac{1}{2} \times 12 \times 25 \right) \\ &= 80 \text{ cm}^2 + 150 \text{ cm}^2 \\ &= \mathbf{230 \text{ cm}^2}\end{aligned}$$

Qn 7

$$\begin{aligned}\text{Area of shaded parts} &= \left(\frac{1}{2} \times 18 \times 10 \right) + \left(\frac{1}{2} \times 12 \times 10 \right) \\ &= 90 \text{ cm}^2 + 60 \text{ cm}^2 \\ &= \mathbf{150 \text{ cm}^2}\end{aligned}$$

Qn 8

$$\begin{aligned}5 \text{ units} &= 30 \text{ cm} \\ 1 \text{ unit} &= 6 \text{ cm} \\ AB &= 1 \text{ unit} = 6 \text{ cm} \\ DE &= 4 \text{ units} = 24 \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{Area of shaded parts} &= \left(\frac{1}{2} \times 24 \times 10 \right) + \left(\frac{1}{2} \times 6 \times 10 \right) \\ &= 120 \text{ cm}^2 + 30 \text{ cm}^2 \\ &= \mathbf{150 \text{ cm}^2}\end{aligned}$$

Unit 6.5 – Composite Figures Involving Triangles

Qn 1

$$\begin{aligned}\text{Area of 1 triangle} &= \frac{1}{2} \times 12 \text{ cm} \times 8 \text{ cm} \\ &= 48 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Area of figure} &= 48 \text{ cm}^2 \times 5 \\ &= \mathbf{240 \text{ cm}^2}\end{aligned}$$

Qn 2

$$\begin{aligned}\text{Area of 1 triangle} &= \frac{1}{2} \times 12 \text{ cm} \times 10 \text{ cm} \\ &= 60 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Area of 8 triangles} &= 60 \text{ cm}^2 \times 8 \\ &= \mathbf{480 \text{ cm}^2}\end{aligned}$$

Qn 3

$$\begin{aligned}\text{Area of 1 triangle} &= \frac{1}{2} \times 10 \text{ cm} \times 8 \text{ cm} \\ &= 40 \text{ cm}^2 \\ \text{Area of figure} &= 40 \text{ cm}^2 \times 6 \\ &= \mathbf{240 \text{ cm}^2}\end{aligned}$$

Qn 4

$$\begin{aligned}P + R &= \frac{1}{2} \text{ rectangle ABCD} \\ &= Q + S \\ S &= 24 \text{ cm}^2 + 45 \text{ cm}^2 - 20 \text{ cm}^2 \\ &= \mathbf{49 \text{ cm}^2}\end{aligned}$$

Qn 5

$$\begin{aligned}\text{Figure 1, Perimeter} &= (21 \text{ cm} - 5 \text{ cm} - 5 \text{ cm}) \times 4 \\ &= \mathbf{44 \text{ cm}} \\ \text{Figure 2, Perimeter} &= 21 \text{ cm} \times 2 \\ &= \mathbf{42 \text{ cm}}\end{aligned}$$

Chapter 7 Percentage

Unit 7.1 – Percentage Increase

Qn 1

$$\begin{aligned}20\% \text{ of original} &\rightarrow 85 \\ 100\% \text{ of original} &\rightarrow 5 \times 85 = \mathbf{425}\end{aligned}$$

Qn 2

$$\begin{aligned}100\% \text{ of original} &\rightarrow 1800 \\ 1\% \text{ of original} &\rightarrow 1800 \div 100 = 18 \\ 15\% \text{ of original} &\rightarrow 18 \times 15 = \mathbf{270}\end{aligned}$$

Qn 3

At first	In the end
Girls $\rightarrow 40\%$	Girls $\rightarrow 40\% + 12$ (50% of total)
Boys $\rightarrow 60\%$	Boys $\rightarrow 60\% - 60$ (50% of total)

$$\begin{aligned}20\% \text{ of the total} &\rightarrow 60 + 12 = 72 \\ 10\% \text{ of the total} &\rightarrow 36\end{aligned}$$

$$\text{Total pupils at first} \rightarrow 10 \times 36 = \mathbf{360}$$

Qn 4

$$\begin{aligned}\text{Aaron} &\rightarrow 30\% \text{ of the sum} \\ \text{Bernard} &\rightarrow 70\% \text{ of the sum}\end{aligned}$$

$$\begin{aligned}\text{Difference} &\rightarrow 40\% \text{ of the sum} = \$120 \\ 1\% \text{ of the sum} &\rightarrow \$120 \div 40 = \$3\end{aligned}$$

$$\text{Sum of money} \rightarrow 100 \times \$3 = \mathbf{\$300}$$

Qn 5

$$\begin{aligned}20\% \text{ of his salary} &\rightarrow \$800 \\ 1\% \text{ of his salary} &\rightarrow \$800 \div 20 = \$40\end{aligned}$$

$$100\% \text{ of his salary} \rightarrow 100 \times \$40 = \mathbf{\$4000}$$

Qn 6

$$\begin{aligned}30\% \text{ of boys} &\rightarrow 30\% \text{ of total} + 36 \\ 1\% \text{ of boys} &\rightarrow 1\% \text{ of total} + 1.2\end{aligned}$$

$$\begin{aligned}100\% \text{ of total} &\rightarrow 1.2 \times 100 = 120 \\ \text{Boys at first} &\rightarrow 120 + 120 = \mathbf{240}\end{aligned}$$

Unit 7.2 – Multiplication in Percentage

Qn 1

At first

$$\begin{aligned}\text{Janice's savings} &= 80\% \\ \text{David's savings} &= 100\%\end{aligned}$$

End

$$\begin{aligned}\text{Janice's savings} &= 80\% \times 80\% \\ &= \frac{80}{100} \times 80\% = 64\%\end{aligned}$$

$$\text{David's savings} = 100\%$$

$$\text{Total savings in the end} = 164\% \rightarrow \$820$$

$$1\% \rightarrow \$820 \div 164 = \$5$$

$$\text{Janice's savings at first} = \$5 \times 80 = \mathbf{\$400}$$

Qn 2

$$\begin{array}{lcl} \text{Income} & \left\{ \begin{array}{l} \text{Wife} \rightarrow 30\% \\ \text{Self} \rightarrow 70\% \end{array} \right. & \end{array}$$

$$\begin{array}{lcl} \text{Income} & \left\{ \begin{array}{l} \text{Wife} \rightarrow \frac{30}{100} \times 120\% = 36\% \\ \text{Self} \rightarrow 120\% - 36\% = 84\% \end{array} \right. & \end{array}$$

$$\begin{array}{lcl} \text{Increase in wife's income} & \rightarrow 6\% & \rightarrow \$240 \\ & 1\% & \rightarrow \$40 \end{array}$$

$$\begin{aligned}\text{Income before increase} &= 100 \times 40 \\ &= \mathbf{\$4000}\end{aligned}$$

Qn 3

$$\begin{array}{lcl} \text{Salary} & \rightarrow & 100\% \\ \text{Savings} & \rightarrow & 45\% \\ \text{Expenditure} & \rightarrow & 55\% \end{array}$$

$$\begin{aligned}\text{Salary} &\rightarrow 80\% \\ \text{Savings} &\rightarrow \frac{45}{100} \times 80\% = 36\%\end{aligned}$$

$$\begin{aligned}\text{Decrease in savings} &= 45\% - 36\% \\ &= 9\%\end{aligned}$$

$$\begin{array}{lcl} 9\% & \rightarrow & \$90 \\ 1\% & \rightarrow & \$10 \end{array}$$

$$\text{Salary at first} \rightarrow 100 \times \$10 = \mathbf{\$1000}$$

Qn 4

$$\begin{aligned}\text{Amount of water left} &\rightarrow 60\% \text{ of } 60\% \\ &\rightarrow \frac{3}{5} \times 60\% = 36\%\end{aligned}$$

$$\begin{aligned}36\% &\rightarrow 72 \text{ litres} \\ 1\% &\rightarrow 2 \text{ litres}\end{aligned}$$

$$\begin{aligned}\text{Volume of water the tank can hold} &\rightarrow 100\% \\ &\rightarrow 100 \times 2 \text{ l} \\ &= \mathbf{200 \text{ l}}\end{aligned}$$

Qn 5

At first

$$\text{Blue} = 80\% \quad \text{Red} = 100\%$$

Qn 5 (Cont.)

In the end

$$\begin{aligned}\text{Blue} &= 110\% \times 80\% \\ &= \frac{110}{100} \times 80\% = 88\%\end{aligned}$$

$$\text{Red} = 100\% - 40\% = 60\%$$

$$\begin{aligned}\text{Difference} &= 28\% \rightarrow 70 \\ 4\% \rightarrow 70 \div 7 &= 10\end{aligned}$$

$$\text{Blue marbles at first} = 80\% \rightarrow 20 \times 10 = \mathbf{200}$$

Qn 6

At first

$$\begin{array}{ll}\text{Muthu} & : \quad 90\% \\ \text{Esther} & : \quad 100\%\end{array}$$

Increase

$$\text{Muthu} : \quad \frac{20}{100} \times 90\% = 18\%$$

Decrease

$$\text{Esther} : \quad 20\%$$

End

$$\begin{array}{ll}\text{Muthu} & : \quad 90\% + 18\% = 108\% \\ \text{Esther} & : \quad 100\% - 20\% = 80\%\end{array}$$

$$\begin{aligned}\text{Difference} \\ 28\% &\rightarrow \$560 \\ 1\% &\rightarrow \$20\end{aligned}$$

$$\begin{aligned}\text{Muthu's salary in the end} &\rightarrow 108\% \\ &\rightarrow 108 \times \$20 = \mathbf{\$2160}\end{aligned}$$

Qn 7

$$\text{Chinese books} = 2 \text{ units}$$

$$\text{English books} = 3 \text{ units}$$

$$\text{Malay books} = 3 \text{ units} \div 2 = 1.5 \text{ units}$$

$$\begin{aligned}\text{Total} &= 6.5 \text{ units} \\ &= 3900\end{aligned}$$

$$1 \text{ unit} = 3900 \div 6.5 = 600$$

$$\begin{aligned}\text{Chinese(original)} &= 2 \times 600 = 1200 \\ \text{Malay (original)} &= 1.5 \times 600 = 900 \\ \text{English original} &= 3 \times 600 = 1800\end{aligned}$$

$$\text{Increase in Chinese} = 20\% \times 1200 = 240$$

$$\text{Increase in Malay} = 10\% \times 900 = 90$$

$$\text{Increase in English} = 510 - 240 - 90 = 180$$

$$\begin{aligned}\text{Percentage increase in English} &= \frac{180}{1800} \times 100\% \\ &= \mathbf{10\%}\end{aligned}$$

Qn 8

$$\begin{aligned}\text{Vernice} &= 3 \text{ units} \\ \text{Nathaniel} &= 4 \text{ units}\end{aligned}$$

$$\text{Increase in Vernice} = 40\% \times 3 \text{ units} = 1.2 \text{ units}$$

Qn 8 (Cont.)

$$\text{Vernice's mass (end)} = 4.2 \text{ units}$$

$$\begin{aligned}\text{Decrease needed for Nathaniel's mass} \\ &= 4.2 \text{ units} - 4 \text{ units} \\ &= 0.2 \text{ units}\end{aligned}$$

$$\begin{aligned}\text{Percentage increase} \\ &= \frac{0.2}{4} \times 100\% \\ &= \mathbf{5\%}\end{aligned}$$

Qn 9

$$\begin{aligned}\text{New length} &= \frac{7}{5} \times 25 \text{ cm} \\ &= 35 \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{New breadth} &= \frac{3}{2} \times 20 \text{ cm} \\ &= 30 \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{New perimeter} &= 35 \text{ cm} + 30 \text{ cm} + 35 \text{ cm} + 30 \text{ cm} \\ &= 130 \text{ cm}\end{aligned}$$

Qn 10

$$\begin{aligned}\text{New length} &= \frac{5}{4} \times 20 \text{ cm} \\ &= 25 \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{New breadth} &= \frac{5}{4} \times 16 \text{ cm} \\ &= 20 \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{New area} &= 25 \text{ cm} \times 20 \text{ cm} \\ &= 500 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Old area} &= 20 \text{ cm} \times 16 \text{ cm} \\ &= 320 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Change in area} &= 500 \text{ cm}^2 - 320 \text{ cm}^2 \\ &= 180 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Percentage increase} &= \frac{5}{4} \times 100\% \\ &= \mathbf{56.25\%}\end{aligned}$$

Qn 11

$$\begin{aligned}\text{Original salary} &= 100\%, \\ \text{Spend} &= 80\%, \\ \text{Saved} &= 20\%\end{aligned}$$

$$\begin{aligned}\text{New salary} &= 80\%, \\ \text{Spend} &= 80\% \times 80\% = 64\% \\ \text{Saved} &= 80\% - 64\% = 16\%\end{aligned}$$

$$\text{Decrease in spending} = 80\% - 64\% = 16\%$$

$$\begin{aligned}16\% \text{ total} &= \$640 \\ 1\% \text{ total} &= \$640 \div 16 = \$40\end{aligned}$$

$$\begin{aligned}\text{April salary} \\ &= 80 \times \$40 \\ &= \mathbf{\$3200}\end{aligned}$$

Qn 12

Original salary = 100%,
Spend = 75%,
Saved = 25%

New salary = 120%,
Spend = $75\% \times 120\% = 90\%$
Saved = $120\% - 90\% = 30\%$

Increase in spending = $90\% - 75\% = 15\%$

15% total = \$450
1% total = $\$450 \div 15 = \30

April salary
= $120 \times \$30$
= **\$3600**

Unit 7.3 – Overlapping Percentage

Qn 1

$100\% - 10\% = 90\%$ (Grade A Math)
 $80\% + 35\% = 115\%$ (Grade B Math)

Percentage of students who chose both grades
 $\rightarrow 115\% - 90\% = 25\%$

25% $\rightarrow 75$
1% $\rightarrow 3$

Total number of students $\rightarrow 100\% \rightarrow 3 \times 100 = \mathbf{300}$

Qn 2

$100\% - 10\% = 90\%$
 $70\% + 45\% = 115\%$

Percentage of children who went for both rides
 $\rightarrow 115\% - 90\% = 25\%$

25% of total $\rightarrow 75$
1% of total $\rightarrow 3$

Total number of children who did not go for either of the two rides $\rightarrow 10\% \rightarrow 3 \times 10 = \mathbf{30}$

Qn 3

$100\% - 5\% = 95\%$
 $65\% + 75\% = 140\%$

Percentage of students who like both table tennis and badminton = $140\% - 95\% = 45\%$

45% $\rightarrow 90$
1% $\rightarrow 2$

Number of students involved $\rightarrow 100\% \rightarrow 100 \times 2 = \mathbf{200}$

Qn 4

$100\% - 16\% = 84\%$
 $82\% + 54\% = 136\%$

Percentage of pupils who do not like any of the 2 sports
= $136\% - 84\%$
= 52%

No. of pupils who enjoyed both swimming and jogging
= $\frac{52}{100} \times 200$
= **104**

Unit 7.4 – GST

Qn 1

$109\% \rightarrow \$523.20$
 $1\% \rightarrow \$523.20 \div 109 = \4.80

$100\% \rightarrow \$4.80 \times 100$
= **\$480**

Qn 2

$9\% \rightarrow \$166.50$
 $1\% \rightarrow \$166.50 \div 9 = \18.50

$100\% \rightarrow \$18.50 \times 100$
= **\$1850**

Qn 3

9% difference $\rightarrow \$45$
1% difference $\rightarrow \$45 \div 9 = \5
100% difference $\rightarrow \$5 \times 100$
= \$500
 $\$2000 - \$500 = \$1500$
 $\$1500 \div 2 = \750

Cost of dryer w/o GST = \$750
Cost of dryer with GST = $109\% \times \$750$
= $\frac{109}{100} \times \$750$
= **\$817.50**

Qn 4

9% difference $\rightarrow \$2.70$
1% difference $\rightarrow \$2.70 \div 9 = \0.30
109% difference $\rightarrow \$0.30 \times 109$
= \$32.70

Cost of pants with GST = $\$85.60 + \32.70
= **\$118.30**

Qn 5

Price of microwave oven = $80\% \times \$2400$
= \$1920

Price after GST = $109\% \times \$1920$
= **\$2092.80**

Qn 6

$109\% \rightarrow \$2616$
 $1\% \rightarrow \$2616 \div 109 = \24

$100\% \rightarrow \$24 \times 100$
= \$2400

$\$2400 \div 4 = \600

Cost of laptop w/o GST = $\$600 \times 3$
= \$1800

Cost of laptop with GST = $109\% \times \$1800$
= $\frac{109}{100} \times \$1800$
= **\$1962**

Unit 7.5 – Simple Interest

Qn 1

$$\begin{aligned}\text{Interest} &= \frac{1.5}{100} \times \$30000 \times 4 \frac{3}{4} \\ &= \$2137.50\end{aligned}$$

$$\begin{aligned}\text{Total amount} &= \$2137.50 + \$30\,000 \\ &= \mathbf{\$32\,137.50}\end{aligned}$$

Qn 2

$$\begin{aligned}\text{Simple interest for a year} &= \$1440 \div 4 \\ &= \$360\end{aligned}$$

$$\begin{aligned}\text{Original sum} &= \frac{100}{2.4} \times \$360 \\ &= \mathbf{\$15\,000}\end{aligned}$$

Qn 3

$$\begin{aligned}\text{Interest for 4 years} &\rightarrow \frac{3.5}{100} \times \$30000 \times 4 = \$4200 \\ \text{Total owed to the bank} &\rightarrow \$4200 + \$30\,000 = \mathbf{\$34\,200}\end{aligned}$$

Qn 4

$$\begin{aligned}(\text{Interest for 3 years}) &\rightarrow 12\% \\ 12\% &\rightarrow \$40\,320 \\ 1\% &\rightarrow \$40\,320 \div 12 = \$3360\end{aligned}$$

$$(\text{Principal amount}) 100\% \rightarrow \$3360 \times 100 = \mathbf{\$336\,000}$$

Qn 5

$$\begin{aligned}(\text{a}) 2\% &\rightarrow \$72 \\ 1\% &\rightarrow \$72 \div 2 = \$36 \\ 100\% &\rightarrow \$36 \times 100 = \mathbf{\$3600}\end{aligned}$$

$$(\text{b}) \text{ Total sum after 4 years} \rightarrow \$3600 + \$72 \times 4 = \mathbf{\$3888}$$

Qn 6

$$\begin{aligned}\text{Total amount owed (Mr Krishnan)} &\rightarrow 100\% + 3.5 \times 4 = \\ &114\%\end{aligned}$$

$$\text{Total amount owed (Mr Lim)} \rightarrow 100\% + 3\% \times 4 = 112\%$$

$$\text{Difference} \rightarrow 114\% - 112\% = 2\%$$

$$\text{Amount each borrowed} \rightarrow \frac{100}{2} \times \$250 = \mathbf{\$12\,500}$$

Unit 7.6 – Discount and Percentage Discount

Qn 1

$$\begin{aligned}\text{Discounted price of 1 torch} &= \$200 \div 25 \\ &= \$8\end{aligned}$$

$$\begin{aligned}\text{Original price of 1 torch} &= \frac{100}{80} \times \$8 \\ &= \mathbf{\$10}\end{aligned}$$

Qn 2

$$\begin{aligned}\text{Usual price of wallet} &= \frac{100}{80} \times \$144 \\ &= \$180\end{aligned}$$

$$\begin{aligned}\text{Discount given to wallet} &= \$180 - \$144 \\ &= \$36\end{aligned}$$

$$\begin{aligned}\text{Discount given to handbag} &= \$78 - \$36 \\ &= \$42\end{aligned}$$

$$\begin{aligned}\text{Original price of handbag} &= \$42 + \$238 \\ &= \$280\end{aligned}$$

Qn 2 (Cont.)

$$\begin{aligned}\text{Percentage discount for the handbag} &= \frac{42}{280} \times 100\% \\ &= \mathbf{15\%}\end{aligned}$$

Qn 3

$$109\% \rightarrow \$274.68$$

$$1\% \rightarrow \$274.68 \div 109 = \$2.52$$

$$100\% \rightarrow \$2.52 \times 100 = \$252$$

$$90\% \text{ of original bill} \rightarrow 252$$

$$\begin{aligned}10\% \text{ of original bill} &\rightarrow \$252 \div 9 \\ &= \$28\end{aligned}$$

$$\begin{aligned}100\% \text{ of original bill} &= \$28 \times 10 \\ &= \mathbf{\$280}\end{aligned}$$

Qn 4

$$100\% \text{ of usual price} = \$150$$

$$\begin{aligned}1\% \text{ of usual price} &= \$150 \div 100 \\ &= \$1.50\end{aligned}$$

$$\begin{aligned}90\% \text{ of usual price} &= 90 \times \$1.50 \\ &= \$135\end{aligned}$$

$$100\% \text{ of discounted price} = \$135$$

$$\begin{aligned}1\% \text{ of discounted price} &= \$135 \div 100 \\ &= \$1.35\end{aligned}$$

$$\begin{aligned}95\% \text{ of discounted price} &= 95 \times \$1.35 \\ &= \mathbf{\$128.25}\end{aligned}$$

Qn 5

$$\begin{aligned}\text{Discounted price of 1 muffin} &= \$10 \div 5 \\ &= \$2\end{aligned}$$

$$\begin{aligned}\text{Original price of 1 muffin} &= \frac{100}{80} \times \$2 \\ &= \mathbf{\$2.50}\end{aligned}$$

Qn 6

At first,
Sells at 10% discount \rightarrow sell at 90% of the usual selling price

Sells at 30% discount \rightarrow sell at 70% of the usual selling price

$$\begin{aligned}\text{Difference in the selling price} &\rightarrow 20\% \text{ of selling price} \\ &= \$30 + \$10\end{aligned}$$

$$\begin{aligned}20\% \text{ of selling price} &\rightarrow \$40 \\ 1\% \text{ of selling price} &\rightarrow \$2\end{aligned}$$

$$\begin{aligned}\text{Cost price of watch} &\rightarrow 90 \times 2 - 30 \text{ or } 70 \times 2 + 10 = \$150 \\ \$150 + \$100 &= \mathbf{\$250}\end{aligned}$$

Unit 7.7 – Equal Fractions

Qn 1

$$45\% \text{ of Calvin's stickers} = 25\% \text{ of Brian's stickers}$$

$$\frac{9}{20} \text{ of Calvin's stickers} = \frac{1}{4} \text{ of Brian's stickers}$$

$$\frac{9}{20} \text{ of Calvin's stickers} = \frac{9}{36} \text{ of Brian's stickers}$$

Qn 1 (Cont.)

$$\begin{aligned}\text{Calvin} &= 20 \text{ units} \\ \text{Brian} &= 36 \text{ units} \\ \text{Difference} &= 16 \text{ units} \\ &= 32 \\ 1 \text{ unit} &= 2 \\ \text{Total number of stickers} &= 56 \times 2 \\ &= \mathbf{112}\end{aligned}$$

Qn 2

$$\begin{aligned}35\% \text{ of Joanna} &= 60\% \text{ of Kelvin} \\ \frac{7}{20} \text{ of Joanna} &= \frac{3}{5} \text{ of Kelvin} \\ \frac{21}{60} \text{ of Joanna} &= \frac{21}{35} \text{ of Kelvin}\end{aligned}$$

$$\begin{aligned}\text{Joanna} &= 60 \text{ units} \\ \text{Kelvin} &= 35 \text{ units} \\ \text{Difference} &= 25 \text{ units} \\ &= 125 \\ 1 \text{ unit} &= \$125 \div 5 \\ &= \$25 \\ \text{Amount of money Joanna had at first} \\ &= 60 \times \$25 \\ &= \mathbf{\$1500}\end{aligned}$$

Qn 3

$$\begin{aligned}40\% \text{ of boys} &= 10\% \text{ of girls} \\ \frac{2}{5} \text{ of boys} &= \frac{1}{10} \text{ of girls} \\ \frac{2}{5} \text{ of boys} &= \frac{2}{20} \text{ of girls}\end{aligned}$$

$$\begin{aligned}\text{Boys} &= 5 \text{ units} \\ \text{Girls} &= 20 \text{ units} \\ \text{Difference} &= 15 \text{ units}\end{aligned}$$

$$\begin{aligned}15 \text{ units} &= 510 \\ 1 \text{ unit} &= 34\end{aligned}$$

$$\begin{aligned}\text{Total students in the end} &= 4 \times 34 \\ &= \mathbf{136}\end{aligned}$$

Qn 4

Twice of Rahim's money left = Carena's money left
 $2 \times 10\%$ of Rahim's money = 40% of Carena's money

20% of Rahim's money = 40% Carena's money

$$\frac{1}{5} \text{ of Rahim's money} = \frac{2}{5} \text{ of Carena's money}$$

$$\frac{2}{10} \text{ of Rahim's money} = \frac{2}{5} \text{ of Carena's money}$$

$$\begin{aligned}\text{Rahim's money} &= 10 \text{ units} \\ \text{Carena's money} &= 5 \text{ units} \\ \text{Difference} &= 5 \text{ units}\end{aligned}$$

$$\begin{aligned}5 \text{ units} &= \$85 \\ 1 \text{ unit} &= \$85 \div 5 \\ &= \$17 \\ \text{Rahim at first} &= 10 \times \$17 \\ &= \mathbf{\$170}\end{aligned}$$

Qn 5

Chocolate left is equal to twice cheese left

$$20\% \text{ chocolate} = 2 \times 25\% \text{ cheese}$$

$$20\% \text{ chocolate} = 50\% \text{ cheese}$$

$$\frac{1}{5} \text{ chocolate} = \frac{1}{2} \text{ cheese}$$

$$\begin{aligned}\text{Total} &= 7 \text{ units} \\ 7 \text{ units} &= 350 \\ 1 \text{ unit} &= 50\end{aligned}$$

$$\begin{aligned}\text{Total chocolate muffins given away} \\ &= 4 \times 50 \\ &= \mathbf{200}\end{aligned}$$

Qn 6

The number of girls left is twice the number of boys left.

$$70\% \text{ of girls} = 2 \times 20\% \text{ of boys}$$

$$70\% \text{ of girls} = 40\% \text{ of boys}$$

$$\frac{7}{10} \text{ of girls} = \frac{2}{5} \text{ of boys}$$

$$\frac{14}{20} \text{ of girls} = \frac{14}{35} \text{ of boys}$$

$$\begin{aligned}\text{Boys} &= 35 \text{ units} \\ \text{Girls} &= 20 \text{ units} \\ \text{Difference} &= 15 \text{ units}\end{aligned}$$

$$\begin{aligned}15 \text{ units} &= 90 \\ 1 \text{ unit} &= 90 \div 15 \\ &= 6\end{aligned}$$

$$\begin{aligned}\text{Total students} &= 35 \text{ units} + 20 \text{ units} \\ &= 55 \text{ units}\end{aligned}$$

$$\begin{aligned}55 \text{ units} &= 55 \times 6 \\ &= \mathbf{330}\end{aligned}$$

Unit 7.8 – External Unchanged

Qn 1

At first

$$\begin{aligned}\text{Boys} &: 60\% (3 \text{ units}) \times 7 & (21 \text{ units}) \\ \text{Girls} &: 40\% (2 \text{ units}) \times 7 & (14 \text{ units})\end{aligned}$$

End

$$\begin{aligned}\text{Boys} &: 70\% (7 \text{ units}) \times 3 & (21 \text{ units}) \\ \text{Girls} &: 30\% (3 \text{ units}) \times 3 & (9 \text{ units})\end{aligned}$$

$$\text{Decrease} = 5 \text{ units}$$

$$5 \text{ units} = 5$$

$$1 \text{ unit} = 1$$

$$\begin{aligned}\text{Total number of students in the end} &= 30 \times 1 \\ &= \mathbf{30}\end{aligned}$$

Qn 2

At first

$$\begin{aligned}\text{Children} &: 40\% (2 \text{ units}) \times 3 & (6 \text{ units}) \\ \text{Adults} &: 100\% (5 \text{ units}) \times 3 & (15 \text{ units})\end{aligned}$$

End

$$\begin{aligned}\text{Children} &: 60\% (3 \text{ units}) \times 2 & (6 \text{ units}) \\ \text{Adults} &: 40\% (2 \text{ units}) \times 2 & (4 \text{ units})\end{aligned}$$

Qn 2 (Cont.)

$$\begin{aligned}\text{Decrease in adults} &= 11 \text{ units} \\ 11 \text{ units} &= 22 \\ 1 \text{ unit} &= 2 \\ \text{Total children in the bus} &= 6 \times 2 \\ &= 12\end{aligned}$$

Qn 3

At first

$$\begin{aligned}\text{Lemons} &: 30\% (3 \text{ units}) \\ \text{Others} &: 70\% (7 \text{ units})\end{aligned}$$

End

$$\begin{aligned}\text{Lemons} &: 50\% (1 \text{ unit}) \times 7 \quad (7 \text{ units}) \\ \text{Others} &: 50\% (1 \text{ unit}) \times 7 \quad (7 \text{ units})\end{aligned}$$

$$\begin{aligned}\text{Increase} &= 4 \text{ units} \\ 4 \text{ units} &= 40 \\ 1 \text{ unit} &= 40 \div 4 \\ &= 10\end{aligned}$$

$$\begin{aligned}\text{Number of lemons at first} &= 3 \times 10 \\ &= 30\end{aligned}$$

Qn 4

At first

$$\begin{aligned}\text{Girls} &: 40\% (2 \text{ units}) \times 3 \quad (6 \text{ units}) \\ \text{Boys} &: 60\% (3 \text{ units}) \times 3 \quad (9 \text{ units})\end{aligned}$$

End

$$\begin{aligned}\text{Girls} &: 55\% (11 \text{ units}) \\ \text{Boys} &: 45\% (9 \text{ units})\end{aligned}$$

$$\begin{aligned}\text{Increase in girls} &= 5 \text{ units} \\ 5 \text{ units} &= 20 \\ 1 \text{ unit} &= 4 \\ \text{No. of boys at telematch} &= 9 \times 4 \\ &= 36\end{aligned}$$

Units 7.9 – Repeated Identity

Qn 1

$$\begin{aligned}\text{Arun} &= 80\% \\ \text{Ramesh} &= 100\% \\ \text{Arun} &= 40\% = 80\% \\ \text{Jody} &= 100\% = 200\%\end{aligned}$$

$$\begin{aligned}\text{Total} &= 80\% + 100\% + 200\% = 380\% \\ 380\% &\rightarrow 285 \\ 20\% &\rightarrow 285 \div 19 = 15 \\ \text{Jody} &\rightarrow 200\% \rightarrow 15 \times 10 = 150\end{aligned}$$

Qn 2

$$\begin{aligned}\text{David} &= 90\% = 9u \times 4 \\ &= 36u\end{aligned}$$

$$\begin{aligned}\text{Ian} &= 100\% = 10u \times 4 \\ &= 40u\end{aligned}$$

$$\begin{aligned}\text{Rauf} &= 75\% = 3u \times 9 \\ &= 27u\end{aligned}$$

$$\begin{aligned}\text{David} &= 100\% = 4u \times 9 \\ &= 36u\end{aligned}$$

$$\begin{aligned}\text{Total} &= 36u + 40u + 27u \\ &= 103u\end{aligned}$$

$$\begin{aligned}103u &= 515 \\ 1u &= 515 \div 103 = 5\end{aligned}$$

$$\text{Ian} = 40 \times 5 = 200 \text{ cookies}$$

Qn 3

$$\begin{aligned}\text{Helen} &= 80\% = 4u \times 5 = 20u \\ \text{Fiona} &= 100\% = 5u \times 5 = 25u \\ \text{Daniel} &= 90\% = 9u \times 2 = 18u \\ \text{Helen} &= 100\% = 10u \times 2 = 20u\end{aligned}$$

$$\text{Difference between Daniel and Fiona} = 7u = 28$$

$$1u = 28 \div 7 = 4$$

$$\begin{aligned}\text{Fiona's score} &= 25 \times 4 \\ &= 100 \text{ marks}\end{aligned}$$

Qn 4

$$\begin{aligned}\text{Boys} &= 40\% \\ \text{Girls} &= 100\% \\ \text{Adults} &= 6 \text{ units} \\ \text{Children} &= 5 \text{ units}\end{aligned}$$

$$\begin{aligned}\text{Since } 5u &\rightarrow 140\% \\ 1u &= 140\% \div 5 = 28\%\end{aligned}$$

$$\text{Adults} = 6 \times 28\% = 168\%$$

$$\begin{aligned}\text{Difference between adults and girls} \\ &= 168\% - 100\% = 68\%\end{aligned}$$

$$\begin{aligned}68\% &\rightarrow 34 \\ 2\% &\rightarrow 1\end{aligned}$$

$$\text{Total at party} = 308\% \rightarrow 154 \times 1 = 154 \text{ people.}$$

Qn 5

$$\begin{aligned}\text{Red} &= 75\% = 3u \times 5 = 15u \\ \text{Blue} &= 100\% = 4u \times 5 = 20u \\ \text{Green} &= 80\% = 4u \times 3 = 12u \\ \text{Red} &= 100\% = 5u \times 3 = 15u\end{aligned}$$

$$\text{Difference between blue and green marbles} = 8u = 32$$

$$1u = 32 \div 8 = 4$$

$$\text{Total marbles} = 47 \times 4 = 188$$

Qn 6

$$\begin{aligned}\text{Shop A} &= 70\% = 7u \times 2 = 14u \\ \text{Shop B} &= 100\% = 10u \times 2 = 20u \\ \text{Shop B} &= 80\% = 4u \times 5 = 20u \\ \text{Shop C} &= 100\% = 5u \times 5 = 25u\end{aligned}$$

$$\begin{aligned}\text{Total} &= 59u = 295 \\ 1u &= 295 \div 59 = 5\end{aligned}$$

$$\begin{aligned}\text{Difference between Shop C and Shop A} \\ &= 5 \times 11 \\ &= 55\end{aligned}$$

Qn 7

$$\text{Yvonne} = 60\%, \text{ Lynette} = 100\%, \text{ Tania} = 30\%$$

$$\begin{aligned}\text{Yvonne gave } 20\% \times 60\% &= 12\% \text{ to Tania,} \\ \text{and left } 60\% - 12\% &= 48\%\end{aligned}$$

$$\begin{aligned}\text{Lynette gave } 40\% \text{ to Tania, and left } 60\% \\ \text{Increase in Tania} &= 12\% + 40\% = 52\%\end{aligned}$$

$$\begin{aligned}\text{Tania at first} &= 52\% \\ \text{Tania in the end} &= 104\%\end{aligned}$$

Qn 7 (Cont.)
 Difference between Tania and Yvonne in the end = $104\% - 48\% = 56\%$

$56\% \rightarrow 280$
 $1\% \rightarrow 280 \div 56 = 5$

Yvonne gave to Tania = $12 \times 5 = 60$

Unit 7.10 – Unchanged Total

Qn 1

At first
 Adults 70% = $7u \times 3 = 21u$
 Children 30% = $3u \times 3 = 9u$

End
 Adults 50% = $1u \times 10 = 10u$
 Children 100% = $2u \times 10 = 20u$

Decrease in adults
 = $11u$
 = 88

$1u = 8$

Adults in the end = $10 \times 8 = 80$

Qn 2

1st day
 Fixed : 45% (9 units)
 Unfixed : 55% (11 units)

2nd day
 Fixed : $75\% (3 \text{ units}) \times 5 = 15 \text{ units}$
 Unfixed : $25\% (1 \text{ unit}) \times 5 = 5 \text{ units}$

Transfer = 6 units
 6 units = 60
 1 unit = 10

Total pieces in puzzle = 20 units
 = 20×10
 = **200**

Qn 3

1st day
 Fixed : $20\% (1 \text{ unit}) \times 9 = 9 \text{ units}$
 Unfixed : $80\% (4 \text{ units}) \times 9 = 36 \text{ units}$
 Total 45 units

2nd day
 Fixed : $80\% (4 \text{ units}) \times 5 = 20 \text{ units}$
 Unfixed : $100\% (5 \text{ units}) \times 5 = 25 \text{ units}$
 Total 45 units

Transfer = 20 units – 9 units
 = 11 units

11 units = 44
 1 unit = $44 \div 11$
 = 4

Total number of pieces in the puzzle = 45×4
 = **180**

Qn 4

Read : 40% (2 units)
 Unread : 60% (3 units)
 Total 5 units

Qn 4 (Cont.)

Read : 80% (4 unit)
 Unread : 20% (1 unit)
 Total 5 units

Transfer = 4 units – 2 units
 = 2 units
 2 units = 60
 1 unit = $60 \div 2$
 = 30

Total number of pages = 5×30
 = **150**

Qn 5

Read : 40% (2 units) $\times 5 = 10 \text{ units}$
 Unread : 100% (5 units) $\times 5 = 25 \text{ units}$

Read : 60% (3 unit) $\times 7 = 21 \text{ units}$
 Unread : 40% (2 unit) $\times 7 = 14 \text{ units}$

Transfer = 11 units

11 units = 22
 1 unit = 2
 Total pages = 35×2
 = **70**

Qn 6

Cherie = 50% = 1 unit $\times 13 = 13 \text{ units}$
 Daniel + Elias = 100% = 2 units $\times 13 = 26 \text{ units}$

Total = 3 units $\times 13 = 39 \text{ units}$

Daniel = 30% = 3 units $\times 3 = 9 \text{ units}$
 Cherie + Elias = 100% = 10 units $\times 3 = 30 \text{ units}$

Total = 13 units $\times 3 = 39 \text{ units}$

Since the cost of the present remains the same, we find the LCM of 3 and 13, which is 39.

Daniel = 9 units
 Elias = 30 units – 13 units = 17 units

Difference between Elias and Daniel = 17 units – 9 units = 8 units

8 units = \$32
 1 unit = $\$32 \div 8 = \4

Cost of present = $39 \times \$4 = \156

Qn 7

Gerald = 45% = 9 units
 Xavier + Joshua = 55% = 11 units

Total = 20 units

Xavier = 25% = 1 unit $\times 4 = 4 \text{ units}$
 Gerald + Joshua = 100% = 4 units $\times 4 = 16 \text{ units}$

Total = 5 units $\times 4 = 20 \text{ units}$

Since the total number of cookies remains the same, we find the LCM of 5 and 20, which is 20.

Qn 7 (Cont.)
 Xavier = 4 units
 Gerald = 9 units

Difference between Xavier and Gerald = 9 units – 4 units = 5 units

5 units = 25 cookies
 1 unit = $\$25 \div 5 = 5$ cookies

Total cookies = $20 \times 5 = 100$

Unit 7.11 – Constant Difference

Qn 1

Boys : 30% (3 units)
 Girls : 70% (7 units)
 Difference 4 units

Boys : 60% (3 units) $\times 2 = 6$ units
 Girls : 100% (5 units) $\times 2 = 10$ units
 Difference 2 units $\times 2 = 4$ units

Increase each = 6 units – 3 units
 = 3 units

3 units = 9
 1 unit = $9 \div 3 = 3$

Total number of students in the end = 16 units
 = $16 \times 3 = 48$

Qn 2

Alan : 75% (3 units) $\times 3 = 9$ units
 Kumar : 100% (4 units) $\times 3 = 12$ units
 Difference = 1 unit $\times 3 = 3$ units

Alan : 25% (1 unit)
 Kumar : 100% (4 units)
 Difference = 3 units

Decrease each = 9 units – 1 unit
 = 8 units

8 units = \$400
 1 unit = $\$400 \div 8 = \50

Amount of money Alan had at first = $9 \times \$50 = \450

Qn 3

School X = 1680
 School Y = $20\% \times 1680 + 1680 = 2016$
 Difference = $2016 - 1680 = 336$

Since an equal number of students left each school, difference remains the same,

School X (end) = 60%
 School Y (end) = 100%

Difference = 40% $\rightarrow 336$
 10% $\rightarrow 336 \div 4 = 84$

School X (end) = $84 \times 6 = 504$

Qn 4

At first

Shop X : 4 units $\times 3 = 12$ units
 Shop Y : 7 units $\times 3 = 21$ units
 Difference 3 units $\times 3 = 9$ units

Qn 4 (Cont.)

Shop X : 55% (11 units)
 Shop Y : 100% (20 units)
 Difference 9 units

Decrease each = 12 units – 11 units
 = 1 unit

1 unit = 75

Number of shirts Shop X had in the end = $11 \times 75 = 825$

Qn 5

Small Square : 40% (2 units) $\times 2 = 4$ units
 Big Square : 100% (5 units) $\times 2 = 10$ units
 Difference 3 units $\times 2 = 6$ units

Unshaded small: 1 unit $\times 3 = 3$ units
 Unshaded big : 3 units $\times 3 = 9$ units
 Difference 2 units $\times 3 = 6$ units

Decrease each = 1 unit
 1 unit = 20 cm²
 Area (small square) = $4 \times 20 \text{ cm}^2 = 80 \text{ cm}^2$

Qn 6

Alexander : 40% (2 units)
 Brother : 100% (5 units)
 Difference 3 units

Alexander : 75% (3 units) $\times 3 = 9$ units
 Brother : 100% (4 unit) $\times 3 = 12$ units
 Difference 1 unit $\times 3 = 3$ units

Increase each = 9 units – 2 units
 = 7 units

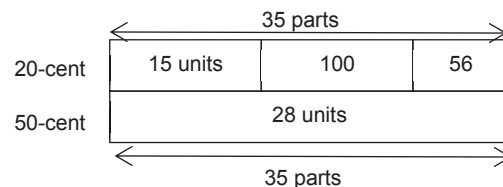
7 units = 21
 1 unit = $21 \div 7 = 3$

Alexander's age now = $2 \times 3 = 6$

Unit 7.12 – External Changed

Qn 1

$\times 5 \left\{ \begin{array}{ll} 20\text{c coins} & 50\text{c coins} \\ 75\% (3 \text{ units}) & 100\% (4 \text{ units}) \\ + 20 & - 8 \\ \hline 60\% (7 \text{ parts}) & 40\% (5 \text{ parts}) \end{array} \right. \times 7$



13 units = 156 coins
 1 unit = $156 \div 13 = 12$ coins

Sum of money at first = $\$0.20 \times 3 \times 12 + \$0.50 \times 4 \times 12 = \31.20

Qn 2

$$\begin{array}{r} \text{Elias} \\ \times 4 \left\{ \begin{array}{l} 45\% (9 \text{ units}) \\ +39 \\ \hline 4 \times 75\% (3p) \end{array} \right. \quad \text{Ramesh} \\ \left\{ \begin{array}{l} 100\% (20 \text{ units}) \\ +20 \\ \hline 100\% (4p) \times 3 \end{array} \right\} \times 3 \end{array}$$

Elias	36 units	156
Ramesh	60 units	60

$$\begin{array}{l} 24 \text{ units} = 96 \\ 1 \text{ unit} = 4 \end{array}$$

$$\begin{array}{l} \text{Total Elias at first} = 9 \times 4 \\ = 36 \end{array}$$

Qn 3

Last year : 90% → 9 units 100% → 10 units
In the end : 70% → 7 parts 100% → 10 parts

$$\begin{array}{r} \text{School X} \quad \text{School Y} \quad \text{School X} \quad \text{School Y} \\ \times 10 \left\{ \begin{array}{l} 9 \text{ units} \\ -220 \\ \hline 7 \text{ parts} \end{array} \right. \quad \left\{ \begin{array}{l} 10 \text{ units} \\ +200 \\ \hline 10 \text{ parts} \end{array} \right\} \times 7 \quad \left\{ \begin{array}{l} 90 \text{ units} \\ -2200 \\ \hline 70 \text{ parts} \end{array} \right. \quad \left\{ \begin{array}{l} 70 \text{ units} \\ +1400 \\ \hline 70 \text{ parts} \end{array} \right\} \end{array}$$

70 parts

School X	90 units
School Y	70 units 1400 2200
	20 units

$$\begin{array}{l} 20 \text{ units} = 1400 + 2200 \\ = 3600 \\ 1 \text{ unit} = 3600 \div 20 \\ = 180 \end{array}$$

$$\begin{array}{l} \text{Number of students who enrolled into School X last year} \\ = 9 \times 180 \\ = 1620 \end{array}$$

$$\begin{array}{l} \text{Number of students who enrolled into School Y last year} \\ = 10 \times 180 \\ = 1800 \end{array}$$

Qn 4

75% → 3 units 100% → 4 units

$$\times 8 \left\{ \begin{array}{l} \text{Daniel} \\ 3 \text{ units} \\ +\$20 \\ \hline 5 \text{ parts} \end{array} \right. \quad \left\{ \begin{array}{l} \text{Annabel} \\ 4 \text{ units} \\ +\$40 \\ \hline 8 \text{ parts} \end{array} \right\} \times 5 \quad \left\{ \begin{array}{l} \text{Daniel} \\ 24 \text{ units} \\ +\$160 \\ \hline 40 \text{ parts} \end{array} \right. \quad \left\{ \begin{array}{l} \text{Annabel} \\ 20 \text{ units} \\ +\$200 \\ \hline 40 \text{ parts} \end{array} \right\}$$

Daniel	24 units	\$160
Annabel	20 units	\$200

$$4 \text{ units} = \$40$$

$$\begin{array}{l} 1 \text{ unit} = \$40 \div 4 \\ = \$10 \end{array}$$

$$\begin{array}{l} \text{Daniel's savings at first} = 3 \times \$10 \\ = \$30 \end{array}$$

Qn 5

$$\begin{array}{r} \text{Chickens} \quad \text{Ducks} \\ \times 4 \left\{ \begin{array}{l} 5 \text{ units} \\ -50 \\ \hline 4 \times (25\%) 1p \end{array} \right. \quad \left\{ \begin{array}{l} 8 \text{ units} \\ -8 \\ \hline 4p (100\%) \end{array} \right. \end{array}$$

Chickens	20 units	8
Ducks	8 units	200

$$\begin{array}{l} 12 \text{ units} = 192 \\ 1 \text{ unit} = 16 \\ \text{Ducks at first} = 8 \times 16 \\ = 128 \end{array}$$

Qn 6

May : 90% → 9 units 100% → 10 units
June : 80% → 4 parts 100% → 5 parts

$$\times 5 \left\{ \begin{array}{l} \text{Mrs Tan} \\ 9 \text{ units} \\ +\$400 \\ \hline 4 \text{ parts} \end{array} \right. \quad \left\{ \begin{array}{l} \text{Mrs Ismal} \\ 10 \text{ units} \\ +\$600 \\ \hline 5 \text{ parts} \end{array} \right\} \times 4 \quad \left\{ \begin{array}{l} \text{Mrs Tan} \\ 45 \text{ units} \\ +\$2000 \\ \hline 20 \text{ parts} \end{array} \right. \quad \left\{ \begin{array}{l} \text{Mrs Ismal} \\ 40 \text{ units} \\ +\$2400 \\ \hline 20 \text{ parts} \end{array} \right\}$$

Mrs Tan	45 units	\$2000
Mrs Ismal	40 units	\$2400

$$\begin{array}{l} 5 \text{ units} = \$400 \\ 1 \text{ unit} = \$400 \div 5 \\ = \$80 \end{array}$$

$$\begin{array}{l} \text{Mrs Tan's salary in May} = 9 \times \$80 \\ = \$720 \end{array}$$

Chapter 8 Volume

Unit 8.1 – Finding Volume of a Cuboid with Given Dimension

Qn 1

$$\begin{array}{l} \text{Volume of cuboid} = L \times B \times H \\ = 9 \text{ cm} \times 5 \text{ cm} \times 6 \text{ cm} \\ = 270 \text{ cm}^3 \end{array}$$

Qn 2

$$\begin{array}{l} \text{Volume of cuboid} = L \times B \times H \\ = 5 \text{ cm} \times 4 \text{ cm} \times 12 \text{ cm} \\ = 240 \text{ cm}^3 \end{array}$$

Qn 3

$$\begin{array}{l} \text{Capacity of tank} = L \times B \times H \\ = 30 \text{ cm} \times 20 \text{ cm} \times 12 \text{ cm} \\ = 7200 \text{ cm}^3 \end{array}$$

Qn 4

$$\begin{array}{l} \text{Volume of water} = L \times B \times H \\ = 40 \text{ cm} \times 25 \text{ cm} \times 10 \text{ cm} \\ = 10\,000 \text{ cm}^3 \end{array}$$

Qn 5

$$\begin{array}{l} \text{Volume of water} = L \times B \times H \\ = 20 \text{ cm} \times 20 \text{ cm} \times 25 \text{ cm} \\ = 10\,000 \text{ cm}^3 \end{array}$$

Qn 6

$$\begin{aligned}\text{Volume of water} &= L \times B \times H \\ &= \frac{3}{5} \times 12 \text{ cm} \times 12 \text{ cm} \times 20 \text{ cm} \\ &= \mathbf{1728 \text{ cm}^3}\end{aligned}$$

Qn 7

$$\begin{aligned}\text{Volume of water} &= L \times B \times H \\ &= \frac{2}{3} \times 18 \text{ cm} \times 18 \text{ cm} \times 24 \text{ cm} \\ &= \mathbf{5184 \text{ cm}^3}\end{aligned}$$

Qn 8

$$\begin{aligned}\frac{2}{3} \text{ of tank} &= 3600 \text{ ml} \\ \frac{1}{3} \text{ of tank} &= 1800 \text{ ml} \\ \text{Volume of water the tank can hold} &= 1800 \text{ cm}^3 \times 3 \\ &= \mathbf{5400 \text{ cm}^3}\end{aligned}$$

Qn 9

$$\begin{aligned}\frac{3}{4} \text{ of tank} &= 1500 \text{ cm}^3 \\ \frac{1}{4} \text{ of tank} &= 500 \text{ cm}^3 \\ \text{Full tank} &= 500 \text{ cm}^3 \times 4 \\ &= \mathbf{2000 \text{ cm}^3}\end{aligned}$$

Qn 10

Height = 4 units, width = 1 unit, length = 2 units

$$\begin{aligned}4 \text{ units} &= 20 \text{ cm} \\ 1 \text{ unit} &= 5 \text{ cm} \\ \text{Height} &= 20 \text{ cm} \\ \text{Width} &= 5 \text{ cm} \\ \text{Length} &= 2 \times 5 \text{ cm} \\ &= 10 \text{ cm} \\ \text{Volume} &= L \times B \times H \\ &= 10 \text{ cm} \times 5 \text{ cm} \times 20 \text{ cm} \\ &= \mathbf{1000 \text{ cm}^3}\end{aligned}$$

Qn 11

$$\begin{aligned}\text{Breadth} &= \frac{1}{4} \times 200 \text{ cm} \\ &= 50 \text{ cm} \\ \text{Height} &= \frac{1}{2} \times 50 \text{ cm} \\ &= 25 \text{ cm} \\ \text{Capacity of tank} &= L \times B \times H \\ &= 220 \text{ cm} \times 50 \text{ cm} \times 25 \text{ cm} \\ &= 250\,000 \text{ cm}^3 \\ &= \mathbf{250 \text{ litres}}\end{aligned}$$

Qn 12

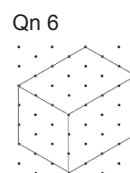
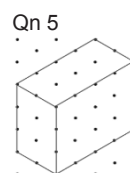
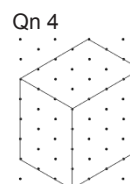
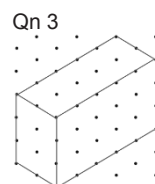
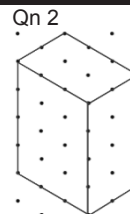
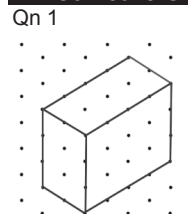
Since width \times height = 36 cm^2 ($6 \text{ cm} \times 6 \text{ cm}$)

$$\begin{aligned}\text{Width} &= \text{Height} \\ &= 6 \text{ cm} \\ \text{Length} &= 2 \times 6 \text{ cm} \\ &= 12 \text{ cm}\end{aligned}$$

Qn 12 (Cont.)

$$\begin{aligned}\text{Volume of cuboid} &= L \times B \times H \\ &= 12 \text{ cm} \times 6 \text{ cm} \times 6 \text{ cm} \\ &= \mathbf{432 \text{ cm}^3}\end{aligned}$$

Unit 8.2 – Drawing Cubes and Cuboids on Isometric Grids



Unit 8.3 – Finding Dimension with Given Volume

Qn 1

$$\begin{aligned}\frac{2}{3} \text{ of tank} &= 8400 \text{ cm}^3 \\ \frac{1}{3} \text{ of tank} &= 4200 \text{ cm}^3 \\ \text{Full Tank} &= 4200 \text{ cm}^3 \times 3 \\ &= 12\,600 \text{ cm}^3 \\ \text{Base area} &= \frac{\text{Volume}}{\text{Height}} \\ &= \frac{12\,600 \text{ cm}^3}{21 \text{ cm}} \\ &= \mathbf{600 \text{ cm}^2}\end{aligned}$$

Qn 2

Since volume = $L \times B \times H$

(a) Length = $\frac{\text{Volume}}{B \times H}$

$$\begin{aligned}&= \frac{135 \text{ cm}^3}{6 \text{ cm} \times 5 \text{ cm}} \\ &= \mathbf{4.5 \text{ cm}}\end{aligned}$$

(b) Length = $\frac{\text{Volume}}{\text{Area}}$

$$\begin{aligned}&= \frac{288 \text{ cm}^3}{72 \text{ cm}^2} \\ &= \mathbf{4 \text{ cm}}\end{aligned}$$

Qn 3

$$\text{Height} = \frac{\text{Volume}}{\text{Base area}}$$

$$= \frac{1430 \text{ cm}^3}{130 \text{ cm}^2}$$

$$= 11 \text{ cm}$$

Qn 4

$$\text{Base area} = \frac{\text{Volume}}{\text{Height}}$$

$$= \frac{1920 \text{ cm}^3}{8 \text{ cm}}$$

$$= 240 \text{ cm}^2$$

Since length \times breadth $\rightarrow 5 \text{ units} \times 3 \text{ units} = 240 \text{ cm}^2$

$$1 \text{ unit} \times 1 \text{ unit} \rightarrow 240 \text{ cm}^2 \div 15 = 16 \text{ cm}^2$$

$$16 \text{ cm}^2 = 4 \text{ cm} \times 4 \text{ cm}$$

$$1 \text{ unit} = 4 \text{ cm}$$

$$\text{Length} = 5 \times 4 \text{ cm}$$

$$= 20 \text{ cm}$$

Qn 5

$$\text{Volume of water} = L \times B \times H$$

$$2880 \text{ cm}^3 = 3 \text{ units} \times 3 \text{ units} \times 5 \text{ units}$$

Therefore $1 \text{ unit} \times 1 \text{ unit} \times 1 \text{ unit}$

$$= \frac{2880}{3 \times 3 \times 5}$$

$$= \frac{2880}{45}$$

$$= 64 \text{ cm}^3$$

$$1 \text{ unit} = 4 \text{ cm}$$

$$\text{Since } (4 \times 4 \times 4) = 64$$

$$\text{Area of base} = 3 \text{ units} \times 3 \text{ units}$$

$$= (3 \times 4) \times (3 \times 4)$$

$$= 144 \text{ cm}^2$$

Unit 8.4 – Length, Area and Volume of Cubes

Qn 1

$$\text{Volume of Cube B} = 1 \text{ unit} \times 1 \text{ unit} \times 1 \text{ unit} = 1 \text{ unit}^3$$

$$= 64 \text{ cm}^3$$

$$\text{Length of cube B} = 4 \text{ cm (since } 4 \times 4 \times 4 = 64)$$

$$\text{Length of Cube A} = 3 \times 4 \text{ cm} = 12 \text{ cm}$$

$$\text{Volume of cube A} = 12 \text{ cm} \times 12 \text{ cm} \times 12 \text{ cm} = 1728 \text{ cm}^3$$

$$\text{Difference in volume} = 1728 \text{ cm}^3 - 64 \text{ cm}^3 = 1664 \text{ cm}^3$$

Qn 2

$$\text{Volume of metal cube} = 8 \text{ cm} \times 8 \text{ cm} \times 8 \text{ cm}$$

$$= 512 \text{ cm}^3$$

$$\text{Volume of 1 cube} = 512 \text{ cm}^3 \div 64$$

$$= 8 \text{ cm}^3$$

$$2 \text{ cm} \times 2 \text{ cm} \times 2 \text{ cm} = 8 \text{ cm}^3$$

$$\text{Length of edge of smaller cube} = 2 \text{ cm}$$

Qn 3

$$\text{Since } L \times B \times H = 125 \text{ and } L = B = H$$

$$L = 5 \text{ cm}$$

$$\text{Area of shaded face}$$

$$= 5 \text{ cm} \times 5 \text{ cm}$$

$$= 25 \text{ cm}^2$$

Qn 4

$$L \times L = 81 \text{ cm}^2 \text{ (} 9 \text{ cm} \times 9 \text{ cm)}$$

$$L = 9 \text{ cm}$$

$$\text{Volume of cube} = 9 \text{ cm} \times 9 \text{ cm} \times 9 \text{ cm}$$

$$= 729 \text{ cm}^3$$

Qn 5

$$\text{Volume of cube X} = 27 \times 1 \text{ cm}^3 = 27 \text{ cm}^3$$

$$\text{Length of cube X} = 3 \text{ cm (since } 3 \times 3 \times 3 = 27)$$

Qn 6

Let the length of cube A be 2 units and length of cube B be 1 unit.

$$\text{Total surface area of A} = 2 \text{ units} \times 2 \text{ units} \times 6 = 24 \text{ units}^2$$

$$\text{Total surface area of B} = 1 \text{ unit} \times 1 \text{ unit} \times 6 = 6 \text{ units}^2$$

$$\text{Difference in total surface area} = 24 \text{ units}^2 - 6 \text{ units}^2$$

$$= 18 \text{ units}^2$$

$$18 \text{ units}^2 = 162 \text{ cm}^2$$

$$1 \text{ units}^2 = 162 \text{ cm}^2 \div 18 = 9 \text{ cm}^2$$

$$1 \text{ unit} = 3 \text{ cm (since } 3 \times 3 = 9)$$

$$\text{Length of cube A} = 2 \times 3 \text{ cm} = 6 \text{ cm}$$

$$\text{Volume of cube A} = 6 \text{ cm} \times 6 \text{ cm} \times 6 \text{ cm} = 216 \text{ cm}^3$$

Qn 7

$$\text{Volume of cube B} = 3 \text{ units} \times 3 \text{ units} \times 3 \text{ units} = 27 \text{ units}^3$$

$$27 \text{ units}^3 = 81 \text{ cm}^3$$

$$1 \text{ unit}^3 = 81 \text{ cm}^3 \div 27 = 3 \text{ cm}^3$$

$$\text{Volume of cube A} = 1 \text{ unit} \times 1 \text{ unit} \times 1 \text{ unit} = 1 \text{ unit}^3 = 3 \text{ cm}^3$$

Qn 8

$$\text{Volume of cube C} = 3 \text{ units} \times 3 \text{ units} \times 3 \text{ units} = 27 \text{ units}^3$$

$$\text{Volume of cube D} = 4 \text{ units} \times 4 \text{ units} \times 4 \text{ units} = 64 \text{ units}^3$$

$$64 \text{ units}^3 = 128 \text{ cm}^3$$

$$1 \text{ unit}^3 = 128 \text{ cm}^3 \div 64 = 2 \text{ cm}^3$$

$$\text{Volume of cube C} = 27 \times 2 \text{ cm}^3 = 54 \text{ cm}^3$$

Unit 8.5 – Volume and Area of Unit Cubes

Qn 1

$$\text{Volume} = (1 + 3 + 8) \times 1 \text{ cm}^3$$

$$= 12 \text{ cm}^3$$

Qn 2

$$\text{Volume of solid} = (1 + 2 + 3) \times 1 \text{ cm}^3$$

$$= 6 \text{ cm}^3$$

Qn 3

$$\text{Volume of solid} = (1 + 1 + 6) \times 1 \text{ cm}^3 \\ = \mathbf{8 \text{ cm}^3}$$

Qn 4

$$\text{Volume of solid} = (3 + 4) \times 1 \text{ cm}^3 \\ = \mathbf{7 \text{ cm}^3}$$

Qn 5

$$\text{Volume of solid} = (1 + 1 + 3 + 9) \times 1 \text{ cm}^3 \\ = \mathbf{14 \text{ cm}^3}$$

Qn 6

Front = 7 faces, Back = 7 faces, Left = 6 faces,
Right = 6 faces, Top = 9 faces, Bottom = 9 faces
Total = 44 faces

$$\text{Total area to be painted} = 44 \times 1 \text{ cm}^2 \\ = \mathbf{44 \text{ cm}^2}$$

Qn 7

Front = 8 faces, Back = 8 faces, Left = 9 faces,
Right = 9 faces, Top = 10 faces, Bottom = 10 faces
Total = 54 faces

$$\text{Total area to be painted} = 54 \times 1 \text{ cm}^2 \\ = \mathbf{54 \text{ cm}^2}$$

Qn 8

Front = 4 faces, Back = 4 faces, Left = 4 faces
Right = 4 faces, Top = 5 faces, Bottom = 5 faces
Total = 26 faces

$$\text{Total area to be painted} = 26 \times 1 \text{ cm}^2 \\ = \mathbf{26 \text{ cm}^2}$$

Unit 8.6 – Volume = Base Area x Height

Qn 1

$$\text{Height} = \frac{\text{Volume}}{\text{Base area}} \\ = \frac{84 \text{ cm}^3}{28 \text{ cm}^2} \\ = \mathbf{3 \text{ cm}}$$

Qn 2

$$\frac{2}{3} \text{ of tank} = 96\,000 \text{ cm}^3$$

$$\frac{1}{3} \text{ of tank} = 48\,000 \text{ cm}^3$$

$$\text{Full volume} = 48\,000 \text{ cm}^3 \times 3 \\ = 144\,000 \text{ cm}^3$$

$$\text{Height} = \frac{144\,000 \text{ cm}^3}{60 \text{ cm} \times 40 \text{ cm}} \\ = \mathbf{60 \text{ cm}}$$

Qn 3

$$\text{Time taken to fill the tank} = \frac{110 \times 90 \times 50}{16\,500} \\ = \mathbf{30 \text{ min}}$$

Qn 4

$$\text{Total volume} = 3.5 \times 1000 \times 5 \times 60 \\ = 1\,050\,000 \text{ cm}^3$$

$$\text{Depth at first} = \frac{1050000}{125 \times 84} \\ = \mathbf{100 \text{ cm}}$$

Qn 5

$$\text{In 1 min, both taps filled} = 140 \text{ cm}^3 + 100 \text{ cm}^3 \\ = 240 \text{ cm}^3$$

Time taken for both taps to completely fill the tank

$$= \frac{30 \times 24 \times 20}{240}$$

$$= \mathbf{60 \text{ min}}$$

Qn 6

$$\text{Volume of water leaked} = (400 + 300) \times 6 \\ = 4200 \text{ cm}^3$$

$$\text{Depth at first} = \frac{4200}{60 \times 10} \\ = 7 \text{ cm}$$

$$\text{New height} = 15 \text{ cm} - 7 \text{ cm} \\ = \mathbf{8 \text{ cm}}$$

Qn 7

(a) Volume of water at first

$$= \frac{4}{5} \times 40 \text{ cm} \times 30 \text{ cm} \times 25 \text{ cm} \\ = \mathbf{24\,000 \text{ cm}^3} \text{ or } \mathbf{24 \ell}$$

(b) Volume of water in glass tank = 24 000 – 4 000
= 20 000

$$\text{Height} = \frac{200}{50 \times 25} \\ = \mathbf{16 \text{ cm}}$$

Qn 8

Length = 3 units, breadth = 1 unit, height = 1.5 units
Half the height = 1.5 units ÷ 2 = 0.75 units = 6 cm

$$1 \text{ unit} = 6 \text{ cm} \div 0.75 = 8 \text{ cm}$$

$$\text{Volume of water in can hold} \\ = 3 \times 8 \text{ cm} \times 8 \text{ cm} \times 1.5 \times 8 \text{ cm} \\ = \mathbf{2304 \text{ cm}^3}$$